

North Dakota Geological Survey

Preliminary Results of Temperature Logging in the Williston Basin to determine Heat Flow

By

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Abstract

The North Dakota Geological Survey (NDGS) has embarked on a temperature survey of the Williston Basin, North Dakota. To date, 23 temporarily abandoned oil and gas wells have been logged using a memory tool equipped with a temperature, gamma-ray, and casing collar locator probe lowered by a slickline. Several methods were used to estimate heat flow at the various locations including calculations based on average laboratory values of thermal conductivity, existing heat flow maps, the Bullard Method, and finding the harmonic mean of thermal conductivity. Although there is general agreement in calculated heat flow values between the various methods presented above, the results are largely predicated upon initial assumptions of either heat flow, thermal conductivity, or both.

While we are confident in the measurements obtained during this study with respect to thermal gradient, additional information with regard to thermal conductivity of the geologic formations will be required to estimate heat flow within the Williston Basin with better accuracy. Geologic formations can often be differentiated on the basis of "marker" beds, but there can be wide variations in mineralogy, lithology, porosity, permeability, density, etc., depending upon depositional environment, depth of burial and secondary processes from one location to another which can profoundly influence thermal conductivity and therefore greatly affect the calculated heat flow.

Introduction

In 2014, the North Dakota Geological Survey (NDGS) initiated a temperature logging program in the Williston Basin. The primary goal of the program is to gain further insight into the thermal history of the basin that may result in the development of improved models for use in exploration for oil and natural gas (Prensky, 1992). The program has also been designed to gather data useful in the evaluation of the geothermal potential of the Williston Basin. Insight into the timing of petroleum generation, migration, accumulation and preservation can be gained by determining the thermal maturity of hydrocarbons and/or by using the paleoheat flux of a sedimentary basin (Nuccio and Barker, 1990). Subsurface temperature is important to understanding the origin and evolution of sedimentary basins and can also be used in the determination of important kinetic factors as described by Nordeng and Nesheim (2011) and Nordeng (2012, 2013, 2014) that can ultimately be used to predict the oil generation potential of various geologic formations within the Williston Basin. These heat flow values represent critical data that are needed to validate and, where needed, update current heat flow maps (Blackwell and Richards, 2004). Heat flow together with thermal conductivity values of subsurface rocks, can be used to estimate subsurface temperatures at other locations and depths. This information can also be used in the evaluation, assessment and possible exploration and development of geothermal energy in the Williston Basin.

Methodology

While subsurface temperatures are routinely collected during logging and drill stem tests, true formation temperatures are rarely recorded because drilling, well completion and production operations can cause significant variations in the wellbore temperature from the actual temperature of the neighboring strata. These temperature differences can persist for days or

weeks after drilling or production has ceased. For example, during drilling, the circulation of drilling mud can cool the rock, during completion operations curing of cement and acidizing are exothermic reactions that can heat the rock, and gas entering the wellbore during production cools by expansion. In order to confidently obtain accurate subsurface temperatures, care must be taken to assure that the well bore and formation temperatures are the same, i.e. that the temperatures have equilibrated. A number of correction schemes have been derived to account for variations between actual formation temperatures and the measured wellbore temperatures obtained during drilling or while the well is producing such as that developed by Cooper and Jones (1959) or the Horner Method (Lachenbruch and Brewer, 1959). However, the best alternative is to make use of well bores that have been idle for months or, if possible, years so that equilibrated temperatures have been reached. Given these constraints and a review of the pertinent literature, the NDGS concluded that wells that have been temporarily abandoned and undisturbed for at least three months would meet the requirements of this study.

The project consisted of lowering a GOWell Model GTC43C Pegasus[®] temperature probe with an accuracy of 0.5°C into 23 temporarily abandoned oil and gas wells to the bottom of the well (depth of the plug). The tool included a memory controller sub and was lowered by means of a 0.092 inch “slickline” (nonconductive cable) operated by Gibson Energy Inc. (WISCO division). The depth of the logging runs ranged between approximately 3,000 feet (915 m) and 13,000 feet (3960 m). The wells were selected based on location, depth, length of time of being undisturbed, and the ability to obtain permission from the current well operators to perform the logging. Locations of the wells are shown in Figure 1.

After setting the equipment up over a well (Figures 2 and 3), a gauge ring (dummy or slug) was lowered down to verify that there were no obstructions within the wellbore and to determine the maximum depth that could be logged for wells that still contained production tubing or where other potential obstructions might exist within the wellbore. After removal of the gauge ring, a period of time (generally on the order of an hour or more) was allowed to elapse in order for the well fluid temperatures to re-equilibrate before lowering the logging tools. For wells that were known to not contain production tubing, the gauge ring was not deployed. The wells were then logged as the tool was lowered into the well to minimize temperature disturbance or mixing of the fluids arising from the displacement of fluids by the volume of the tool. In addition to temperature, the tool was also equipped with a Casing Collar Locator (CCL) and a Gamma Ray probe to aid in correlation of the temperature probe with depth and with the geologic formations (Figure 4). As noted above, a memory controller sub was used which recorded the probe readings at a rate of one reading every 40 milliseconds (ms). The readings were downloaded to a computer after the tool was brought back to the surface. For comparison purposes, the wells were also logged on the way out of the wellbore. Temperature versus depth profiles of all the wells are presented in Appendix A.

It should be noted that for two of the wells, the Capa Madison Unit H-205 (NDIC #1140) and the Frink 13-15 (NDIC #13132), it is postulated that paraffin may have interfered with the temperature readings by clogging the window of the temperature probe pictured in Figure 5. Paraffins are a white or colorless soft solid that consist of a mixture of hydrocarbon molecules

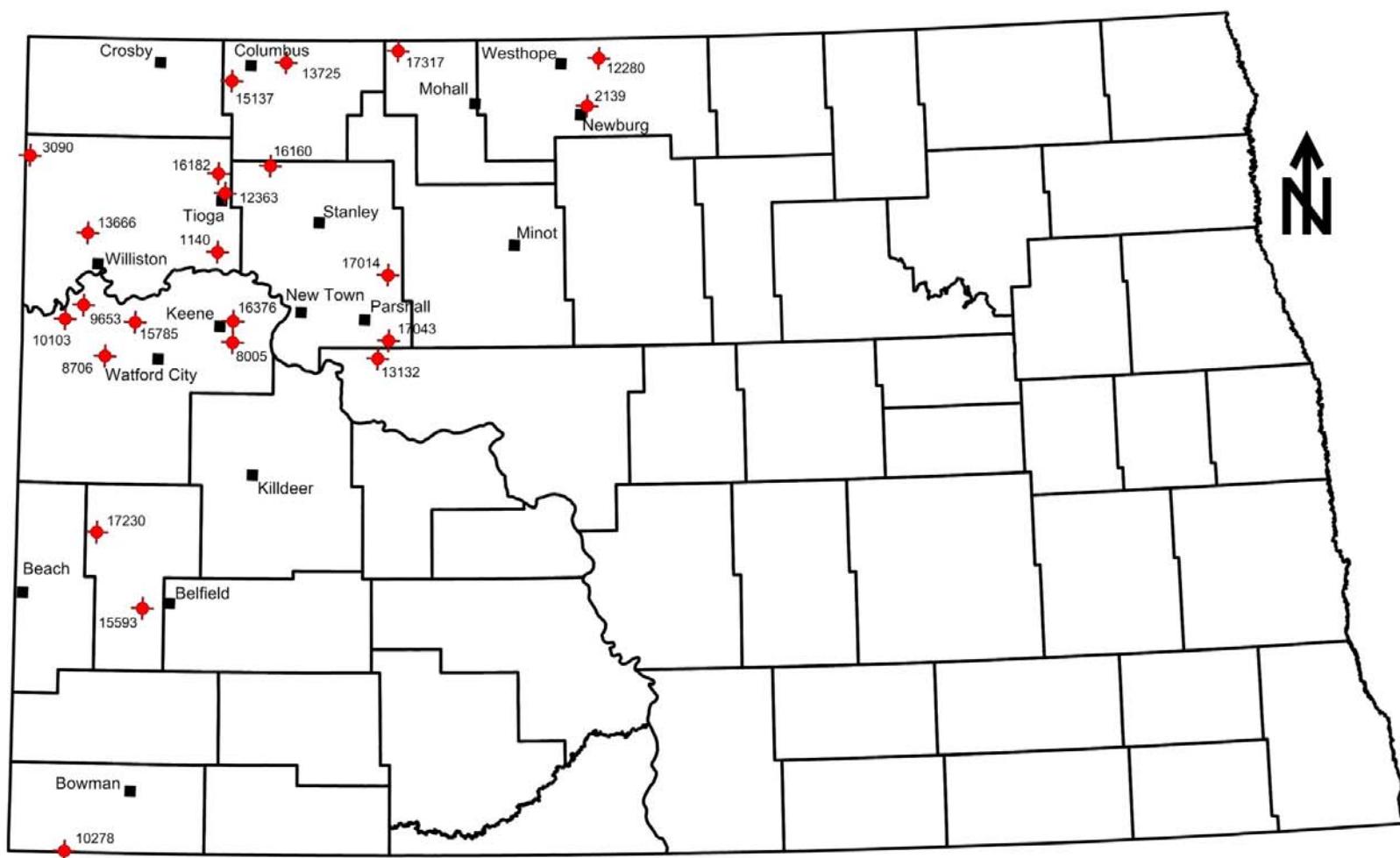




Figure 2. Connecting the tool to the slickline. From left to right: Mike Harden, WISCO, David Smith, WISCO, Jay Jamali, GOWell, and Kevin Hammer, WISCO.



Figure 3. Slickline unit set up over NDIC Well # 12363, Astrid Ongstad 14-22 north of Tioga, ND.

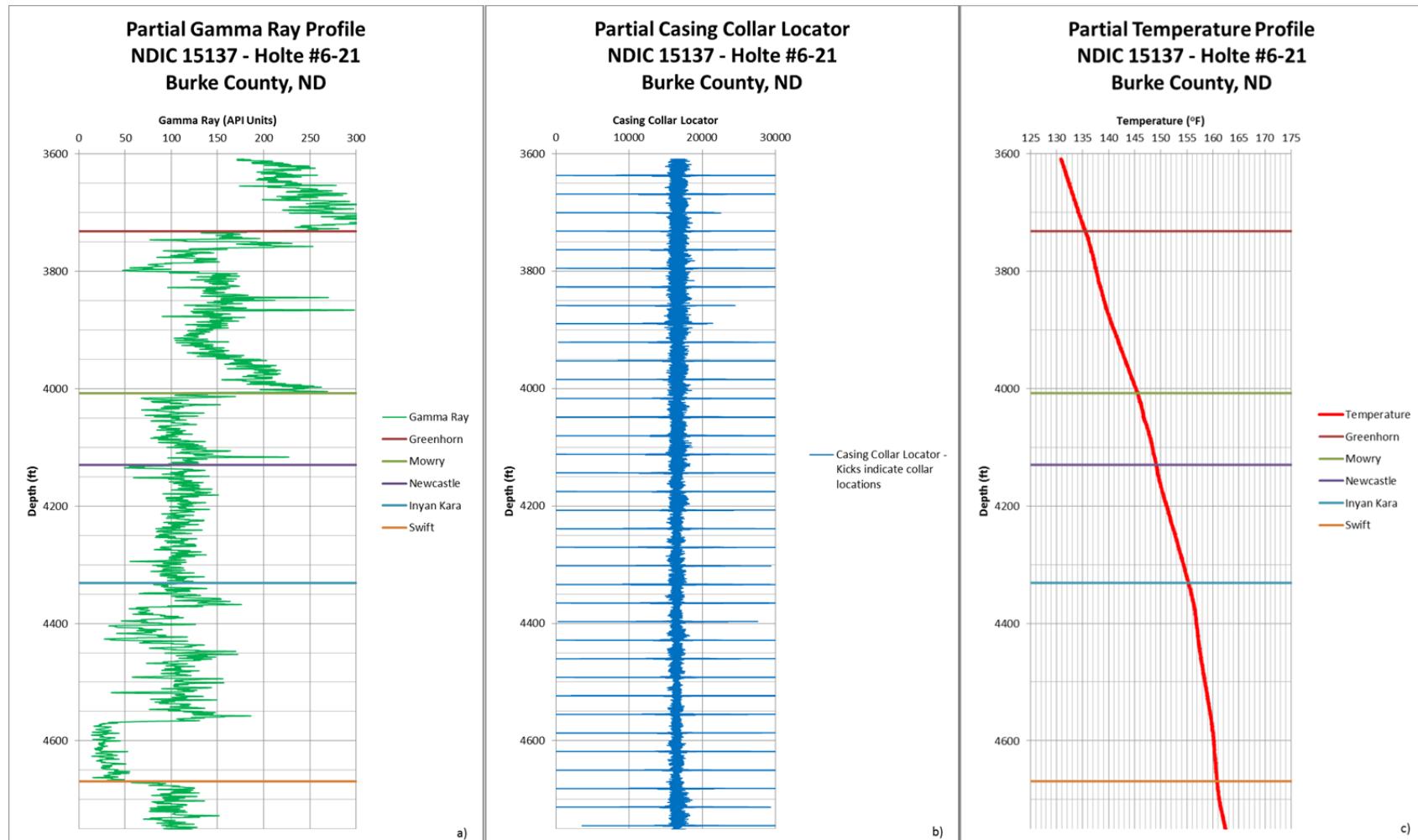


Figure 4. Partial profiles of the Holte #6-21 well: a) partial gamma ray profile illustrating formation top picks; b) partial casing collar locator profile; c) partial temperature gradient profile with formation top picks.

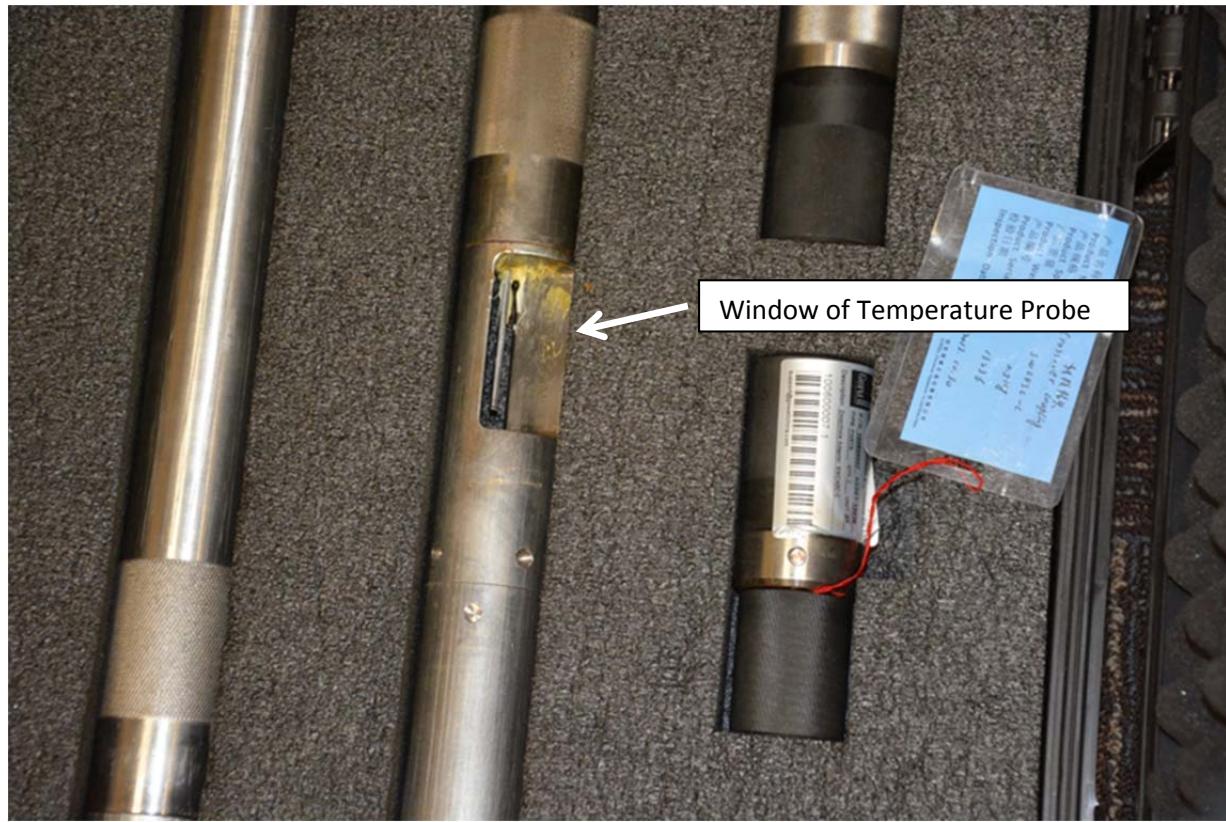


Figure 5. Window of Temperature Probe that may have been clogged by paraffins at two of the wells.

containing between twenty and forty carbon atoms. They are solid at room temperature and begin to melt above approximately 99 °F (37 °C). In these cases the up-hole readings were used for that portion of the profile that appeared to be influenced by the paraffin. Figure 6 shows the downhole and uphole temperature profiles of the Capa Madison Unit H-205 well illustrating how the temperatures appear to have been influenced.

Gradient or station stops were also made as the tool was lowered into the wells. In the first few wells, these stops were made more frequently (every 2000 ft) to ascertain the response time of the tool in an effort to optimize the logging speed and to obtain an indication of the tool precision. An example of one of the gradient stops is presented as Figure 7 and graphs and statistical calculations of all of the gradient stops for all of the wells are included in Appendix B. Once a reasonable logging speed was determined (60 ft/min provided good results), a ten minute gradient stop was typically made at the approximate midpoint of the well and at the bottom of the logging interval for the remaining wells.

Formation thicknesses were determined by initially using depths of formation tops as determined by the NDGS. This information was obtained from the North Dakota Industrial

Temperature Profile
NDIC 1140 - Capa Madison Unit H-205
Williams County, ND

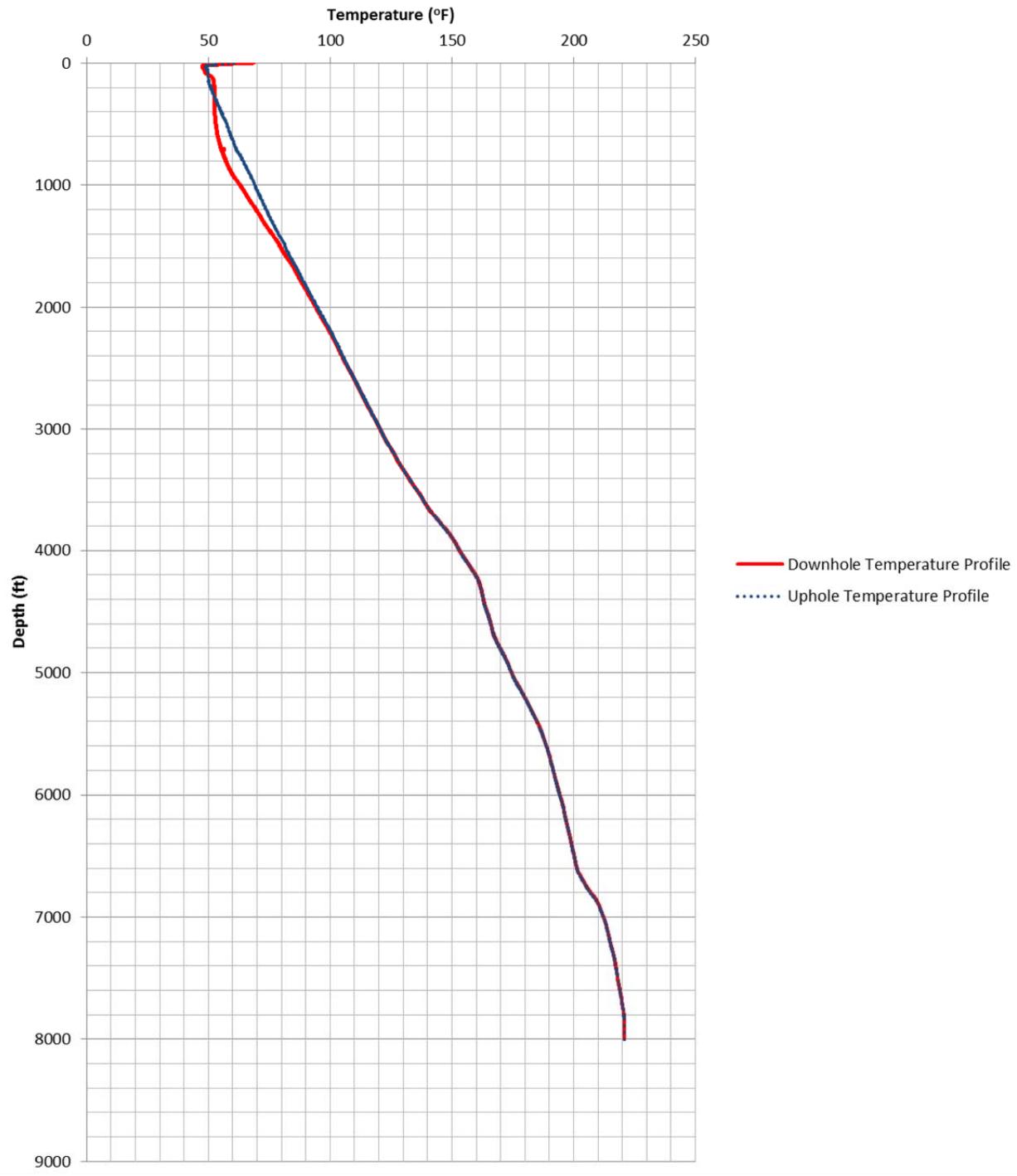


Figure 6. Downhole and Uphole Temperature Profiles of the Capa Madison H-205 well showing potential influence of paraffins clogging the temperature probe window.

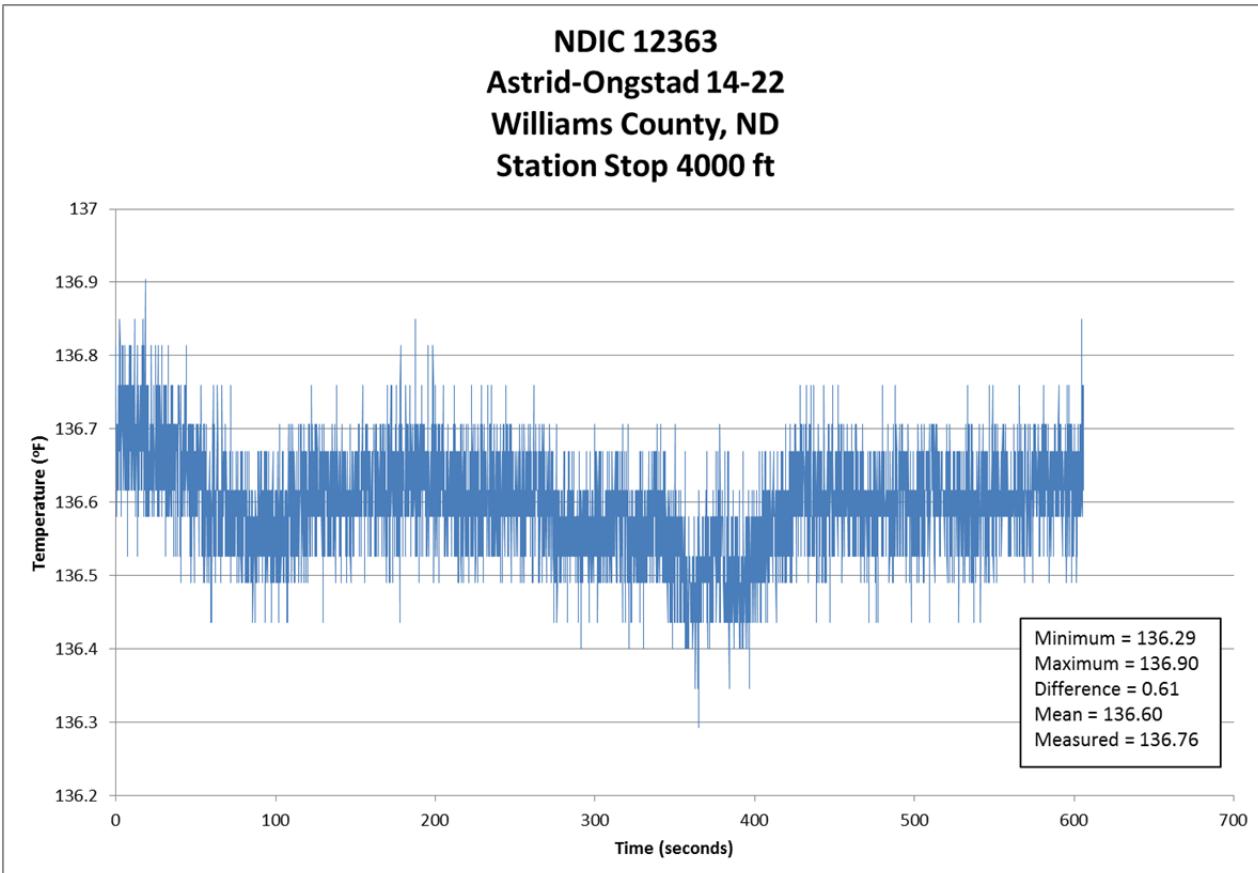


Figure 7. Variation of temperature vs. time at station stop at 4000 ft (1220 m) for NDIC well #12363 – Astrid-Ongstad 14-22 in Williams County, ND.

Commission's (NDIC) Scout Ticket database (<https://www.dmr.nd.gov/oilgas/subscriptionservice.asp>). Formation thicknesses were subsequently adjusted by making corrections for Kelly busing elevations and evaluating the gamma-ray profile from each well to select formation tops. The formation tops have been graphical depicted with the temperature profiles that are presented in Appendix A.

The relationship between heat flow, thermal conductivity, and temperature gradient can be expressed by Fourier's Law:

$$q = \lambda \Delta T / \Delta Z, \quad (1)$$

where: q = conductive heat flow;
 λ = thermal conductivity; and
 $\Delta T / \Delta Z$ = temperature gradient (change of temperature over change in depth).

As presented by Nordeng (2014), this equation can be re-arranged as:

$$\Delta T = q \Delta Z / \lambda. \quad (2)$$

Estimates of the temperature at depth (T_n) are found by adding the temperature changes ($\Delta T_i = QZ_i / \lambda_i$) associated with each deeper stratigraphic unit ($i=1\dots n$) to the “average” surface temperature (T_o) as follows:

$$T_n = T_o + q (Z_1 / \lambda_1 + Z_2 / \lambda_2 + \dots + Z_n / \lambda_n), \quad (3)$$

where:

n = number of overlying stratigraphic units in the section, where $i = 1\dots n$ (the deepest layer);

T_n = temperature at the base of the n^{th} unit;

T_o = average surface temperature;

Z_n = thickness of the n^{th} unit;

λ_n = thermal conductivity of the n^{th} layer.

Thus, to calculate the temperature at any point, it is necessary to know the average surface temperature, the thickness of the units (obtained from well logs), the thermal conductivities of the formations (obtained from the literature or direct measurements, e.g. Gosnold et al., 2012), and the conductive heat flow for the area (obtained from current heat flow maps, such as Blackwell and Richards, 2004). Although reasonable estimates of the average surface temperature and approximate thicknesses of the formations across the basin can be made, the biggest sources of error are caused by using inaccurate thermal conductivities or by assuming incorrect values of heat flow as current maps are based on a relatively limited dataset.

Therefore, several methods were employed to calculate the heat flow for each of the wells using variations of equation 1, such that improved estimates of T_n can be made across the Williston Basin from equation (3). Initially, the temperature gradients measured in the wells that were logged and previously published values of thermal conductivity laboratory measurements, other literature values, and/or empirical estimates (Gosnold et al., 2012) were utilized to calculate the heat flow. The first method used was to match the graphical temperature gradient with assumed thermal conductivity and heat flow values using equation (3) above. Initially, heat flow was adjusted using the thermal conductivity values from the closest well as presented by Gosnold et al. (2012), and temperature at depth was modeled. Heat flow values were adjusted using a number of trials until the modeled temperatures were reasonably close to the measured values, as illustrated in Figure 8.

After a close match was obtained, the thermal conductivity values of each formation were incrementally adjusted until the modeled temperatures fell close to the measured profile. These thermal conductivity values were then used in the other three methods and corresponding algorithms to calculate heat flow as described below. It should be noted that the

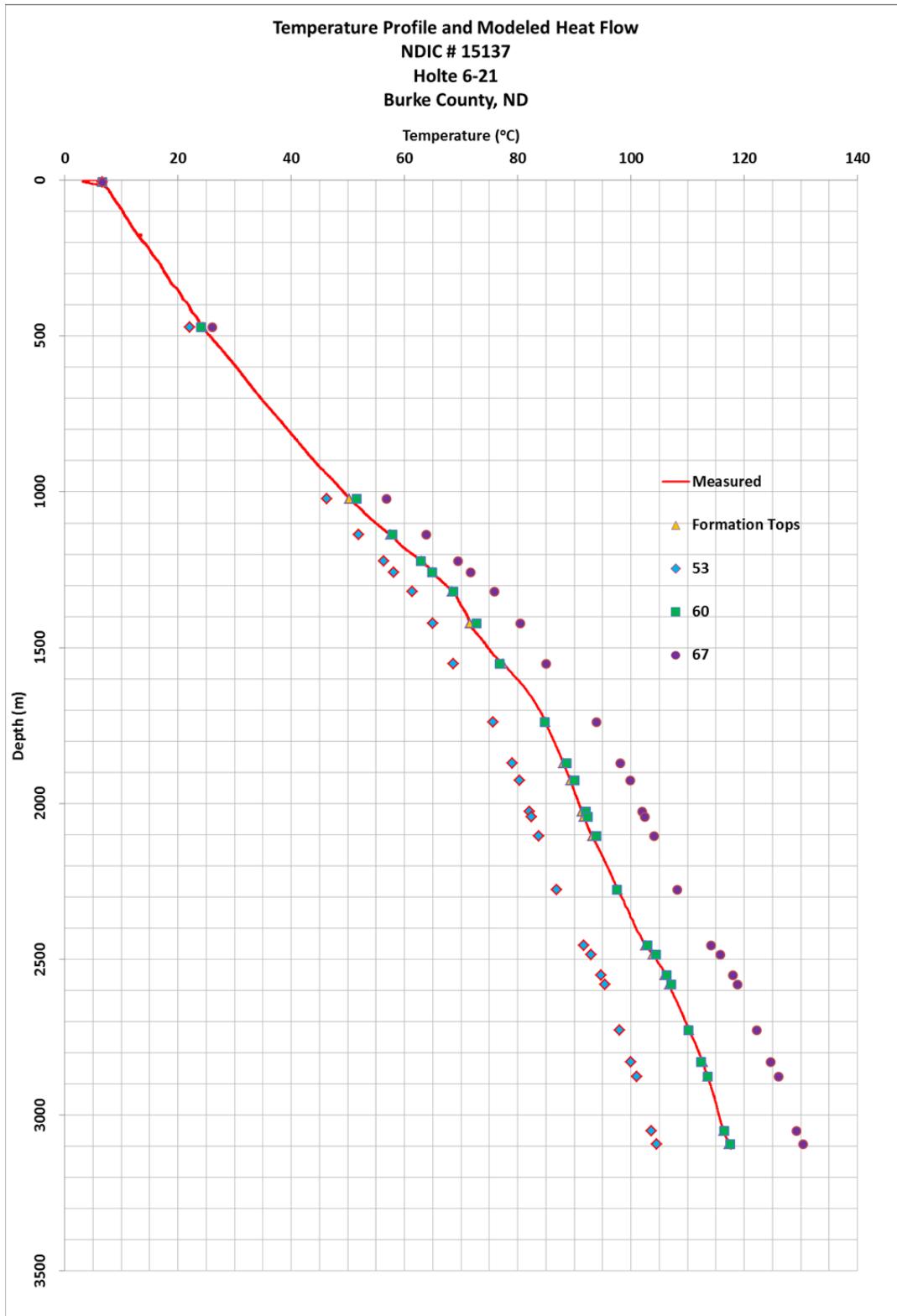


Figure 8. Measured temperature profile and modeled estimates using various assumed heat flow values. After a close was match is obtained, values of thermal conductivity are adjusted to further refine/match the measured profile. Heat flow units are mW m^{-2} .

heat flow of the upper 3000 to 5000 ft (1 to 1.5 km) was adjusted by a factor of about 90% to account for cooler surface temperatures during recent glacial periods and subsequent post-glacial warming per Majorowicz et al. (2012) and Gosnold et al. (2011). The graphical results of all of the wells are included as Appendix C.

The second method used equation (1) and heat flow for each formation was calculated using the thermal conductivities from the graphical method discussed above, and initial formation thickness as determined by the gamma-ray profile correlations discussed above. An average heat flow for all of the formations was then calculated. A weighted average was also determined by calculating a weighted thermal conductivity on the basis of formation thickness divided by the total well depth:

$$q = \lambda_w (\Delta T_t / \Delta Z_t); \text{ and} \quad (4)$$

$$\lambda_w = \lambda_1 * \Delta Z_1 / \Delta Z_t + \lambda_2 * \Delta Z_2 / \Delta Z_t + \dots + \lambda_n * \Delta Z_n / \Delta Z_t, \quad (5)$$

where:

λ_w = weighted thermal conductivity;

ΔT_t = temperature change from surface to bottom of well;

ΔZ_t = total depth of well; and

n, Z_n , and λ_n are as before.

An example of the results is presented in Table 1. In addition, for comparison purposes, average heat flow and weighted heat flow estimates were calculated using the thermal conductivity values utilized by Nordeng and Nesheim (2011) and Nordeng (2014), the results of which are also presented in Table 1. Nordeng arrived at his thermal conductivity values by utilizing a digitized version of the North American heat flow map published by Blackwell and Richards (2004) and back calculating the thermal conductivity values for each formation from the Rauch Shapiro Fee #21-9 well (NDIC #7591) located in Billings County, North Dakota.

The third approach employed the methodology of Bullard (1939), as cited by Beardsmore and Cull (2001). This method uses what Bullard refers to as the Thermal Resistance (R) plotted against the temperature. The thermal resistance is defined as:

$$R_i = R_{(i-1)} + \Delta Z_i / \lambda_i, \quad (6)$$

where:

R_i = thermal resistance of formation i;

ΔZ_i = depth range (formation thickness); and

λ_i = formation thermal conductivity.

Heat flow is determined by calculating the slope of the best fit line of temperature versus thermal resistance as illustrated in Figure 9. As in method 1, separate slopes were calculated for

Table 1. Heat Flow Calculations for the Vernie Chapin 13-21 Well (NDIC #16376) in McKenzie County, ND.

Formation	Depth (z)	ΔZ	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta Z/\lambda$	R_i	λ_{hi}^5	grad _i	Q_{graph}^6	Q_2^7	Q_N^8	$Q_{Bullard}^9$	Q_{hi}^{10}
	(m)		(°C)														
FU/HC/FH ¹¹	0.0	503.2	5.2	22.5	1.40	1.72	0.18	0.22	359.45	359.45			62.5	76.8			
Pierre	503.2	783.6	27.6	39.8	1.15	1.62	0.23	0.32	681.43	1040.87	0.48	44.65	58.4	82.3		21.6	
Greenhorn	1286.9	125.0	67.4	8.1	1.10	1.62	0.03	0.05	113.61	1154.48	1.11	48.38	71.2	104.8		53.9	
Mowry	1411.8	29.0	75.5	1.6	1.20	1.80	0.01	0.01	24.13	1178.61	1.20	49.82	64.7	97.0		59.7	
Newcastle	1440.8	79.9	77.1	4.5	1.50	1.80	0.03	0.04	53.24	1231.85	1.17	49.90	85.3	102.3		58.4	
Inyan Kara	1520.6	107.9	81.6	3.0	1.60	2.35	0.04	0.06	67.44	1299.29	1.17	50.27	43.9	64.5		58.8	
Swift	1628.5	179.2	84.6	7.0	1.40	2.10	0.06	0.10	128.02	1427.30	1.14	48.76	54.5	81.8		55.6	
Rierdon	1807.8	151.5	91.6	6.0	1.60	2.10	0.06	0.08	94.68	1521.98	1.19	47.78	63.1	82.8		56.8	
Spearfish	1959.3	155.8	97.5	3.6	2.40	3.04	0.09	0.12	64.90	1586.88	1.23	47.14	54.7	69.3		58.2	
Opeche	2115.0	126.5	101.1	2.6	2.20	3.04	0.07	0.10	57.50	1644.37	1.29	45.34	44.8	62.0		58.3	
Amsden	2241.5	82.6	103.7	1.7	3.80	3.04	0.08	0.06	21.74	1666.11	1.35	43.93	76.4	61.1		59.1	
Tyler	2324.1	69.2	105.3	4.3	1.60	2.68	0.03	0.05	43.24	1709.35	1.36	43.09	99.2	166.1		58.6	
Big Snowy	2393.3	104.5	109.6	3.3	1.40	3.62	0.04	0.10	74.68	1784.03	1.34	43.63	43.7	112.9		58.5	
Kibbey	2497.8	47.2	112.9	1.0	2.70	3.62	0.03	0.04	17.50	1801.53	1.39	43.11	55.9	74.9		59.8	
Madison	2545.1	187.8	113.8	3.3	3.05	3.45	0.14	0.16	61.56	1863.09	1.37	42.70	53.0	59.9		58.3	
Ratcliffe	2732.8	75.3	117.1	1.6	3.05	3.45	0.06	0.07	24.68	1887.77	1.45	40.96	65.7	74.3		59.3	
Frobisher	2808.1	183.2	118.7	4.5	2.80	3.45	0.13	0.16	65.42	1953.19	1.44	40.44	68.9	84.9		58.1	
Lodgepole	2991.3	243.8	123.2	7.3	2.30	3.45	0.14	0.21	106.02	2059.21	1.45	39.47	69.1	103.6		57.3	
Bakken	3235.1	35.1	130.6	1.5	1.00	4.00	0.01	0.04	35.05	2094.26	1.54	38.75	43.4	173.7		59.9	
Three Forks	3270.2	59.4	132.1	1.6	2.70	4.00	0.04	0.06	22.01	2116.28	1.55	38.80	74.4	110.3		60.0	
Birdbear	3329.6	25.3	133.7	0.6	2.80	4.00	0.02	0.03	9.04	2125.31	1.57	38.60	63.9	91.4		60.5	
Duperow	3354.9	125.9	134.3	3.0	2.60	4.00	0.08	0.13	48.42	2173.73	1.54	38.49	61.4	94.4		59.4	
Souris River	3480.8	79.6	137.3	2.0	2.80	3.09	0.06	0.06	28.41	2202.14	1.58	37.95	68.6	75.7		60.0	
Dawson Bay	3560.4	32.0	139.2	0.8	2.75	3.09	0.02	0.02	11.64	2213.78	1.61	37.65	65.4	73.5		60.5	
Prairie	3592.4	86.9	140.0	1.7	4.00	2.18	0.09	0.05	21.72	2235.50	1.61	37.52	76.7	41.8		60.3	
Winnipegosis	3679.2	34.4	141.6	0.9	2.99	2.83	0.03	0.02	11.52	2247.01	1.64	37.09	75.7	71.7		60.7	
Ashern	3713.7	36.3	142.5	1.0	2.99	2.83	0.03	0.03	12.13	2259.15	1.64	36.98	83.8	79.3		60.8	
Interlake	3750.0	211.2	143.5	4.6	3.77	3.72	0.20	0.20	56.03	2315.17	1.62	36.90	81.2	80.1		59.8	
BOH	3961.2		148.1														
							$\Sigma =$	2.03	2.58								
Notes												Average	65.3	87.6	61	57.5	
1 - Thermal conductivity derived from graphical method												Wtd Average	73.3	93.0			
2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)												Shallow			58.4	37.8	
3 - Weighted average of graphical thermal conductivity												Deep	60		60.3	59.1	
4 - Weighted average of Nordeng's thermal conductivity																	
5 - Harmonic mean of thermal conductivity																	
6 - Heat flow derived from graphical method																	
7 - Heat flow derived from Equation 1 for each formation																	
8 - Heat Flow derived from Equation 1 and Nordeng's λ																	
9 - Heat flow derived from Bullard's Method																	
10 - Heat flow derived using harmonic mean method																	
11- FU/HC/FH - Fort Union Group/Hell Creek Formation/Fox Hills Formation combined																	

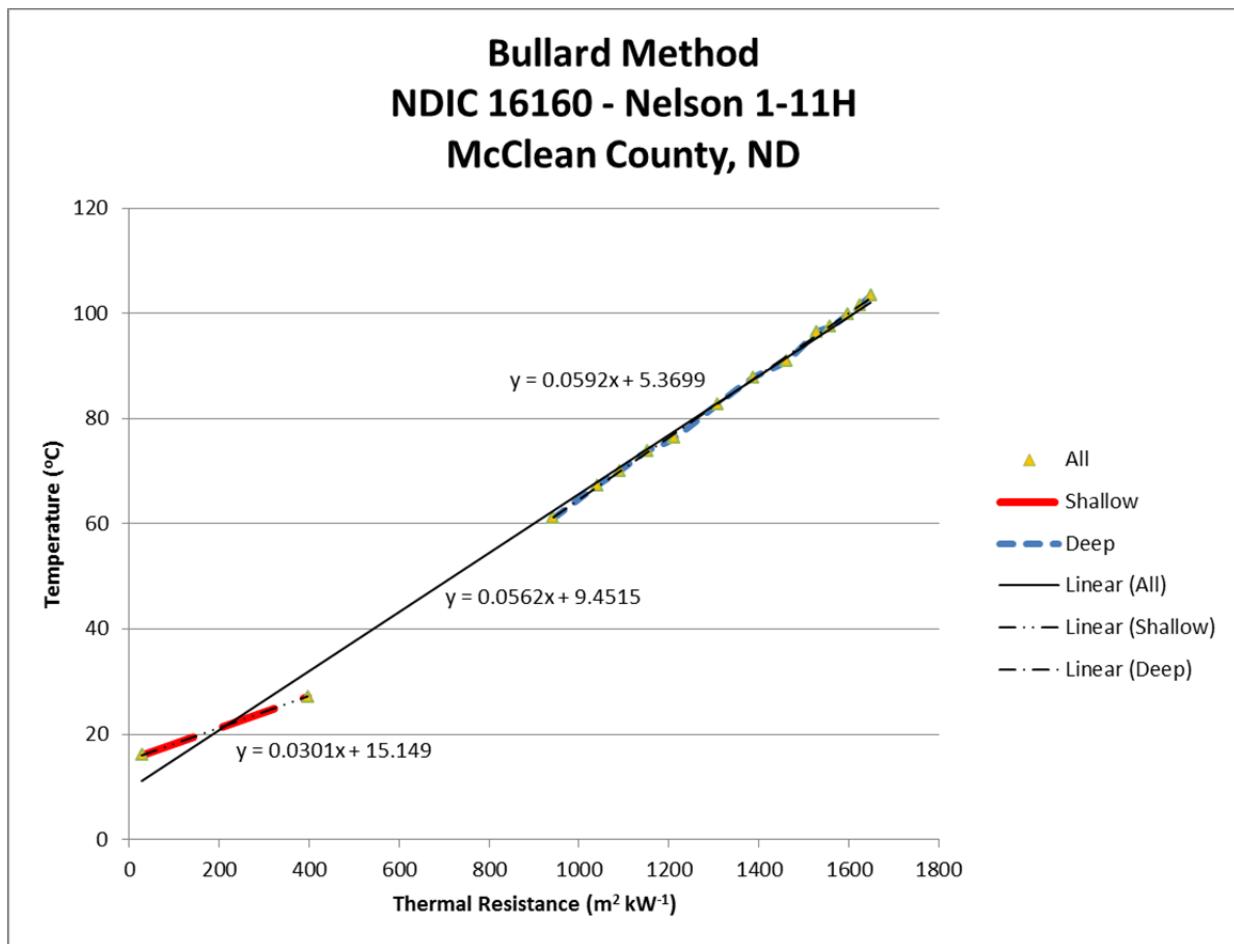


Figure 9. Example of a Bullard Plot. Slope of best fit line is the heat flow.

the shallow portions (upper 1 to 1.5 km) of the well bore that have been influenced by Pleistocene glacial climates and deeper portions that may be more representative of heat flow within the basin that has not been influenced by climatic changes. Results of example calculations are presented in Table 1.

The last method employed to estimate heat flow was to determine the harmonic mean of the thermal conductivity as described by Beardmore and Cull (2011). This method calculates the harmonic mean of the thermal conductivity by dividing the depth to the top of each formation by the thermal resistance calculated using equation (6):

$$\lambda_{hi} = Z_i/R_i \quad (7)$$

where:

λ_{hi} = harmonic mean thermal conductivity;

Z_i = depth to top of formation; and

R_i = as above.

Next, the gradient is determined by dividing the difference between the temperature at the top of the formation and the temperature at the top of the stratigraphic column by the difference between the depth to the top of the formation and the depth to the top of the stratigraphic column under consideration:

$$\text{grad}_i = (T_i - T_s) / (Z_i - Z_s), \quad (8)$$

Where:

grad_i = temperature gradient to top of formation i ;
 T_i = temperature at top of formation i ;
 T_s = temperature at top of stratigraphic column;
 Z_i = depth to top of formation i ; and
 Z_s = depth to top of stratigraphic column.

Heat flow for each formation is then calculated by taking the product of harmonic thermal conductivity times the gradient:

$$q_{hi} = \lambda_{hi} * \text{grad}_i. \quad (9)$$

An example calculation is provided in Table 1 and summaries of the complete results are presented in Table 2. Tables of the calculations for each method are attached as Appendix D. Figure 10 presents a map showing the average of the values obtained from the graphical, harmonic mean, Bullard and the weighted average methods. Figure 11 presents the same results (colors) overlain by a structure contour map (contour lines) of the top of the Three Forks Formation from data obtained from the NDIC database.

Discussion and Conclusions

Results of the preliminary study are presented in Table 2. While there is general agreement in calculated heat flow values between the various methods presented above, the results are largely predicated upon initial assumptions of either heat flow, thermal conductivity, or both. This is clearly illustrated by the large discrepancies between the values obtained by using Nordeng's thermal conductivity values and the values obtained using the other methods. In addition, the average and weighted average of method 2 results in relatively large differences in heat flow between formations. With the exception of the surface temperature forcing signal resulting from global climatic variations during the last ice age and subsequent post-glacial warming, calculated heat flow across the various formations should be nearly equivalent, if the thermal conductivity values used in the analyses are close to actual values.

The results of the harmonic method described above seem to yield the most consistent heat flow values between the formations (Table 1). However this issue still reduces down to a "chicken or egg" scenario in that heat flow and thermal conductivity are dependent upon each other and inaccurate assumptions of one profoundly affects the other. While we are confident in the measurements obtained during this study with respect to thermal gradients, it is evident that additional information with regard to thermal conductivities of the geologic formations will

Table 2. Summary of Heat Flow Estimates by Well

Well #	Well Name		Tabular	Nordeng's	Bullard	Harmonic	Graphical	Average	Use
			mW m ⁻²						
2139	NSCU V-706	Average	43.0	66.5		44			
	Northeast of Newburg, ND	Wtd Avg.	46.7	74.6					
		Shallow ^a				23.2			
		Deep			47.5	44.5	48	46.7	46.7
8005	Sivertson 29-23R1	Average	62.2	80.9		61.5			
	Southeast of Keene, ND	Wtd Avg.	76.2	94.4					
		Shallow				43.9			
		Deep ^c			61.3	63.0	60.3	61.7	61.7
16376	Vernie Chapin 32-21	Average	65.3	87.6		56.8			
	Southeast of Keene, ND	Wtd Avg.	73.3	93.0					
		Shallow				37.8			
		Deep			61.0	59.1	60.0	61.4	61.4
9653	Cutlip #1	Average	49.3	75.4		45.9			
	Northwest of Alexander, ND	Wtd Avg.	52.0	74.8					
		Shallow				33.0			
		Deep			47.9	47.6	48.0	48.2	48.2
10103	Iverson State A-1	Average	49.9	76.3		52.7			
	Northwest of Alexander, ND	Wtd Avg.	54.9	74.9					
		Shallow				43.3			
		Deep			52.1	54.2	50.2	51.6	51.6
12363	Astrid-Ongstad	Average	54.2	82.2		51.4			
	Northeast of Tioga, ND	Wtd Avg.	61.1	87.2					
		Shallow				38.6			
		Deep			52.7	52.7	52.0		52.9
16182	2004 JV-P NDCA 7	Average	53.8	86.5		45.8			
	North of Tioga, ND	Wtd Avg.	56.6	85.2					
		Shallow				33.1	44.1		
		Deep			50.4	47.8	49.0		50.3
13666	Rieder 1-9 SWD	Average	49.8	79.4		45.0			
	North of Williston, ND	Wtd Avg.	52.1	77.9					
		Shallow				34.5			
		Deep			48.0	46.7	48.5	48.3	48.3
15137	Holte 6-21	Average	60.0	87.1		58.0			
	Southwest of Columbus, ND	Wtd Avg.	70.3	90.0					
		Shallow			55.6	57.8			
		Deep			60.8	60.4	60.0	60.3	60.3
15593	FHMU K-810	Average	60.5	87.9		52.4			
	West of Fryburg, ND	Wtd Avg.	64.1	86.2					
		Shallow			55.8	37.9			
		Deep			58.8	55.3	58.0	58.2	58.2
17043	St. Andes 151-89-2413H-1	Average	41.6	60.8		40.1			
	Southeast of Parshall, ND	Wtd Avg.	52.3	69.5					
		Shallow				28.3			
		Deep			41.5	40.5	42.0	41.4	41.4
13132	Frink 13-15	Average	39.7	63.4		34.2			
	South of Parshall, ND	Wtd Avg.	43.1	61.8					
		Shallow				13.3			
		Deep			39.9	38.4	40.0	39.5	39.5
16160	Nelson 1-11H	Average	78.3	110.3		51.5			
	South of Powers Lake, ND	Wtd Avg.	64.7	80.4					
		Shallow			30.1	24.0			
		Deep			59.2	56.1	59.0	58.1	58.1

Notes: a - Shallow is the upper 1 to 1.5 km that may reflect influence of Paleoclimate and subsequent post-glacial warming.

b - Glacial periods may reduce heat flow by 10 to 15% per Majorowicz et al. (2012) and Gosnold et al. (2011).

c - Deep are values calculated below 1 to 1.5 km

Table 2 (cont.) Summary of Heat Flow Estimates by Well

Well #	Well Name		Tabular	Nordeng's	Bullard	Harmonic	Graphical	Average	Use
			mW m ⁻²						
17317	E-M Emmel 10-3	Average	60.9	78.7		49.9			
	West of Sherwood, ND	Wtd Avg.	73.3	84.8					
		Shallow			56.1	13.7			
		Deep			56.8	53.7	59.0	57.6	57.6
12280	Brandjord 1-20	Average	45.2	68.8					
	East of Westhope, ND	Wtd Avg.	51.7	73.7					
		Shallow							
		Deep			52.7	49.8	54.0	52.0	52.0
1140	Capa-Madison Unit H-205	Average	75.2	93.5		58.1			
	South of Tioga, ND	Wtd Avg.	85.8	101.6					
		Shallow			39.2	10.5			
		Deep			68.2	65.4	71.0	68.2	68.2
8706	Berge C 1	Average	51.5	77.5		46.8			
	Southeast of Alexander, ND	Wtd Avg.	56.0	81.0					
		Shallow				32.4			
		Deep			50.8	48.9	52.0	50.8	50.8
17230	Roosevelt Federal 2-4H	Average	56.8	75.7		48.9			
	Northeast of Beach, ND	Wtd Avg.	63.1	82.3					
		Shallow			54.3	29.6			
		Deep			52.7	51.2	55.0	53.9	53.9
15785	Ann 1	Average	52.5	77.8		45.2			
	North of Arnegard, ND	Wtd Avg.	59.3	81.3					
		Shallow			49.3	17.6			
		Deep			50.9	50.0	52.0	51.4	51.4
10278	Mud Buttes State 1-36	Average	53.9	76.0		47.8			
	South of Rhame, ND	Wtd Avg.	59.5	84.0					
		Shallow				41.7			
		Deep			52.2	49.3	52.0	51.8	51.8
17014	Edwards 1-33BH	Average	48.9	70.2		34.0			
	Northwest of Plaza, ND	Wtd Avg.	48.5	66.4					
		Shallow			37.1	26.1			
		Deep			41.0	38.6	40.0	39.9	39.9
3090	Grenora-Madison Unit 08	Average	43.1	73.6	45.5	43.1			
	Southwest of Grenora, ND	Wtd Avg.	45.6	74.2					
		Shallow			44.6	25.6			
		Deep			44.0	47.9	45.5	45.1	45.1
13725	JC Wodds 26H-1	Average	50.8	76.4	52.2	38.8			
	North of Lignite, ND	Wtd Avg.	53.8	78.7					
		Shallow			50.6	25.4			
		Deep			53.6	48.9	54.0	51.8	51.8

Notes: a - Shallow is the upper 1 to 1.5 km that may reflect influence of Paleoclimate and subsequent post-glacial warming.

b - Glacial periods may reduce heat flow by 10 to 15% per Majorowicz et al. (2012) and Gosnold et al. (2011).

c - Deep are values calculated below 1 to 1.5 km

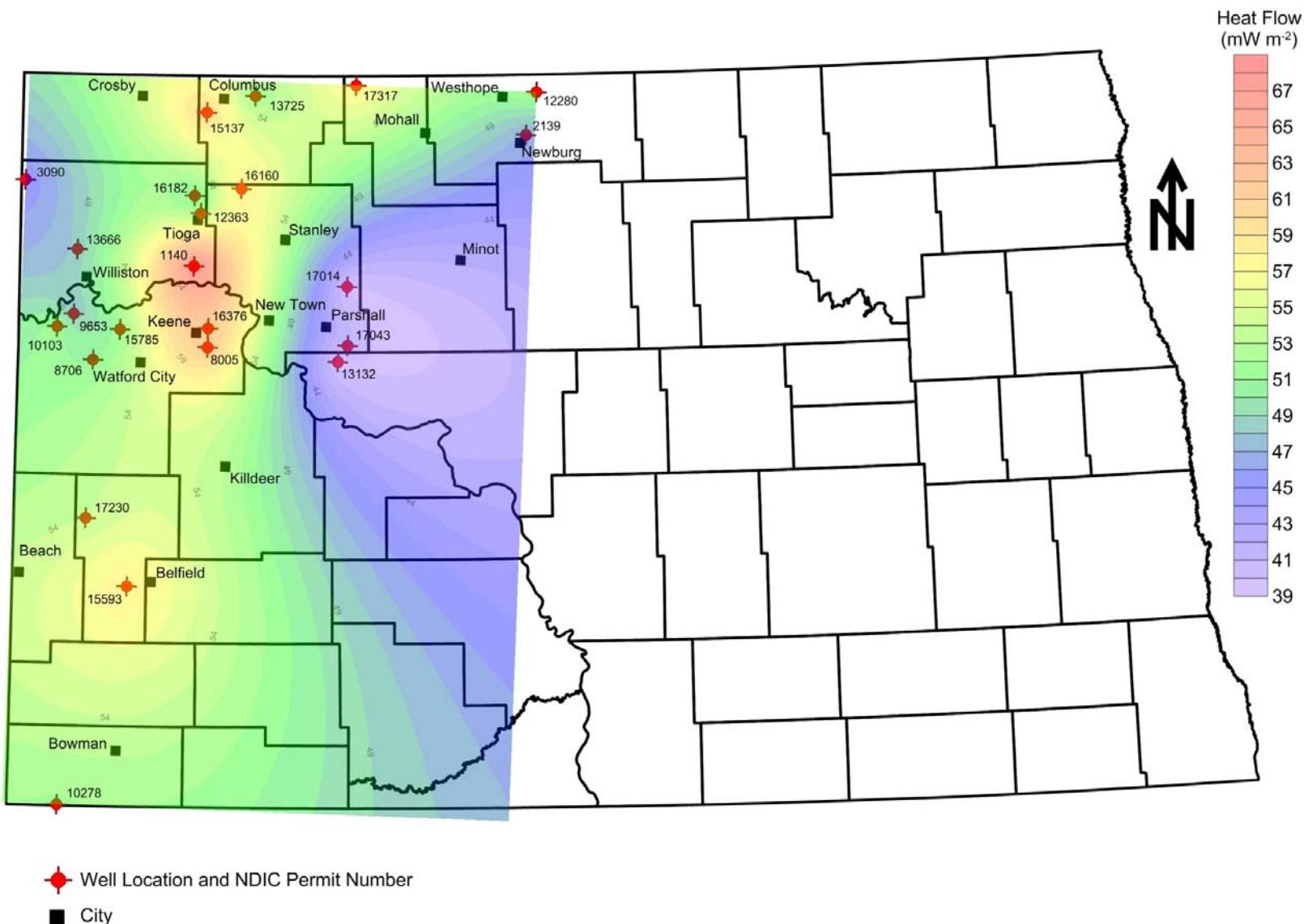


Figure 10. Mean heat flow of the graphical, harmonic mean, the Bullard method and the weighted average methods.

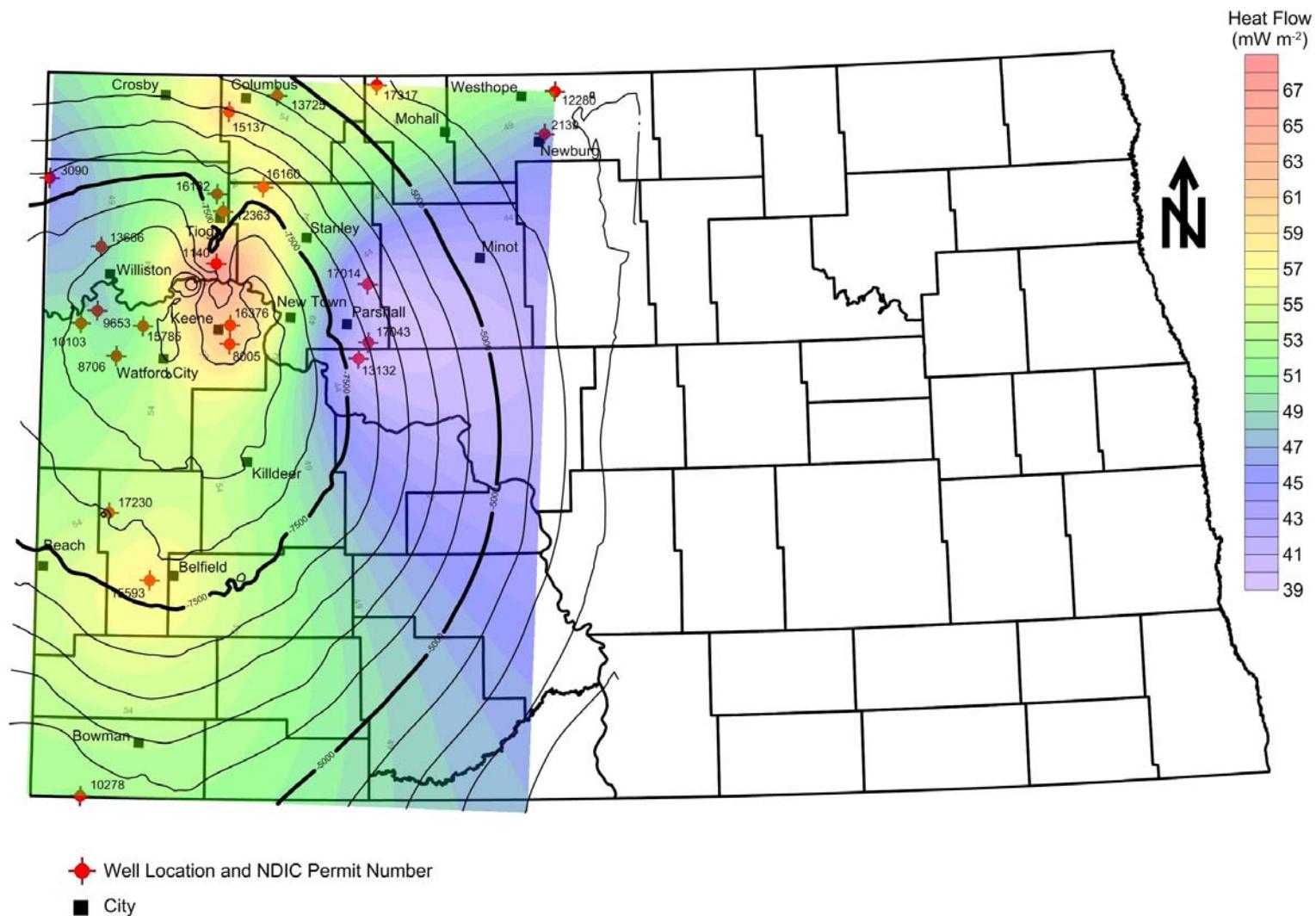


Figure 11. Heat Flow (colors) overlain by structure contours of the top of the Three Forks Formation.

be required to accurately determine heat flow within the Williston Basin. Geologic formations can often be differentiated on the basis of “marker” beds; however there can be wide variations in mineralogy, lithology, porosity, permeability, density, etc., depending upon depositional environment, depth of burial, secondary processes, etc., from one location to another within the same formation.

These criteria can profoundly influence thermal conductivity and therefore greatly influence the calculated heat flow.

Future Work

The NDGS currently has plans to log an additional 20 to 30 wells over the next several years. However, as noted above, some funding may be redirected to obtain additional thermal conductivity information from the wells that are being logged. Ideally, thermal conductivity values from core samples obtained from the wells that are logged would allow for the calculation of a reasonable estimate of heat flow from specific locations. This may also allow for better estimates of thermal conductivity by reverse modeling for the various formations at these locations that do not have core samples. This information, combined with thermal maturity estimates obtained by other methods (Nordeng and Nesheim, 2011) would provide better estimates of heat flow within the Williston Basin, better predictions of thermal maturity of hydrocarbons and the geothermal potential of the region.

Acknowledgements

Funding for this project was provided by the North Dakota Petroleum Council and the State of North Dakota. We would also like to acknowledge Hess Corporation, Jordan Exploration, Inc., Missouri Basin Well Service Inc., Enduro Operating, LLC, Liberty Resources LLC, Vanguard Operating LLC, Whiting Oil and Gas Corporation, Legacy Reserves Operating LP, Triangle USA Petroleum Corporation, Eagle Operating, Inc., TAQA North USA and Citation Oil and Gas Corporation for their cooperation and assistance in allowing us access to their wells.

References

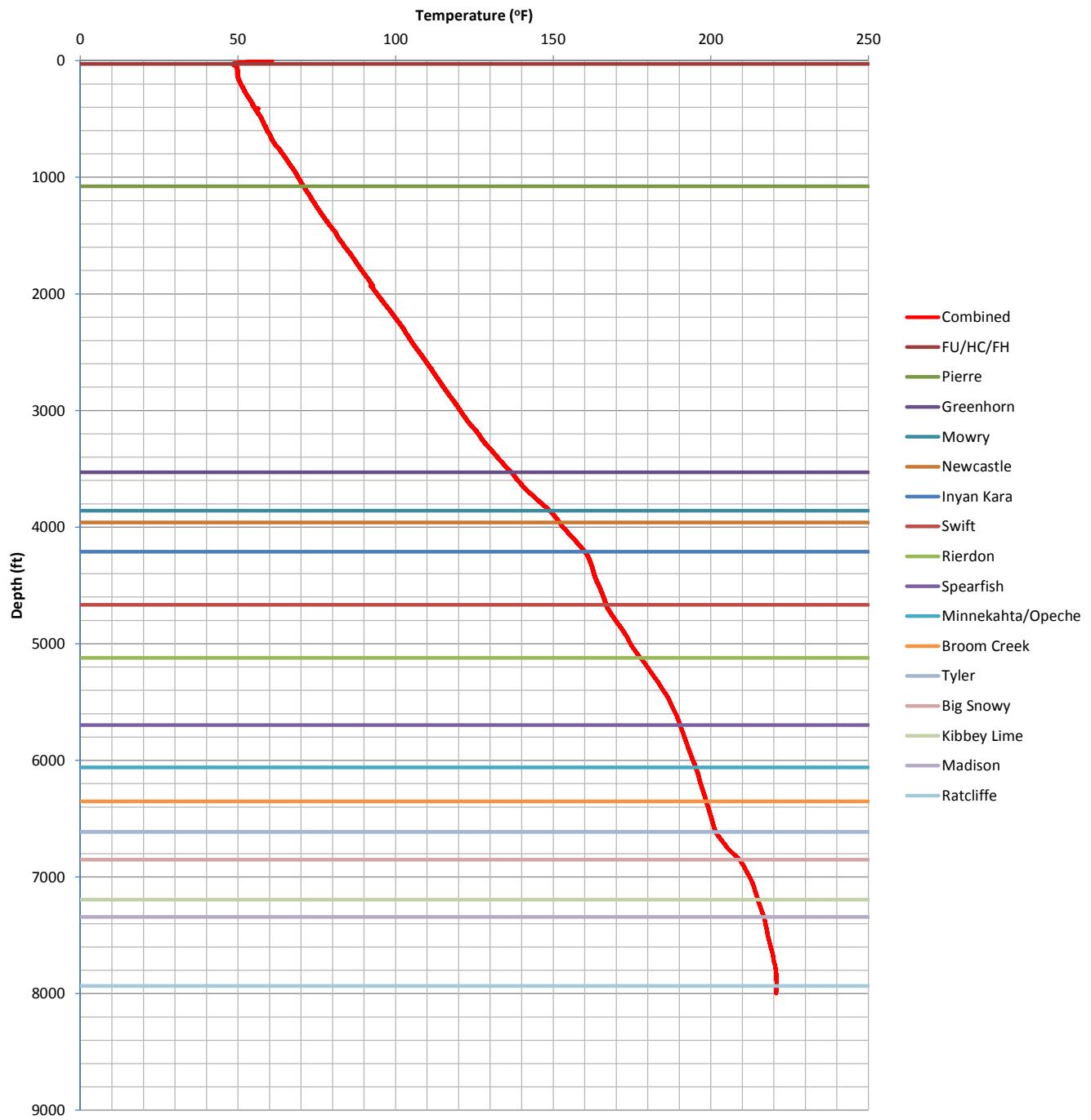
- Blackwell, D.D. and Richards, M.C., 2004, Geothermal map of North America: American Association of Petroleum Geologists, Tulsa Oklahoma, 1 sheet, scale 1:6,500,000.
- Beardmore, G.R., and J.P. Cull, 2001, Crustal heat flow, a guide to measurement and modelling: Cambridge University Press, Cambridge, United Kingdom, 324 pp.
- Bullard, E.C., (1939), Heat flow in South Africa: Proceedings of the Royal Society of London, A, 173, p. 428-450.
- Cooper, L.R., and C. Jones, 1959, The determination of virgin strata temperatures from observations in deep survey boreholes: Geophysical Journal of the Royal Astronomical Society, v. 2, p. 116-131.
- Lachenbruch A.H., and M.C. Brewer, 1959, Dissipation of the temperature effect of drilling a well in Artic Alaska, U.S. Geological Survey Bulletin, 1083-C, p. 73-109.

- Gosnold, W.D., M.R. McDonald, R. Klenner and D. Merriam, 2012, Thermostratigraphy of the Williston Basin, GRC Transactions, v. 36, p. 663-670.
- Gosnold, W., J. Majorowicz, R. Klenner and S. Hauck, 2011 Implications of post-glacial warming for northern hemisphere heat flow, Geothermal Resources Council Transactions, v. 35, p. 795-799.
- Majorowicz, J., W. Gosnold, A. Gray, J. Safanda, R. Klenner, and M. Unsworth, 2012, Implications of post-glacial warming for Northern Alberta heat flow – correcting for the underestimate of the geothermal potential, Geothermal Resources Council Transactions, v. 36, p. 693-698.
- McDonald, M.R., and S.H. Nordeng, 2014, Temperature logging in the Williston Basin; North Dakota Department of Mineral Resources Geo News, v.41, n. 2, p. 11-13.
- Nordeng, S.H., and T.O. Nesheim, 2011, Determination of subsurface temperatures and the fraction of kerogen converted to petroleum within the Rauch Shapiro Fee #21-9, Billings Co., ND, North Dakota Geological Survey, Geological Investigation 146.
- Nordeng, S.H., 2012, Determination of activation energy and frequency factor for samples of the Bakken Formation (Mississippian-Devonian) Williston Basin ND: North Dakota Geological Survey, Geological Investigation 163, 15 pp.
- Nordeng, S.H., 2013, Evaluating source rock maturity using multi-sample kinetic parameters from the Bakken Formation (Mississippian-Devonian) Williston Basin ND, North Dakota Geological Survey, Geological Investigation 164, 19 pp.
- Nordeng, S.H., 2014, Building the science for advancing oil and gas exploration and development in the Williston Basin, North Dakota Department of Mineral Resources Geo News, v.41, n. 1, p. 14-18.
- Nuccio, V.F., and C.E. Barker, eds., 1990, Applications of thermal maturity studies to energy exploration, Society of Economic Paleontologists and Mineralogists, Rocky Mountain Section, 174 pp.
- Prensky, S., 1992, Temperature measurements in boreholes: an overview of engineering and scientific applications, The Log Analyst, v. 33, no. 3, p. 313-333.

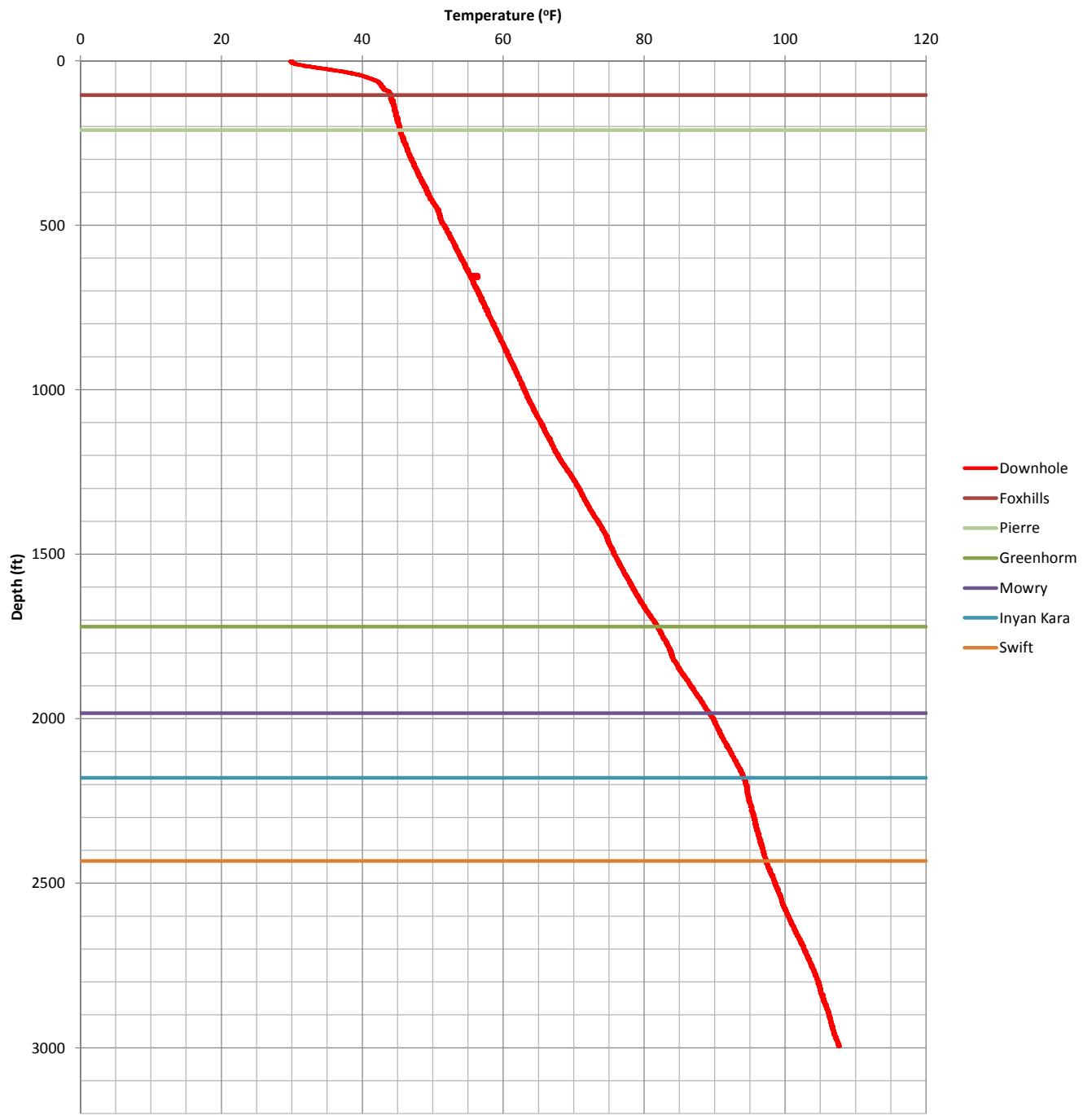
APPENDIX A

TEMPERATURE PROFILES

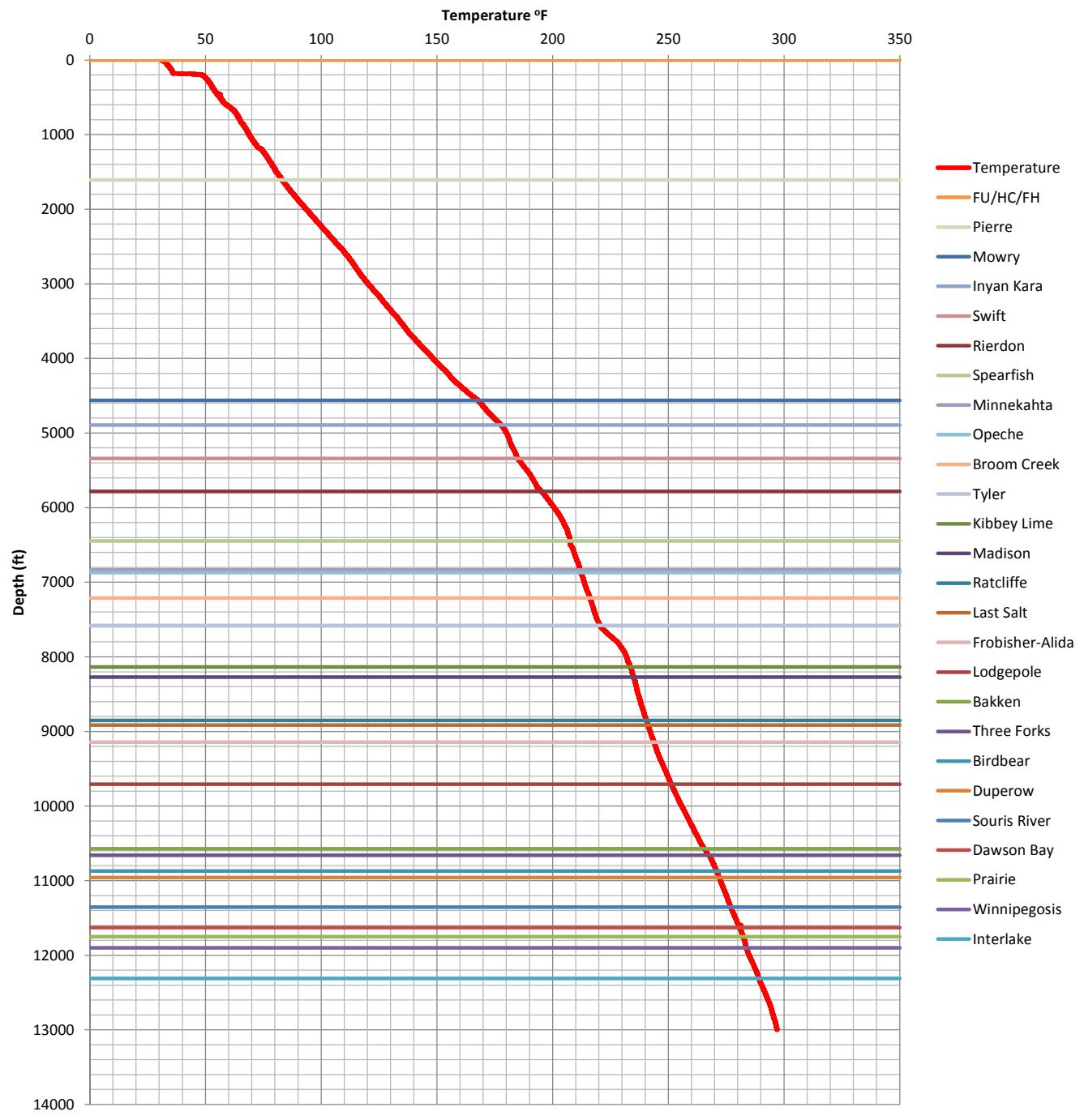
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Williams County, ND



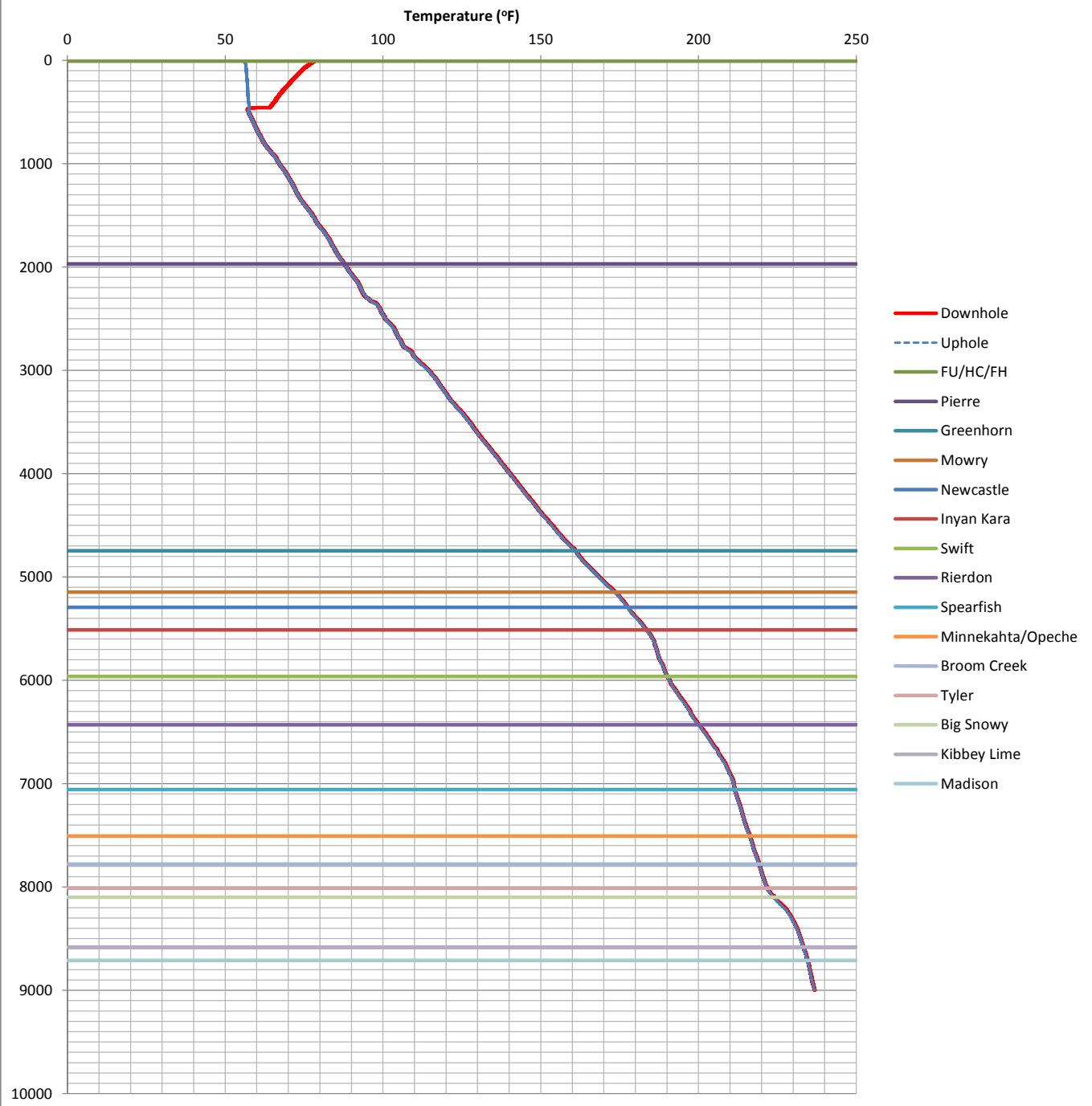
Temperature Profile
NDIC 2139 - NSCU V-706
Bottineau County, ND



Temperature Profile
NDIC 8005 - Sivertson 29-23R #1
McKenzie County, ND



Temperature Profile
NDIC 8706 - Berge C-1
McKenzie County, ND



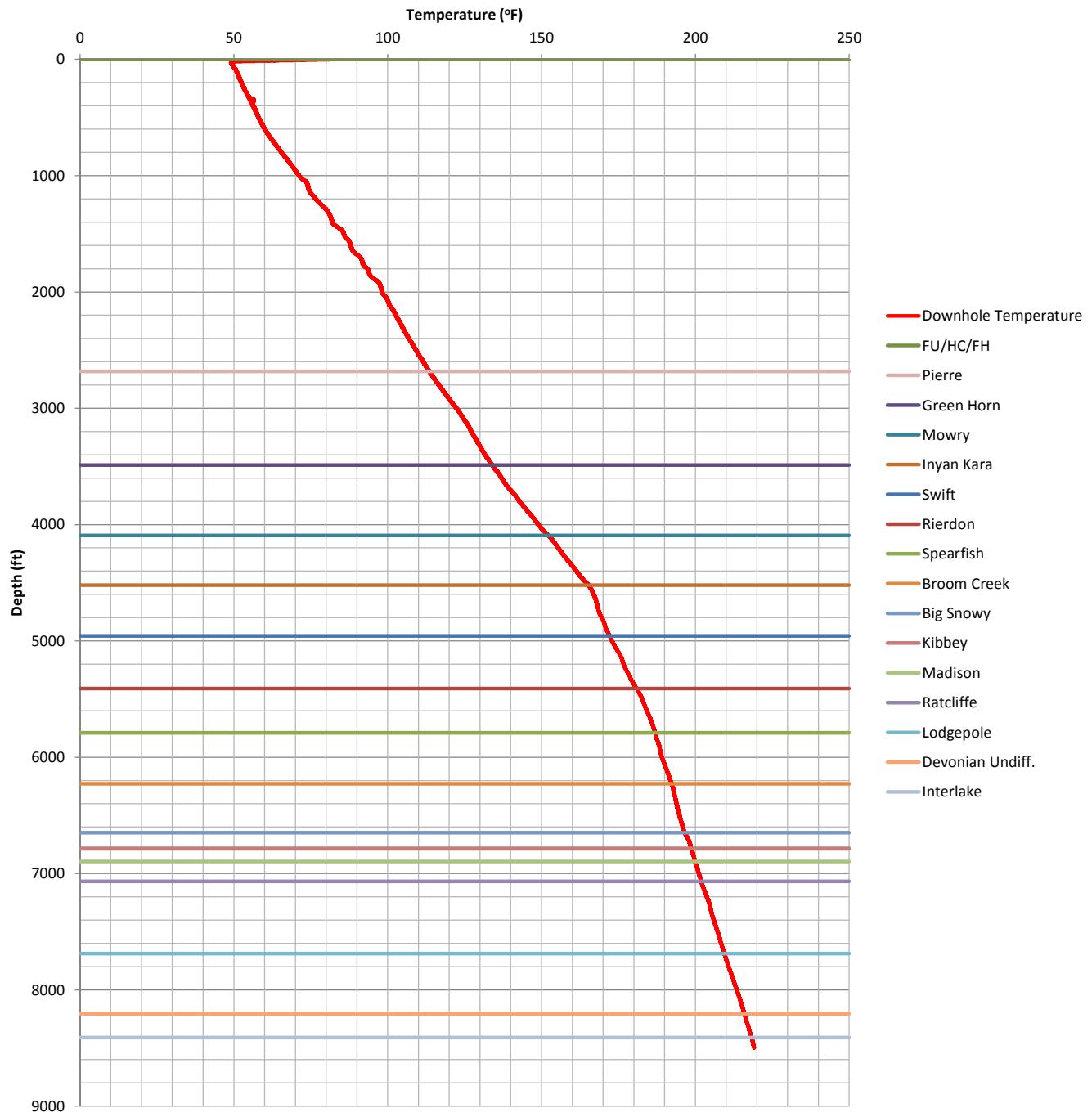
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McKenzie County, ND



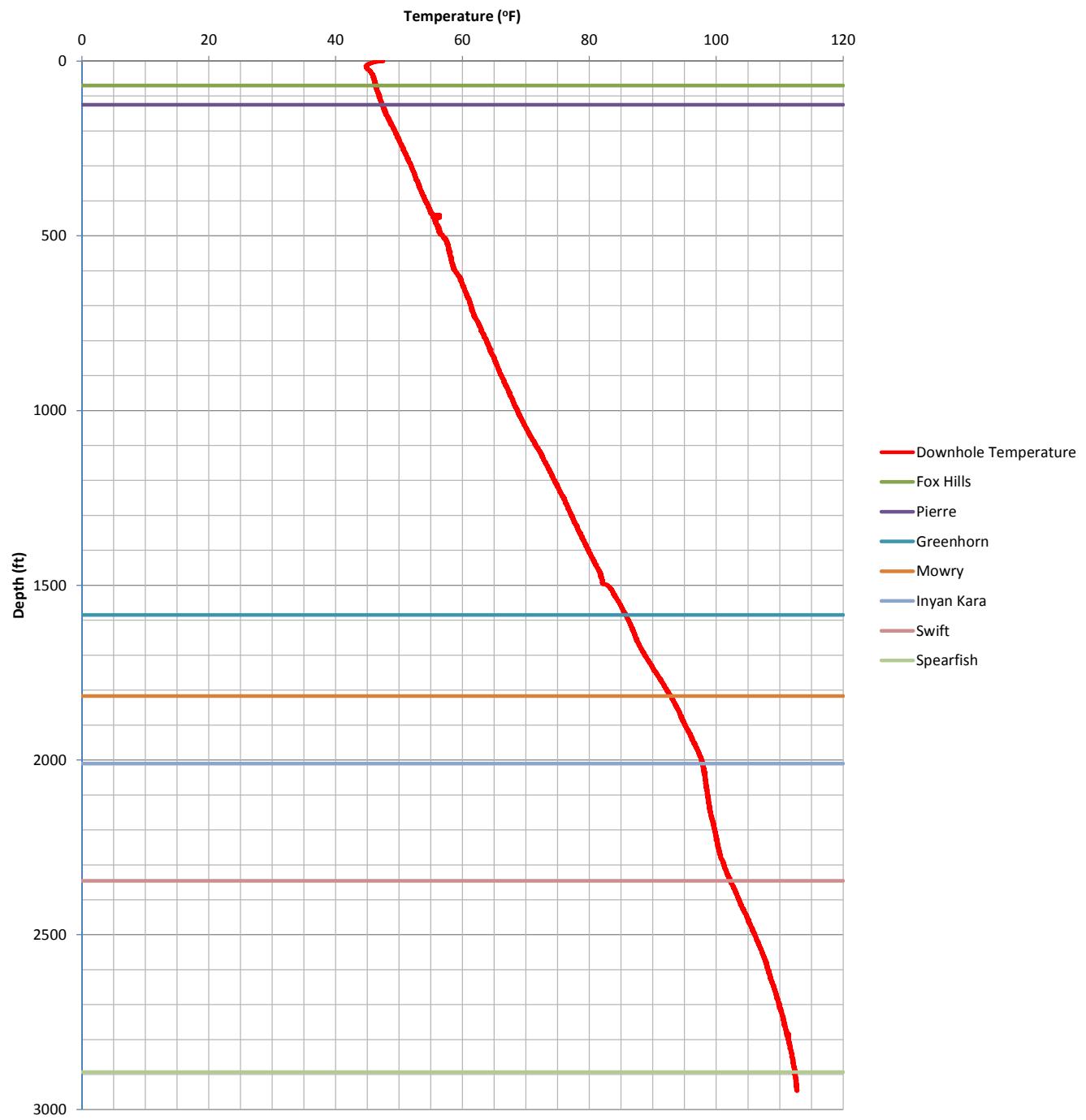
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McKenzie County, ND



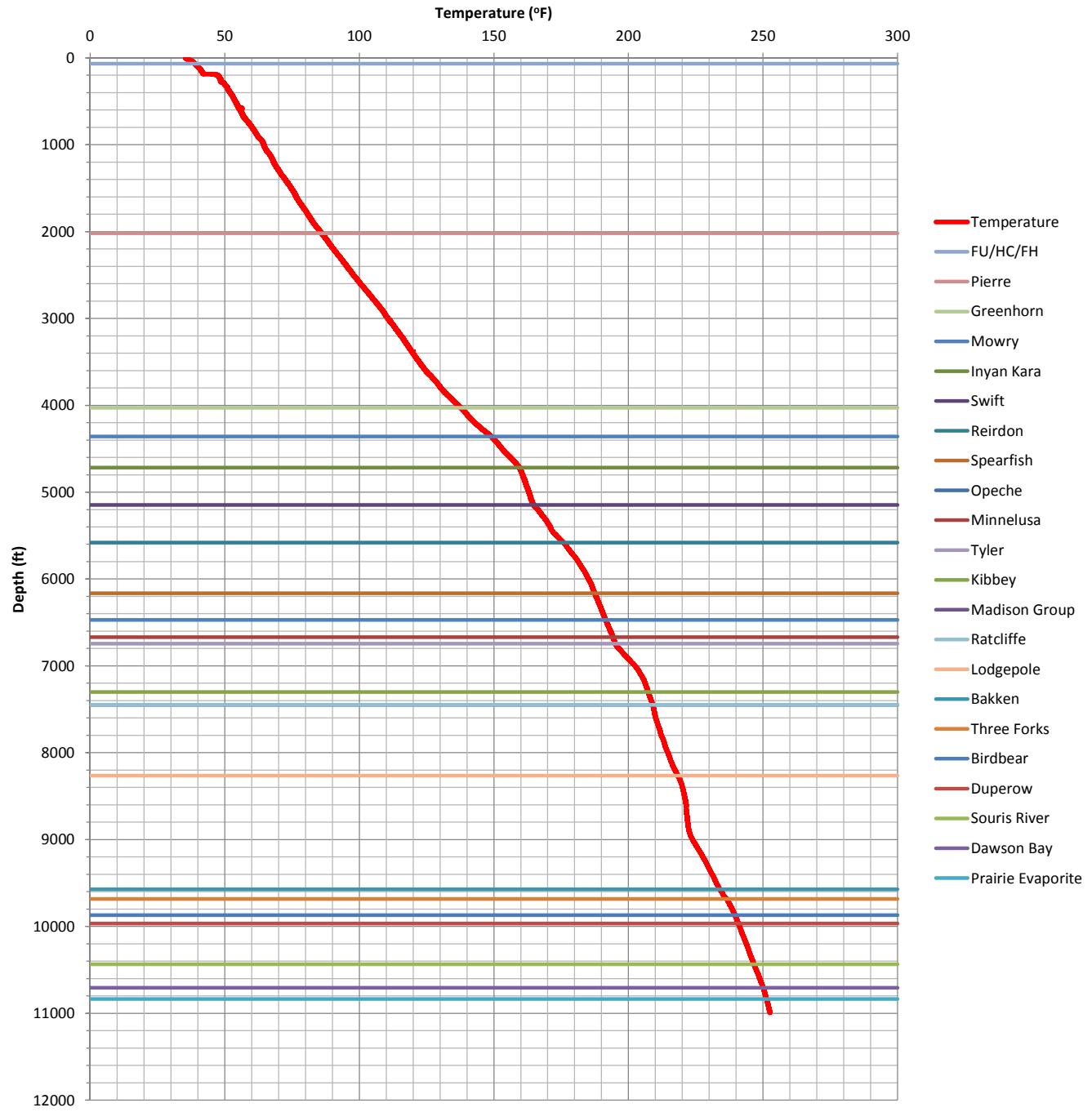
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Bowman County, ND



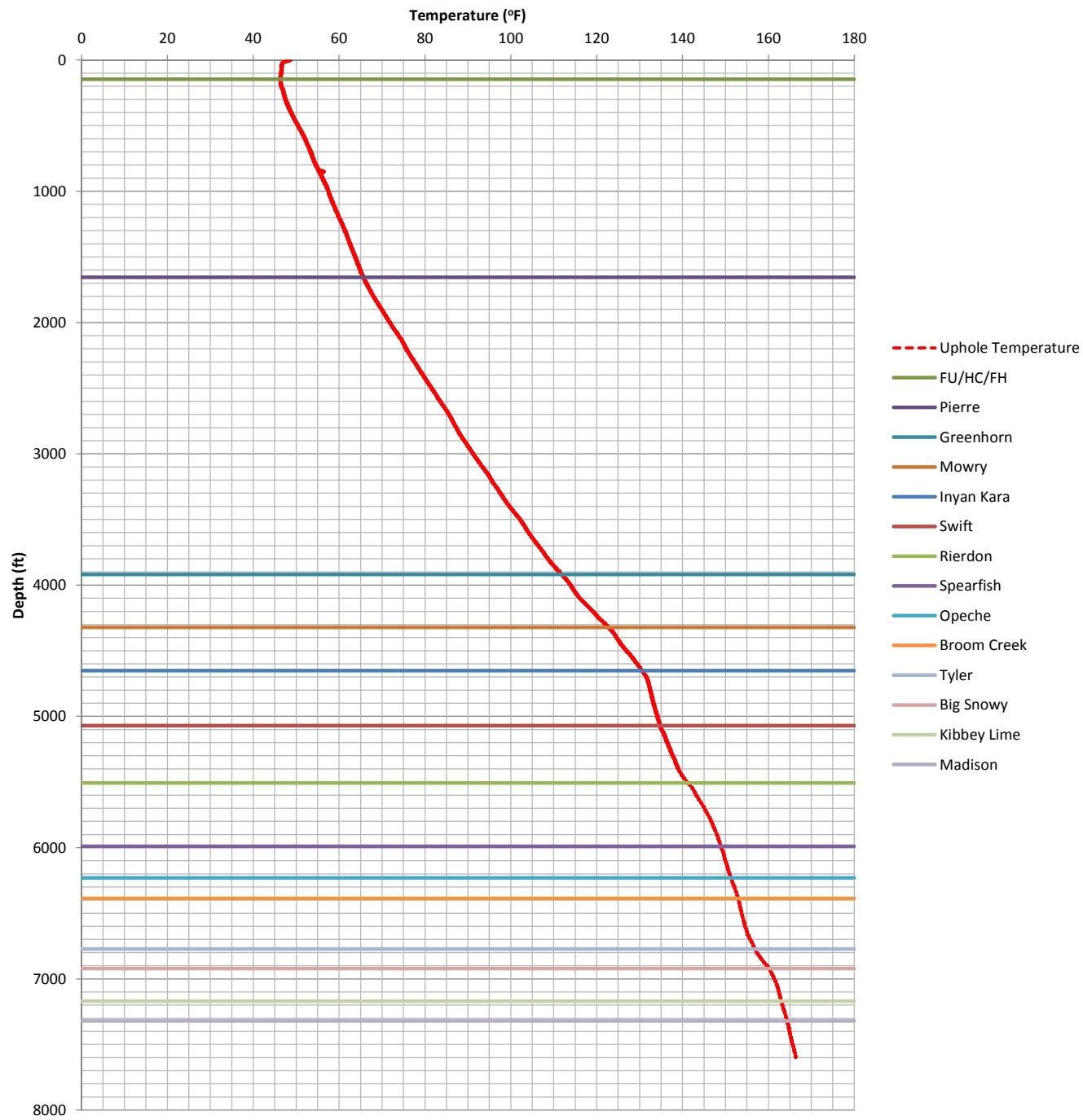
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Bottineau County, ND



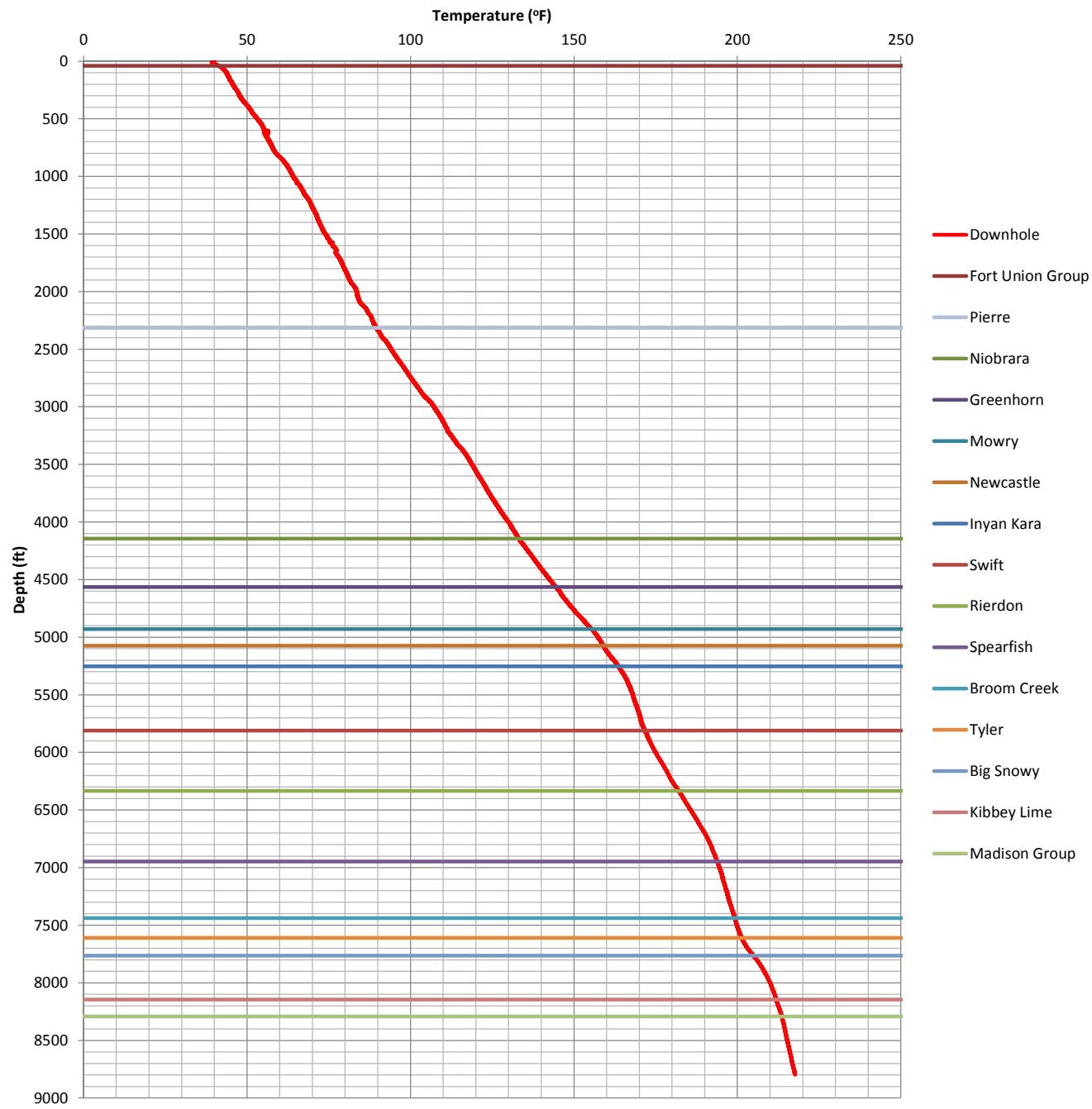
Temperature Profile
NDIC 12363 - Astrid Ongstad 14-22
Williams County, ND



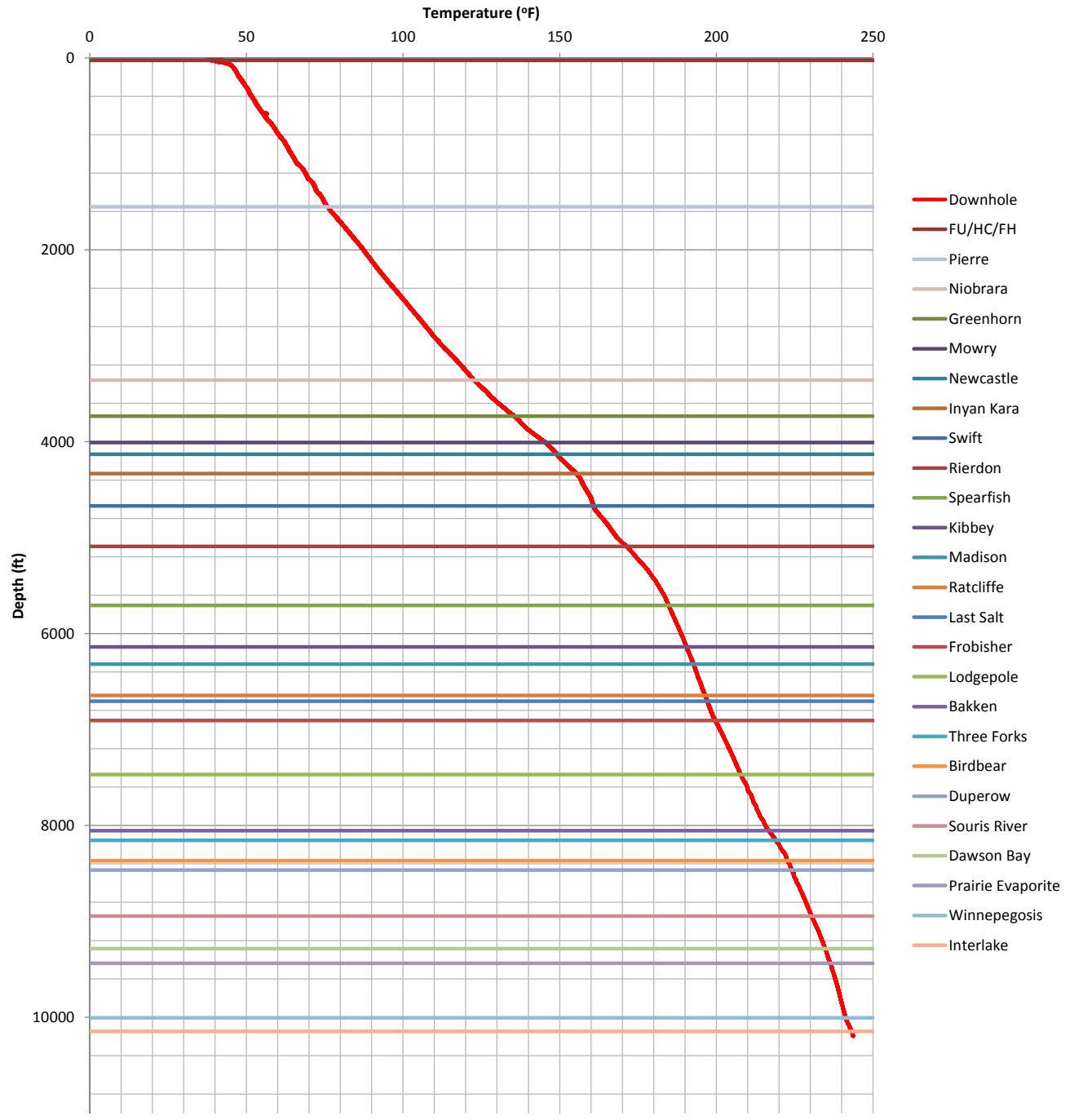
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McClean County, ND



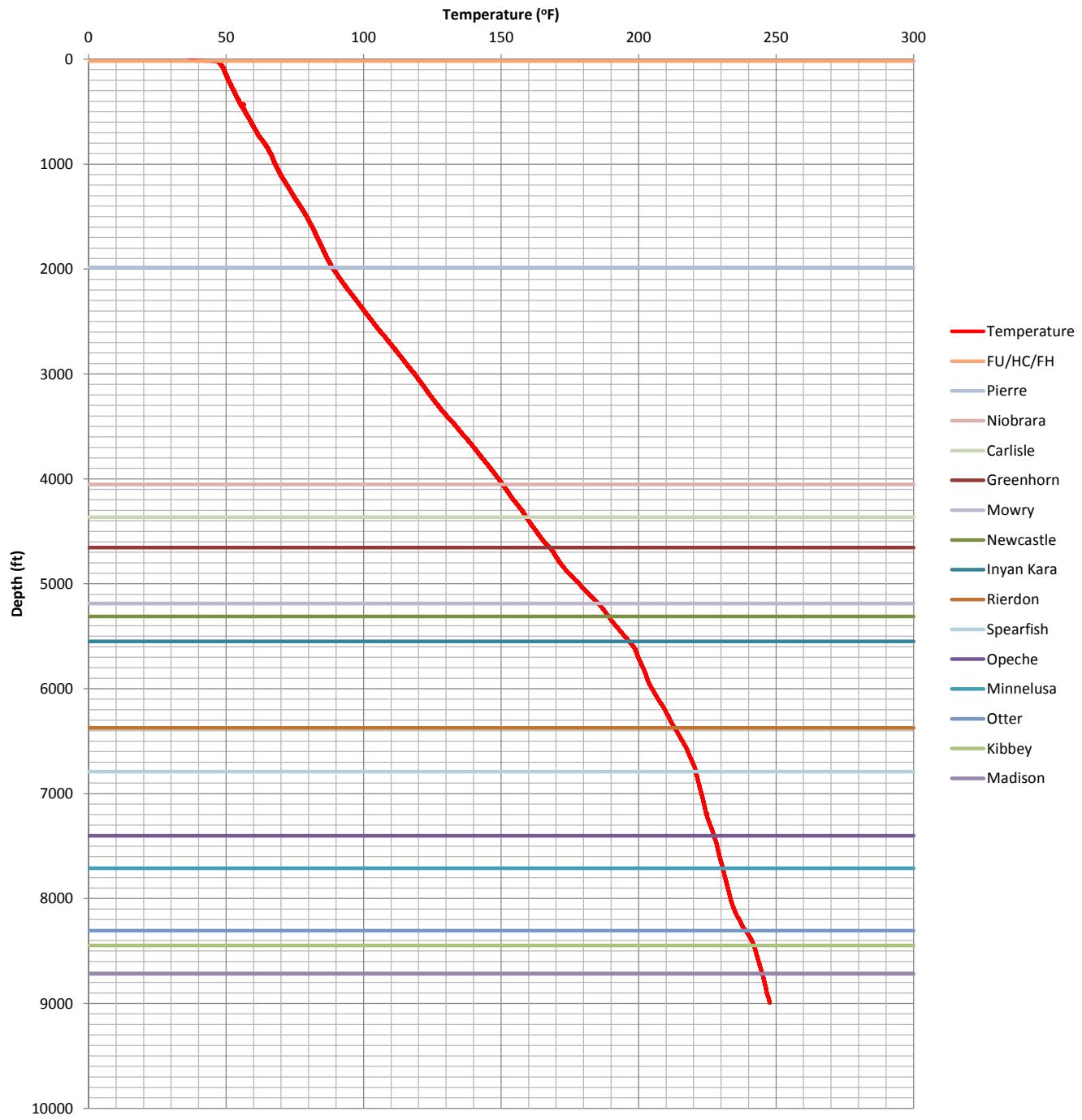
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NDIC 13666 - Rieder 1-9 SWD
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Temperature Profile
NDIC 15137 - Holte #6-21
Burke County, ND



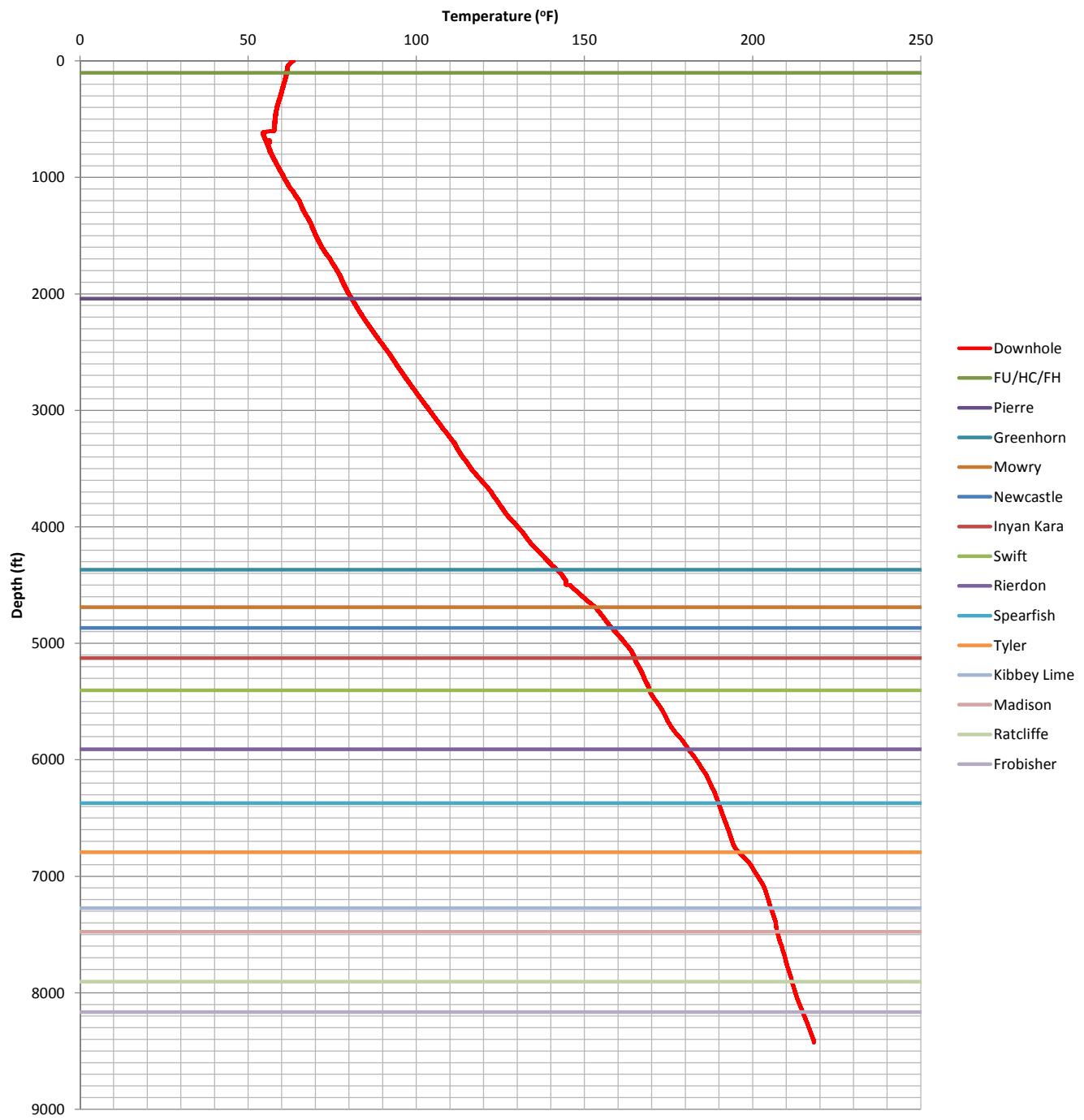
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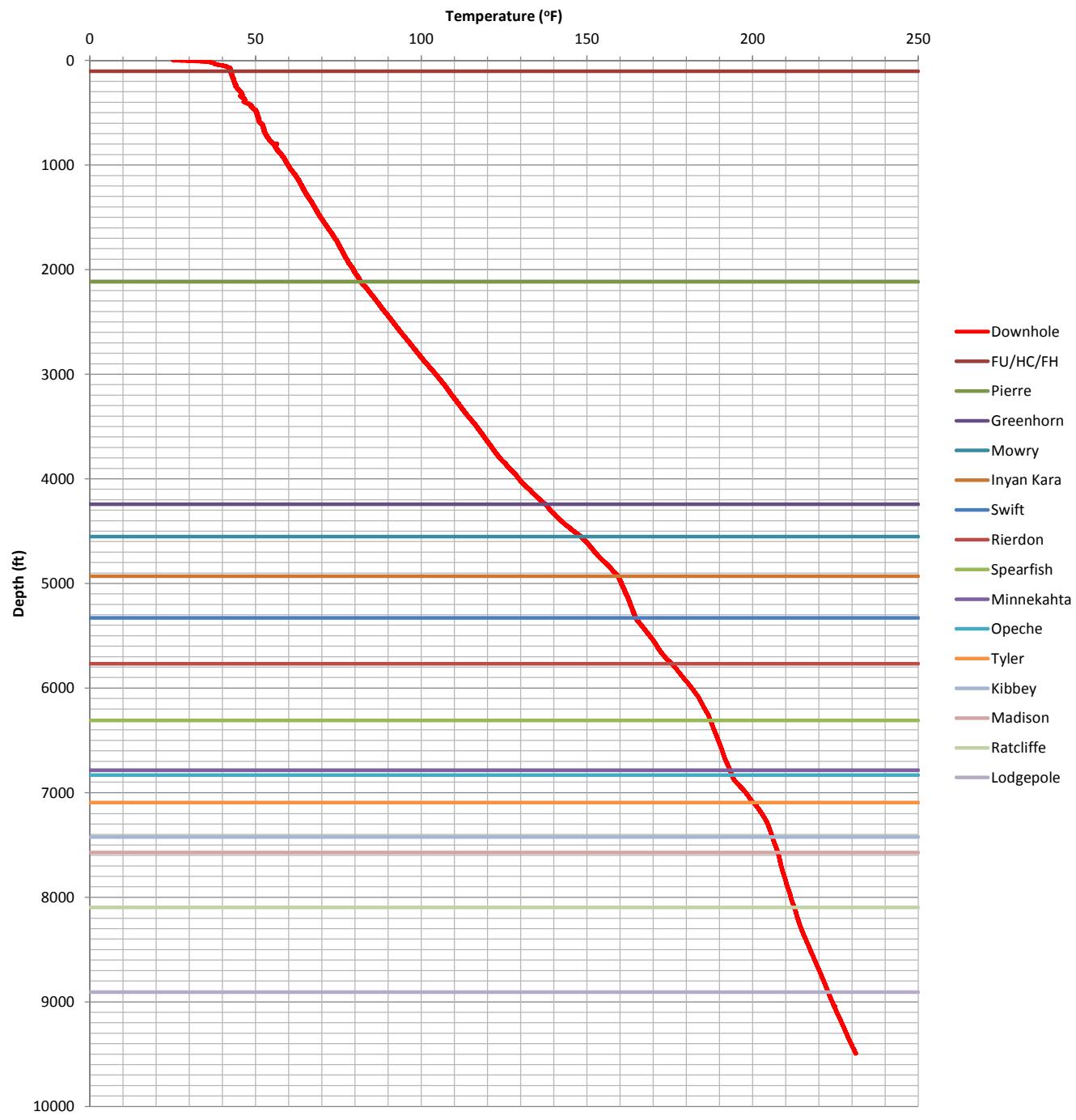
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McKenzie County, ND



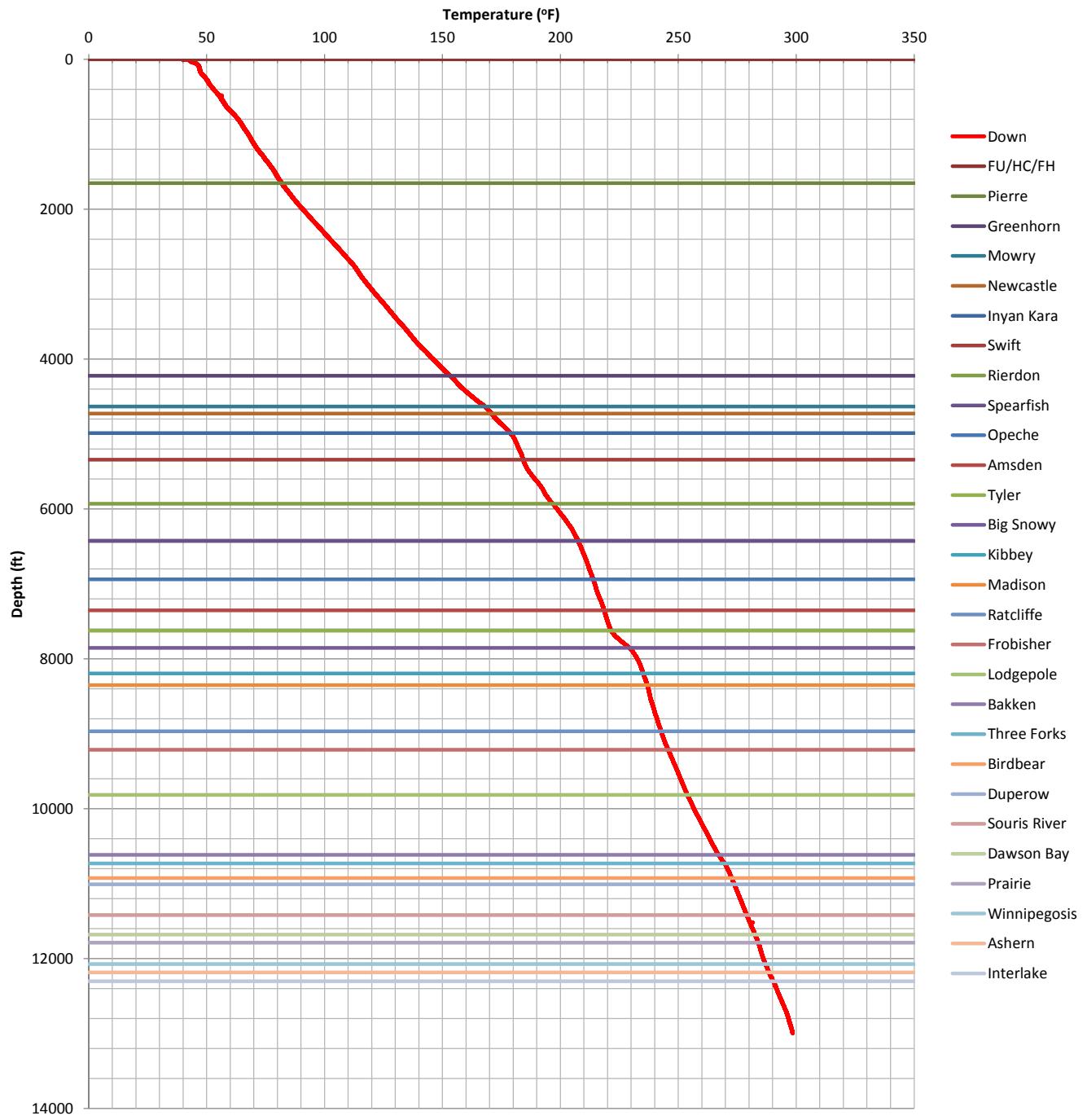
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Mountrail County, ND



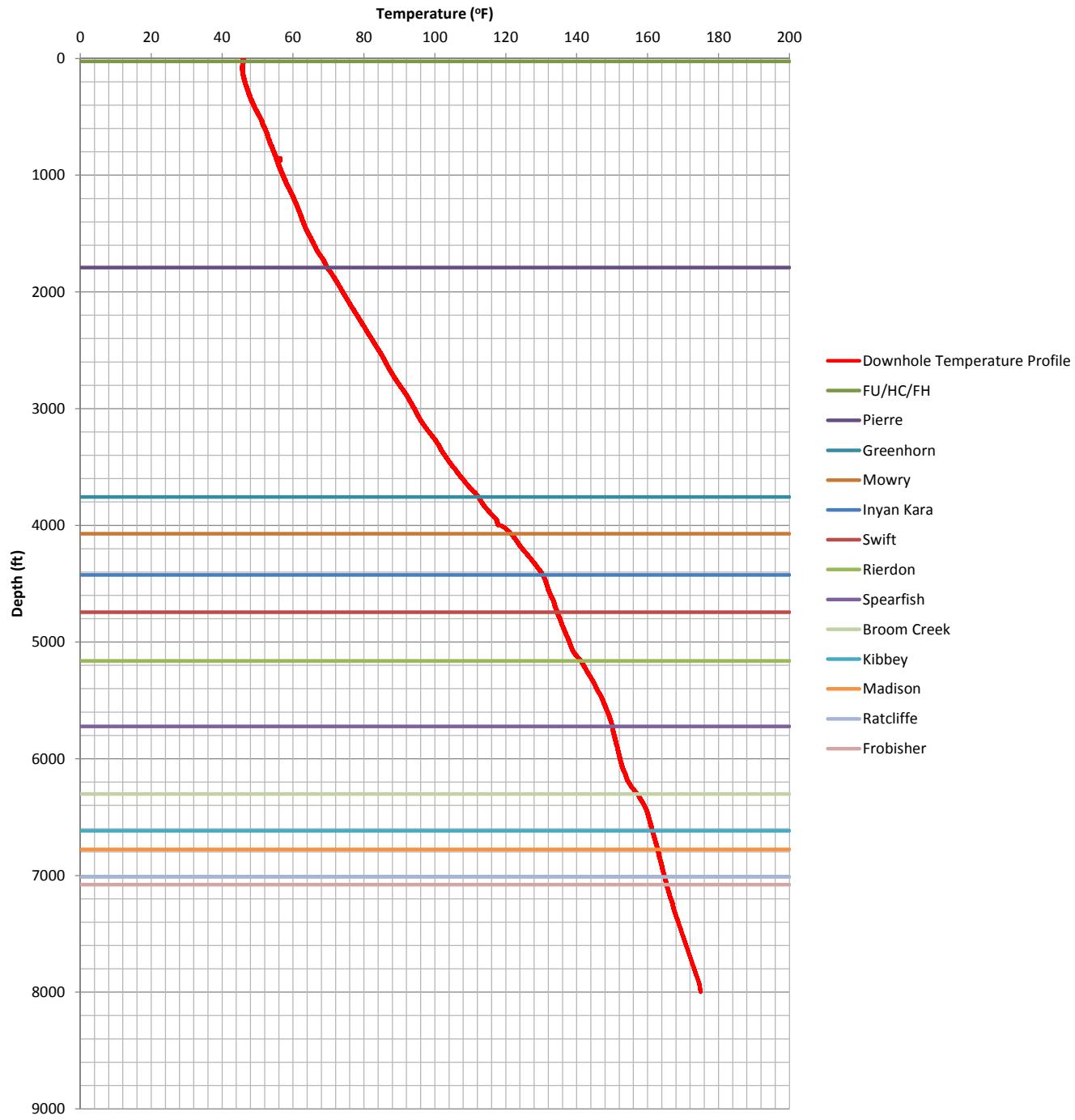
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Williams County, ND



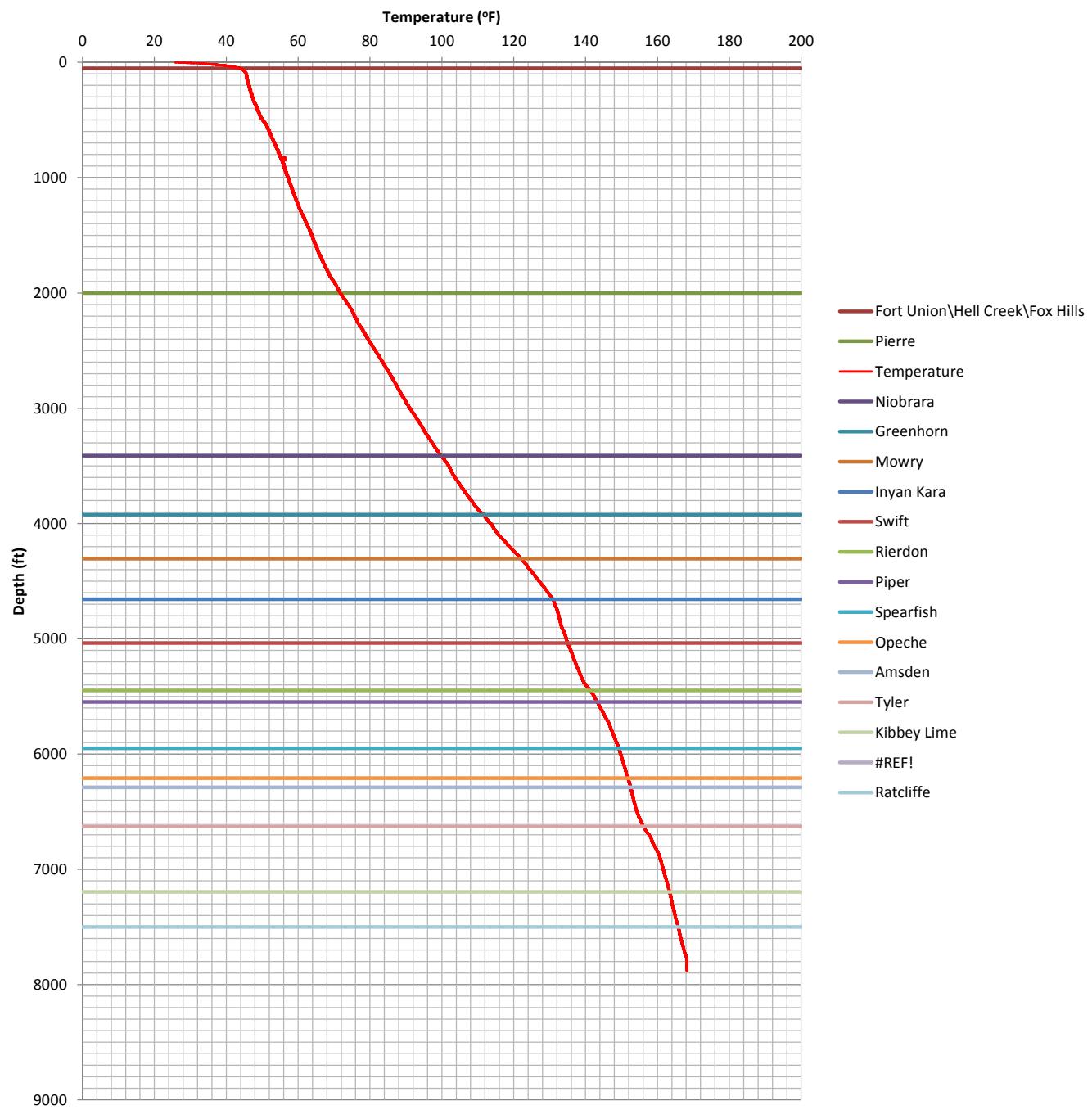
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McKenzie County, ND



Temperature Profile
NDIC 17014 - Edwards 1-33BH
Mountrail County, ND



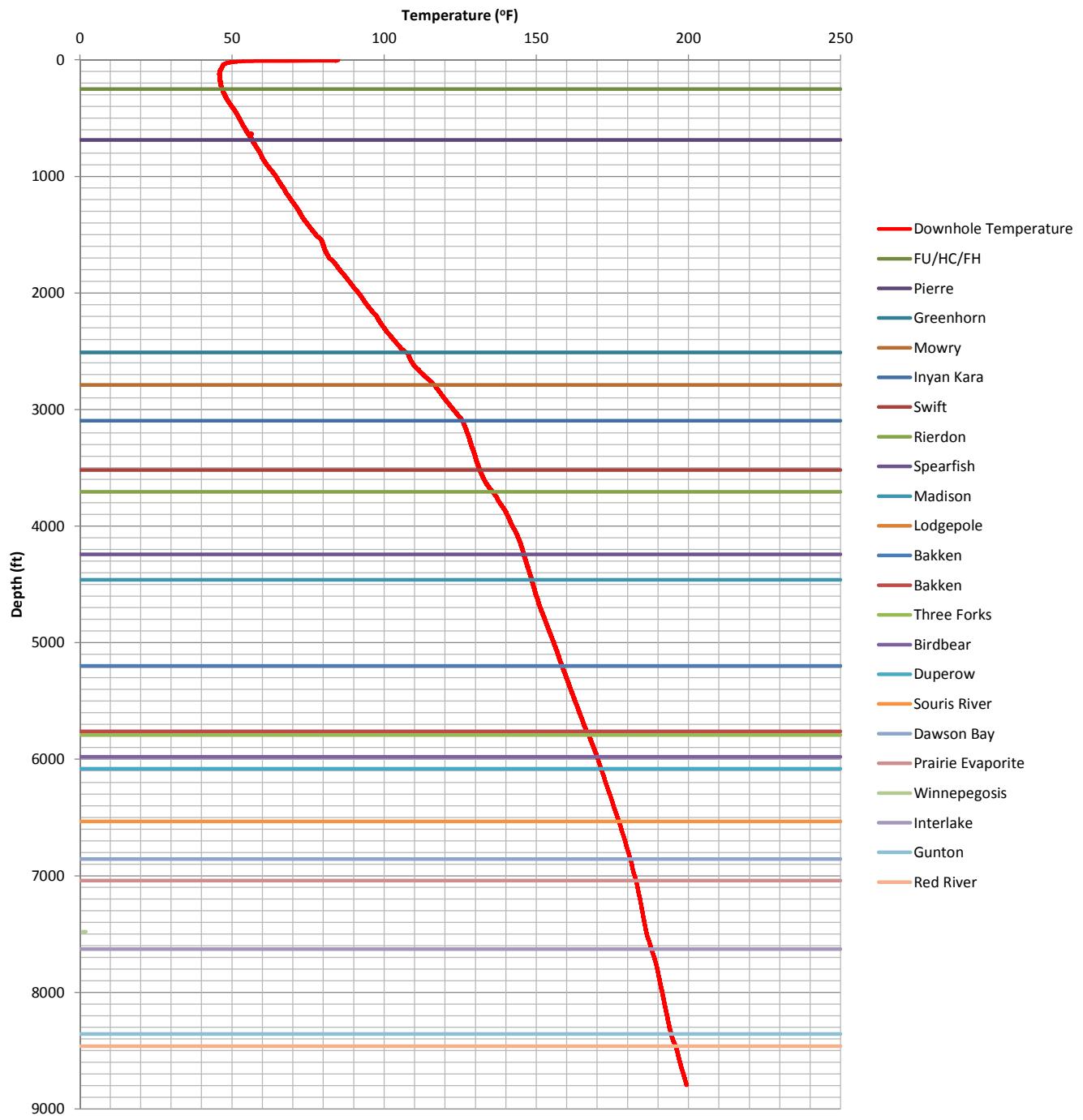
Temperature Profile
NDIC 17043 - St. Andes H-1
Mountrail County, ND



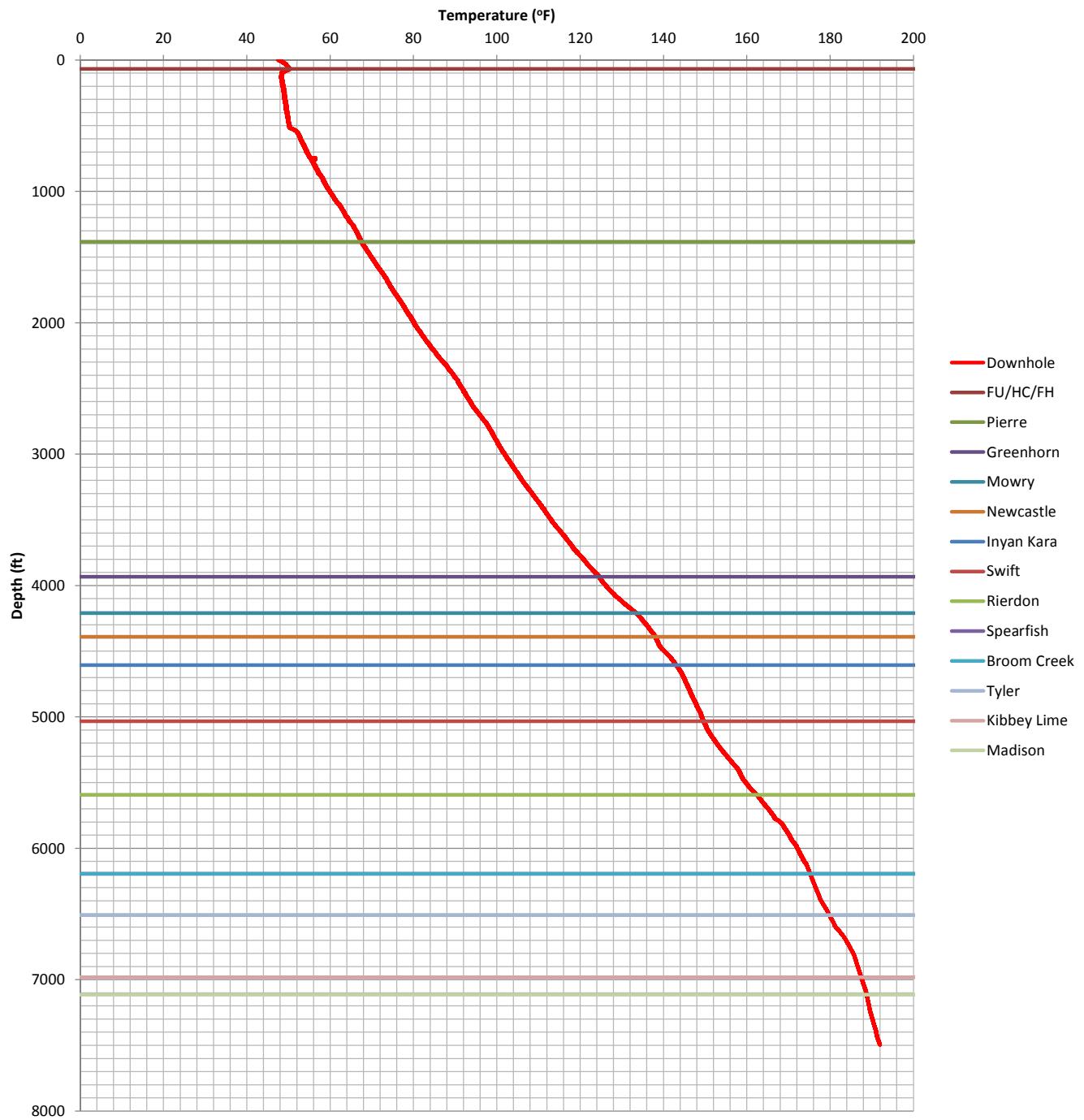
Temperature Profile
NDIC 17230 - Roosevelt Federal 2-4H
Billings County, ND



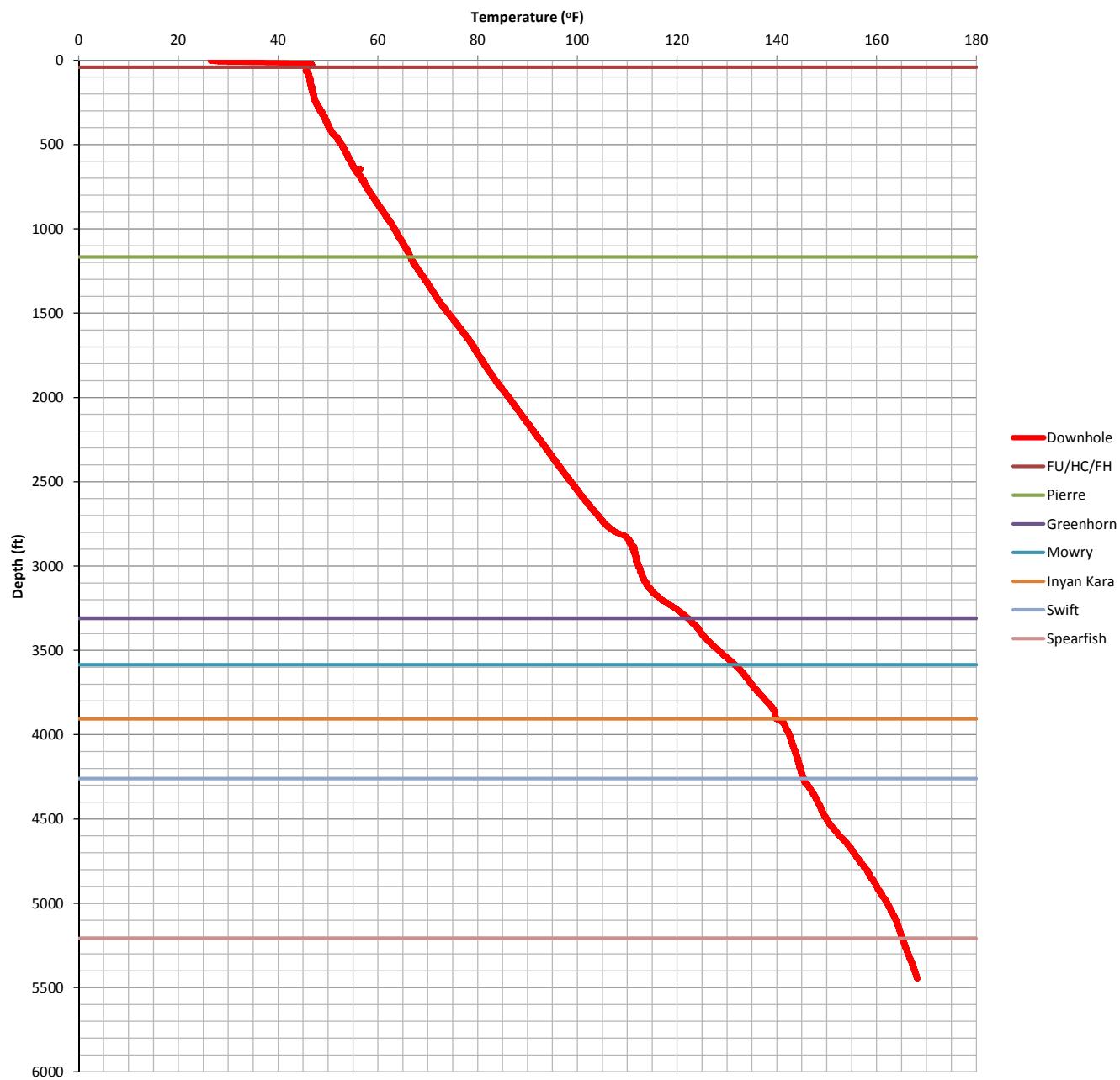
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Renville County, ND



Temperature Profile
NDIC 3090 - Grenora-Madison Unit 08
Williams County, ND



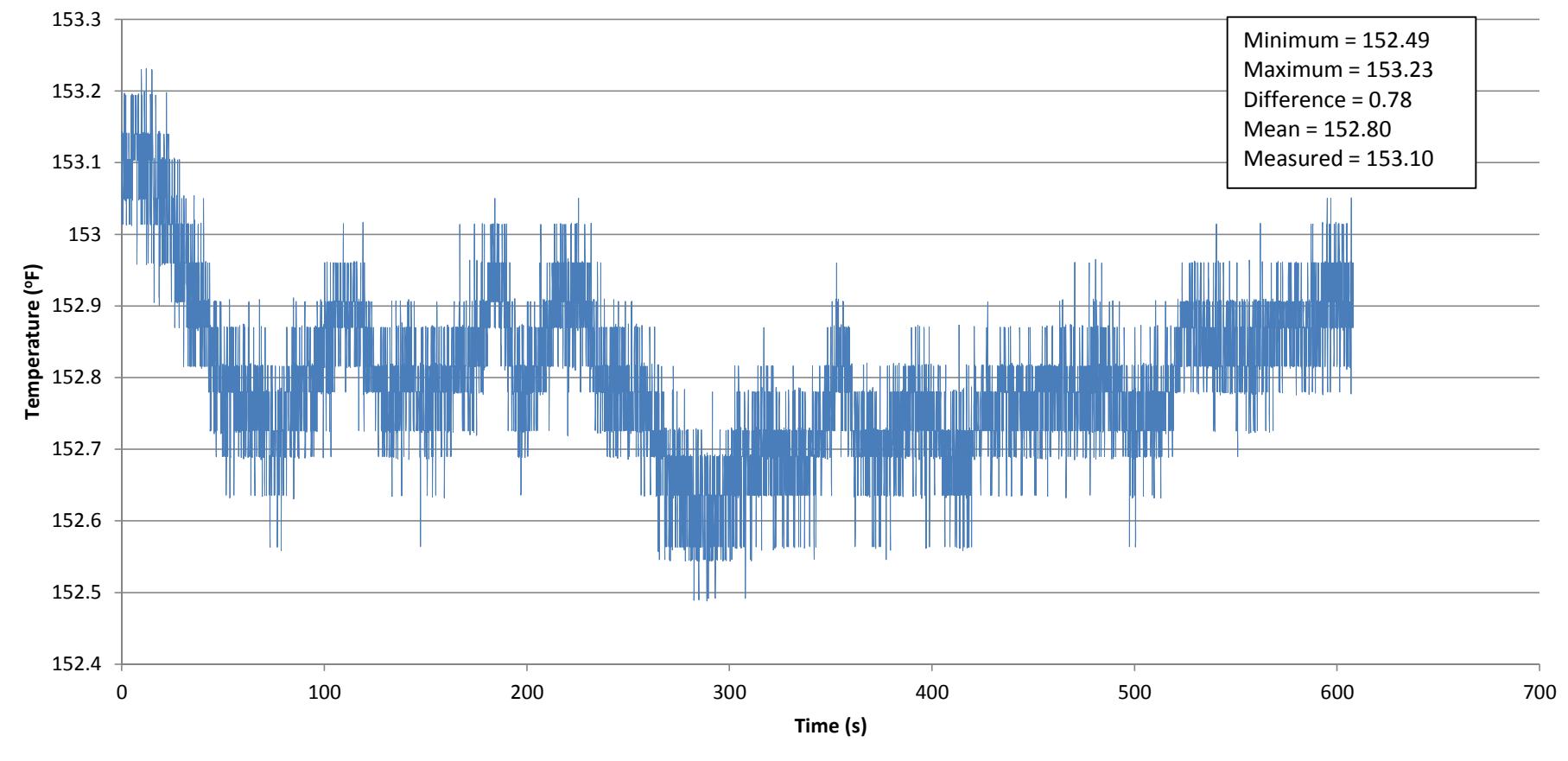
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NDIC 13725 - JC Woods 26H-1
Burke County, ND



APPENDIX B

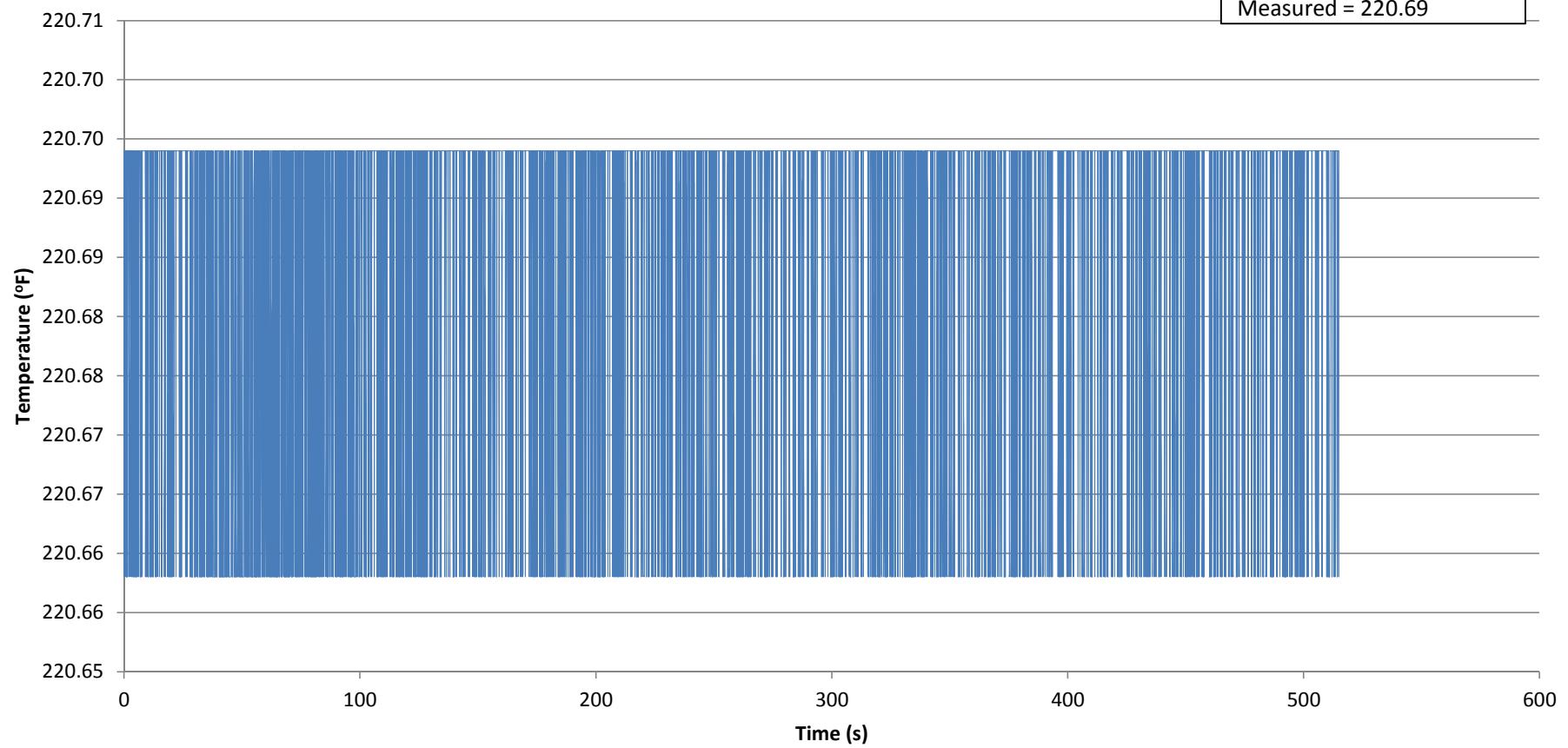
STATION STOPS

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Williams County, ND
Station Stop at 4000 ft



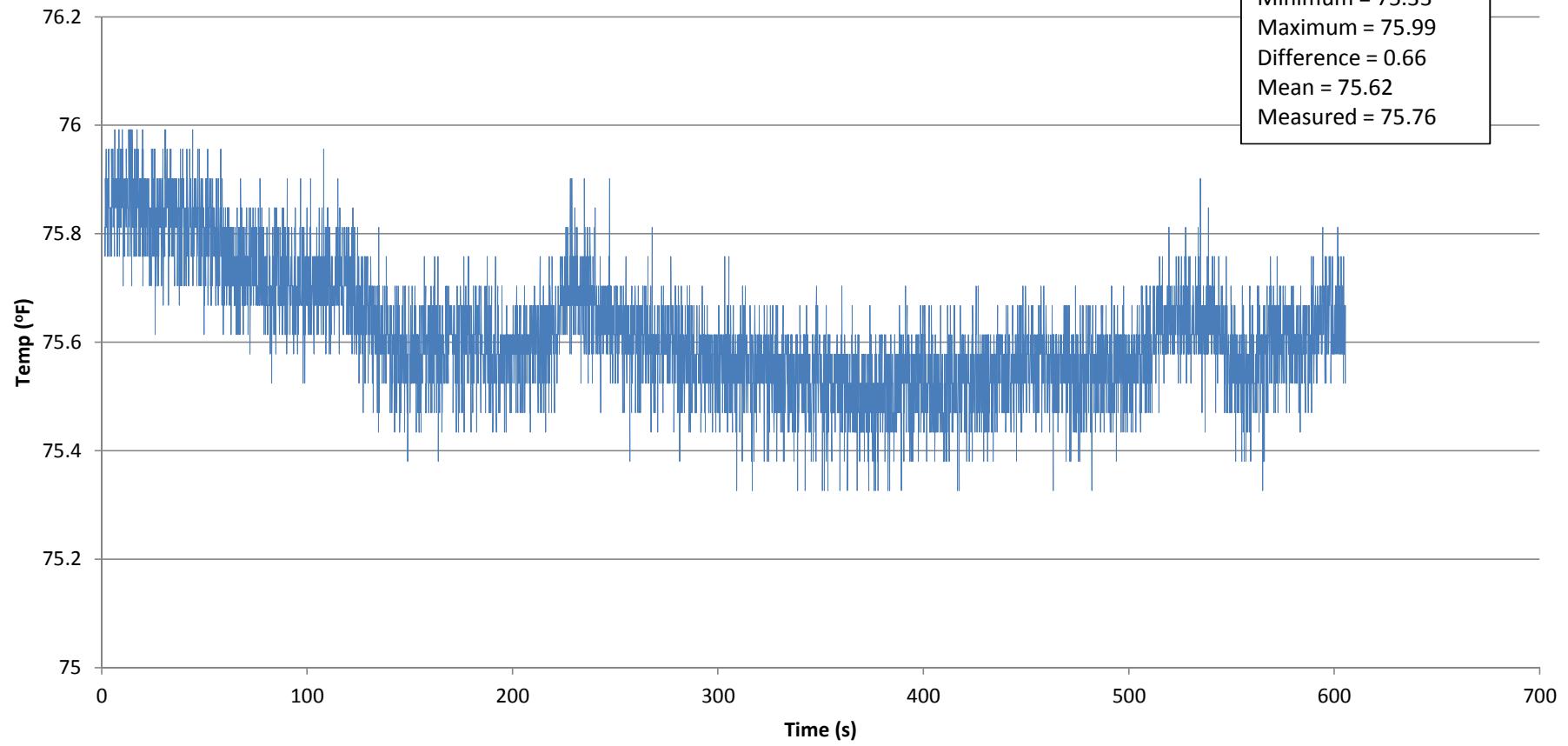
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Measured = 220.69



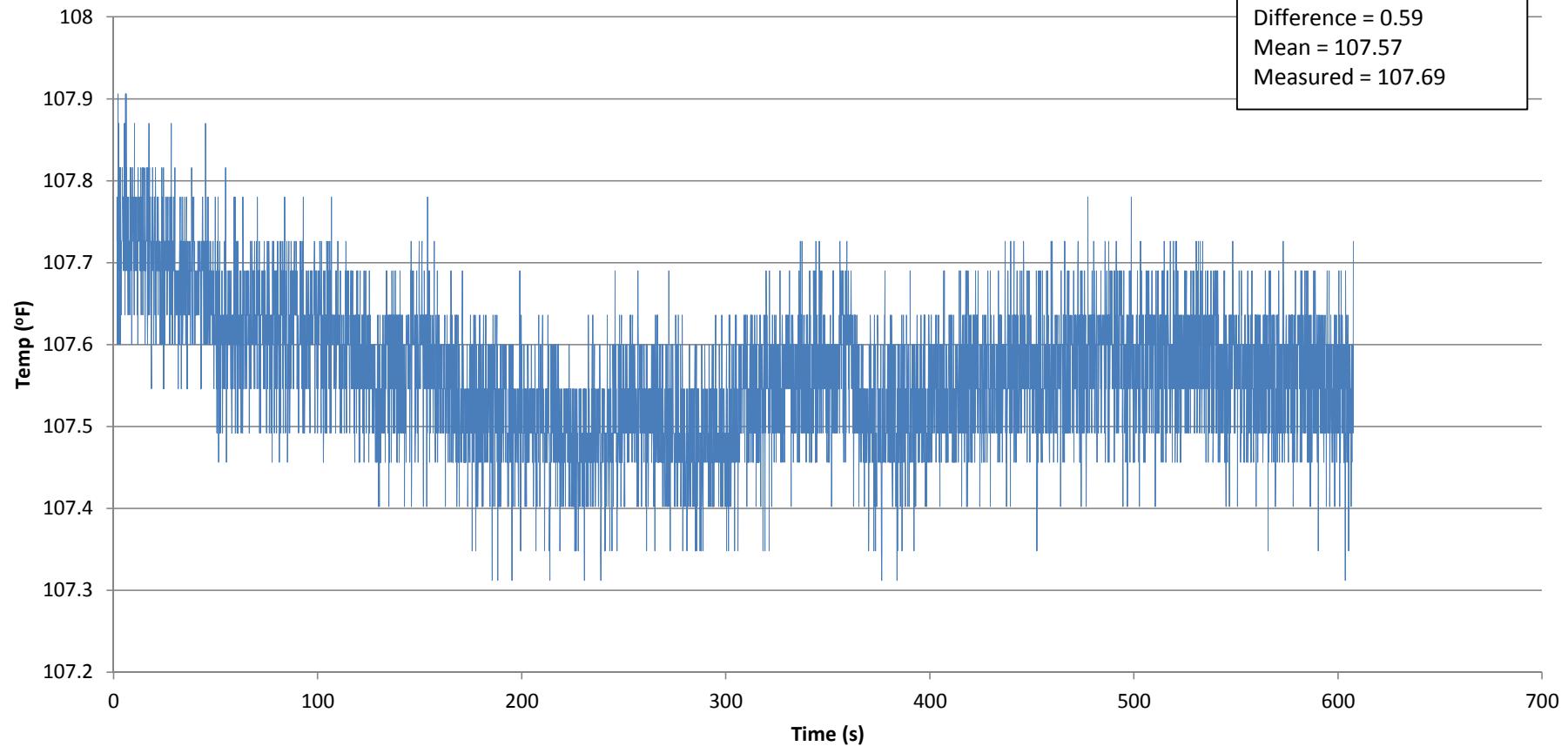
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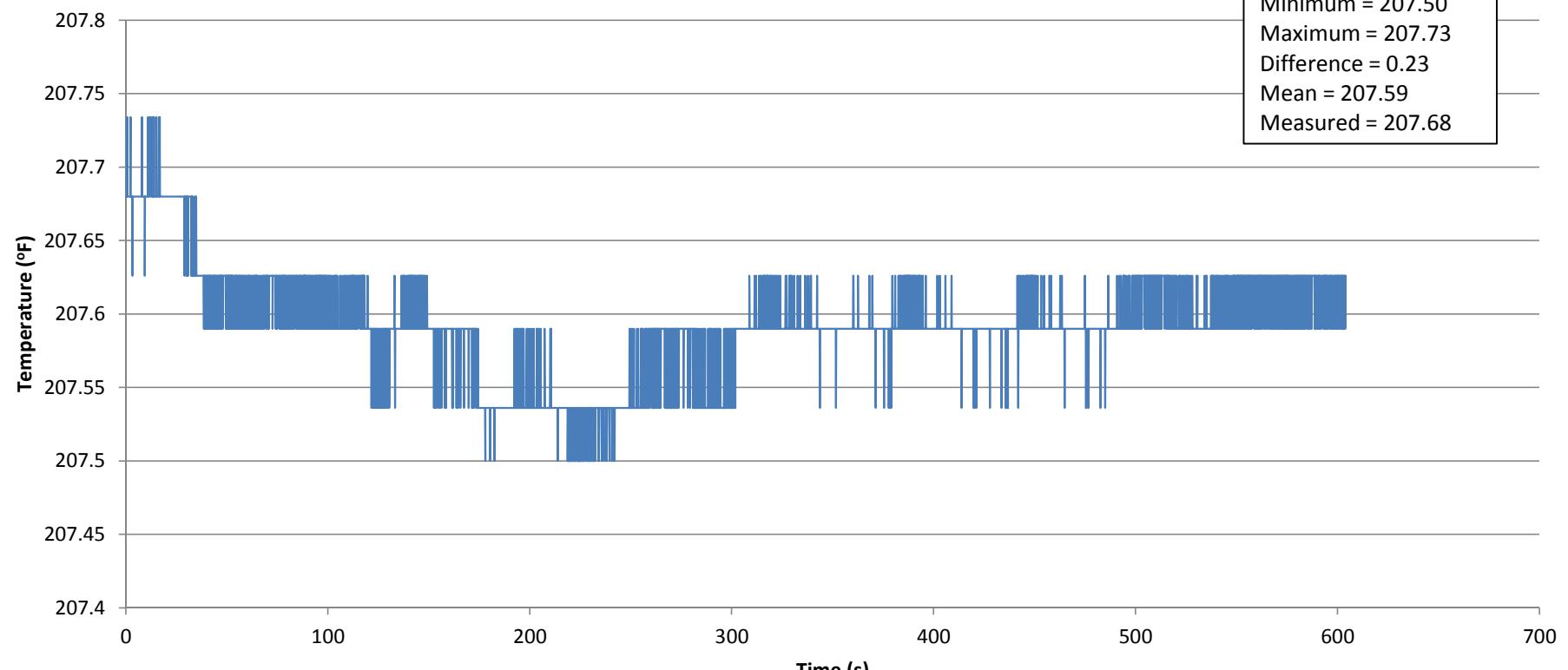
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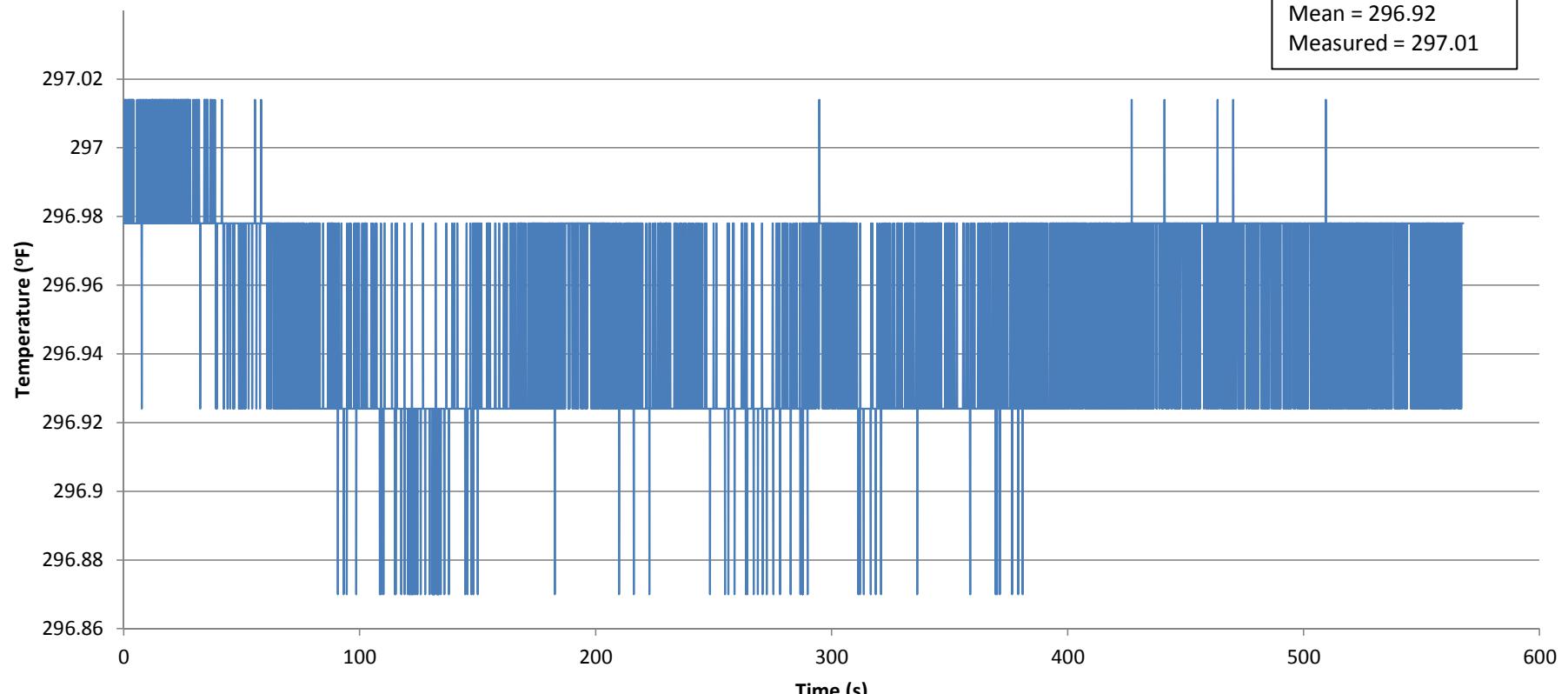
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McKenzie County, ND
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Measured = 207.68

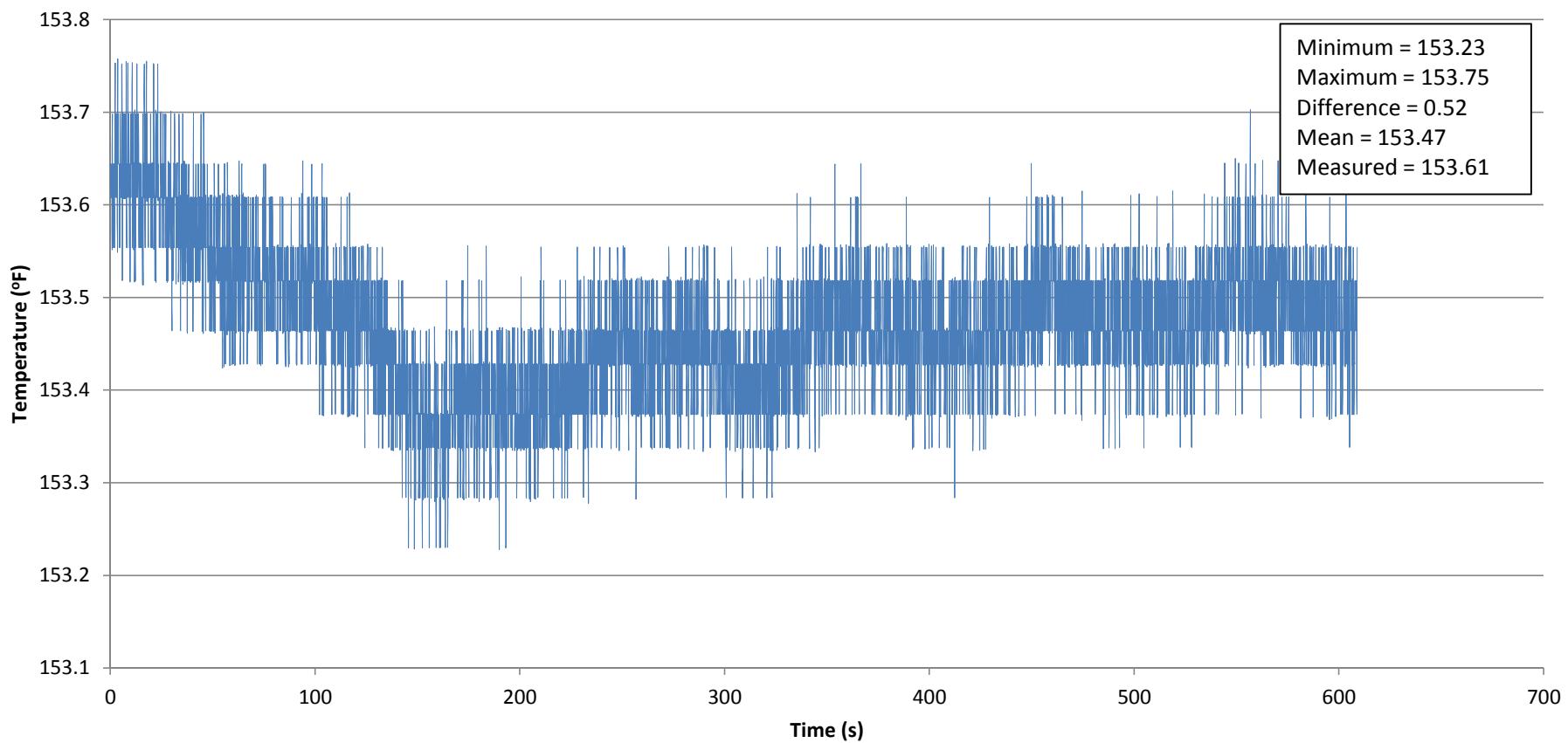


NDIC 8005
Sivertson #29-23R #1
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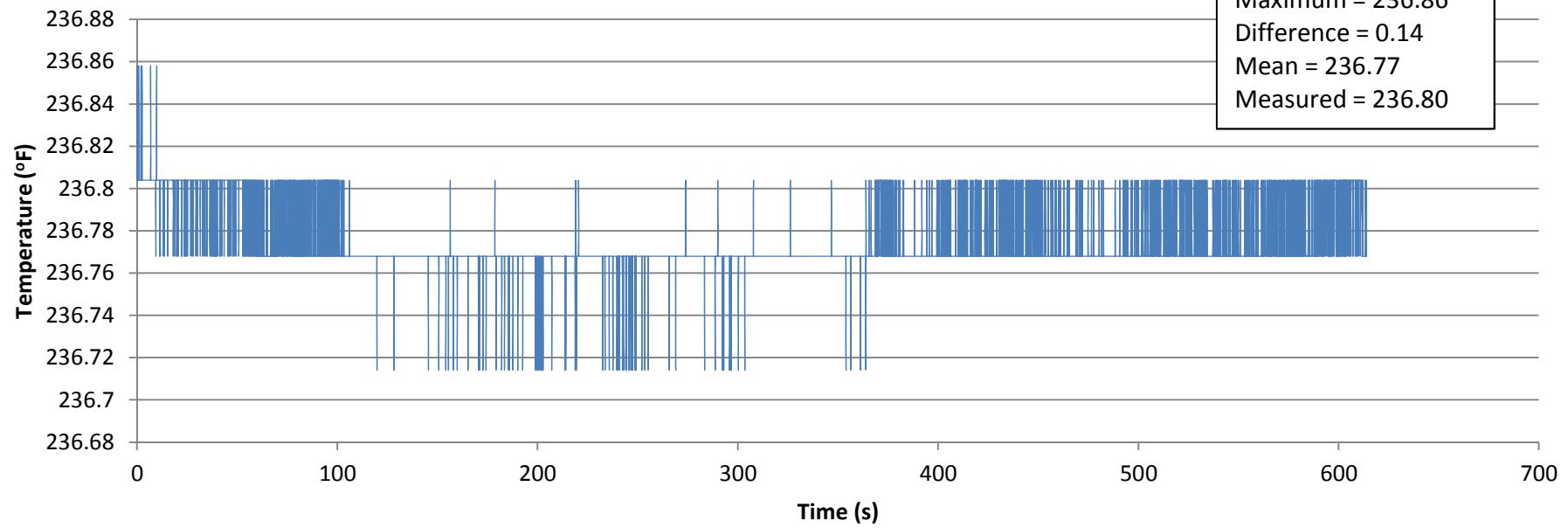


NDIC 8706
Berge C-1
McKenzie County, ND
Station Stop at 4500 ft

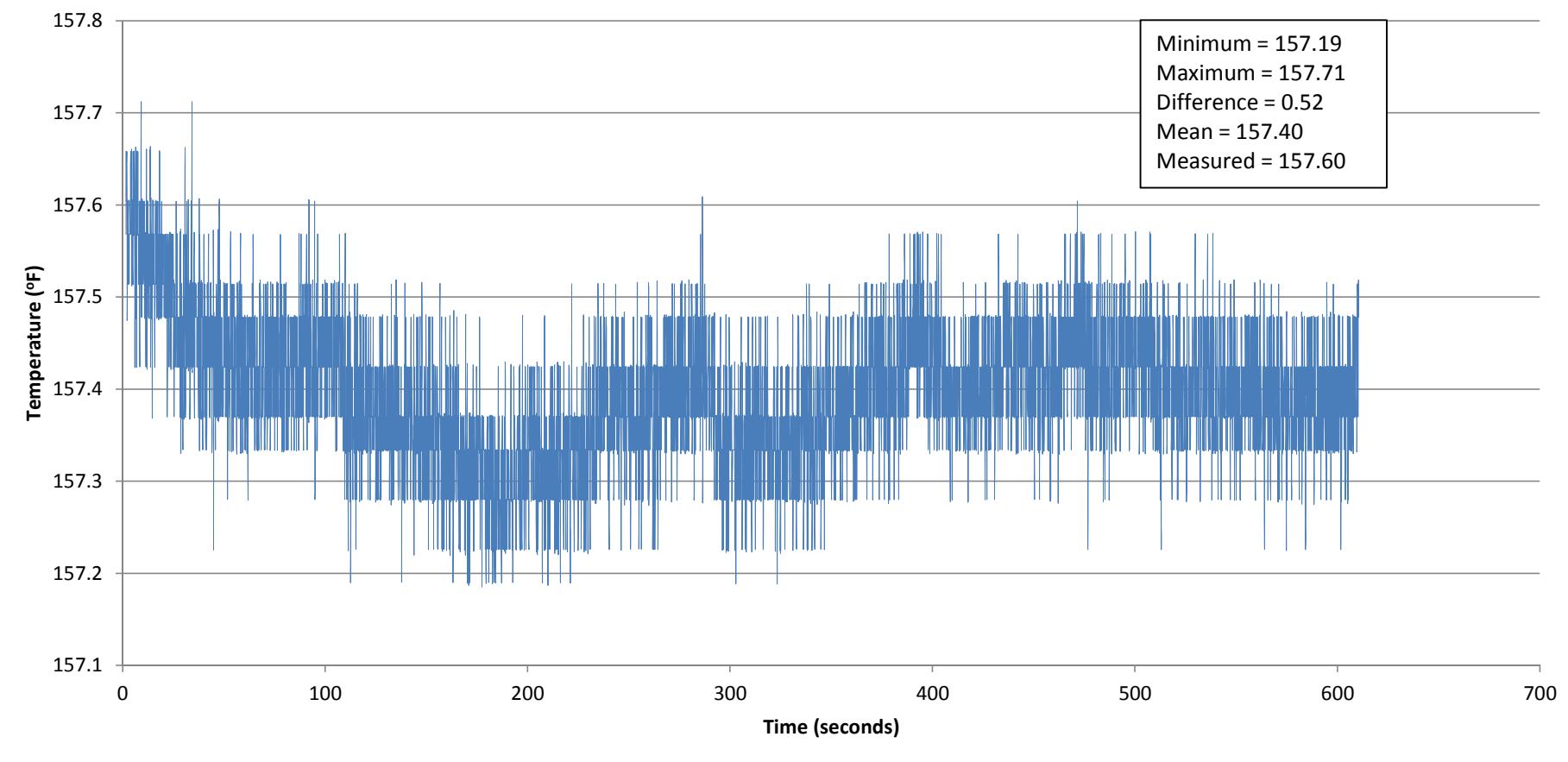


NDIC 8706
Berge C-1
McKenzie County, ND
Station Stop at 9000 ft

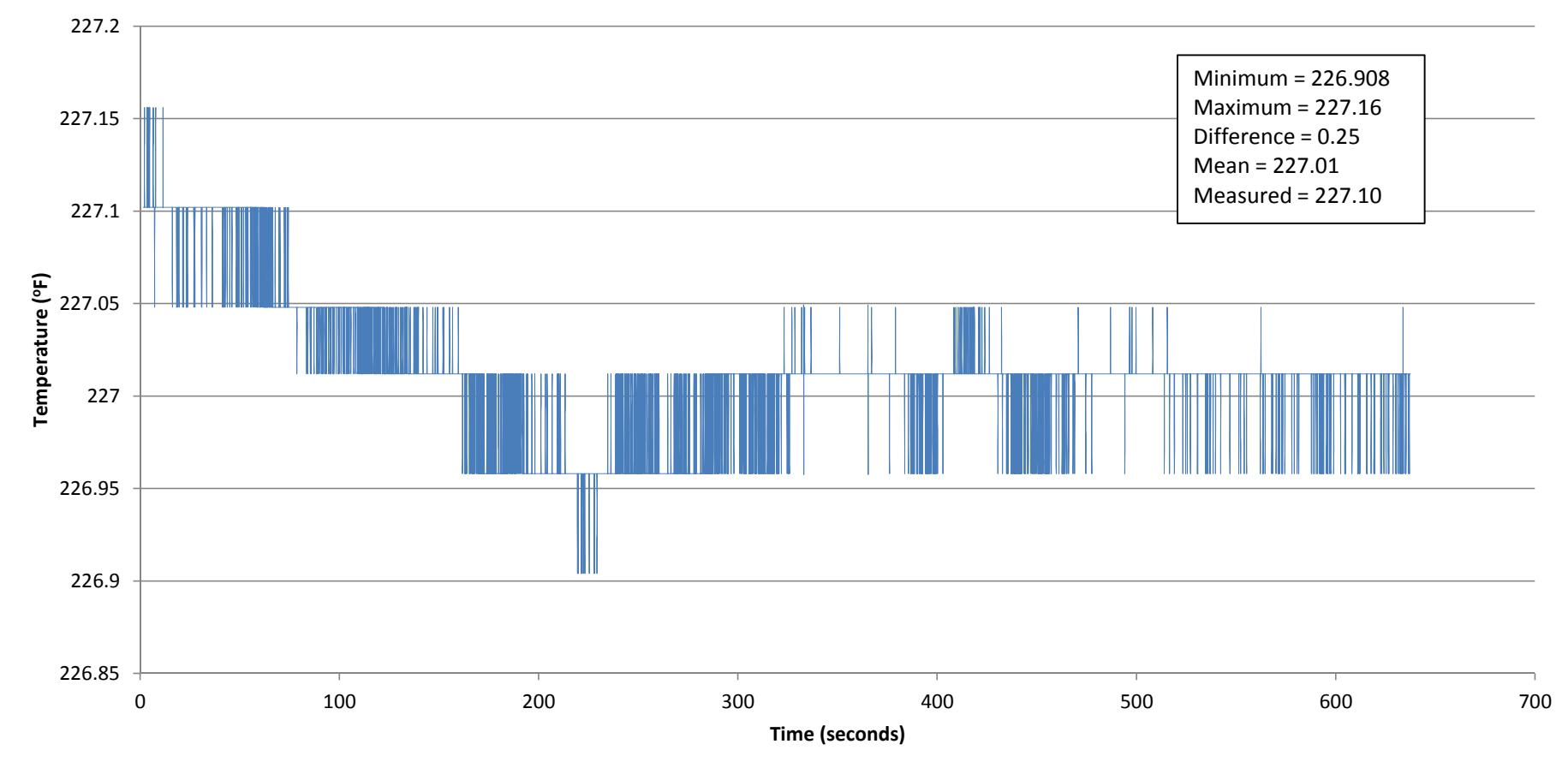
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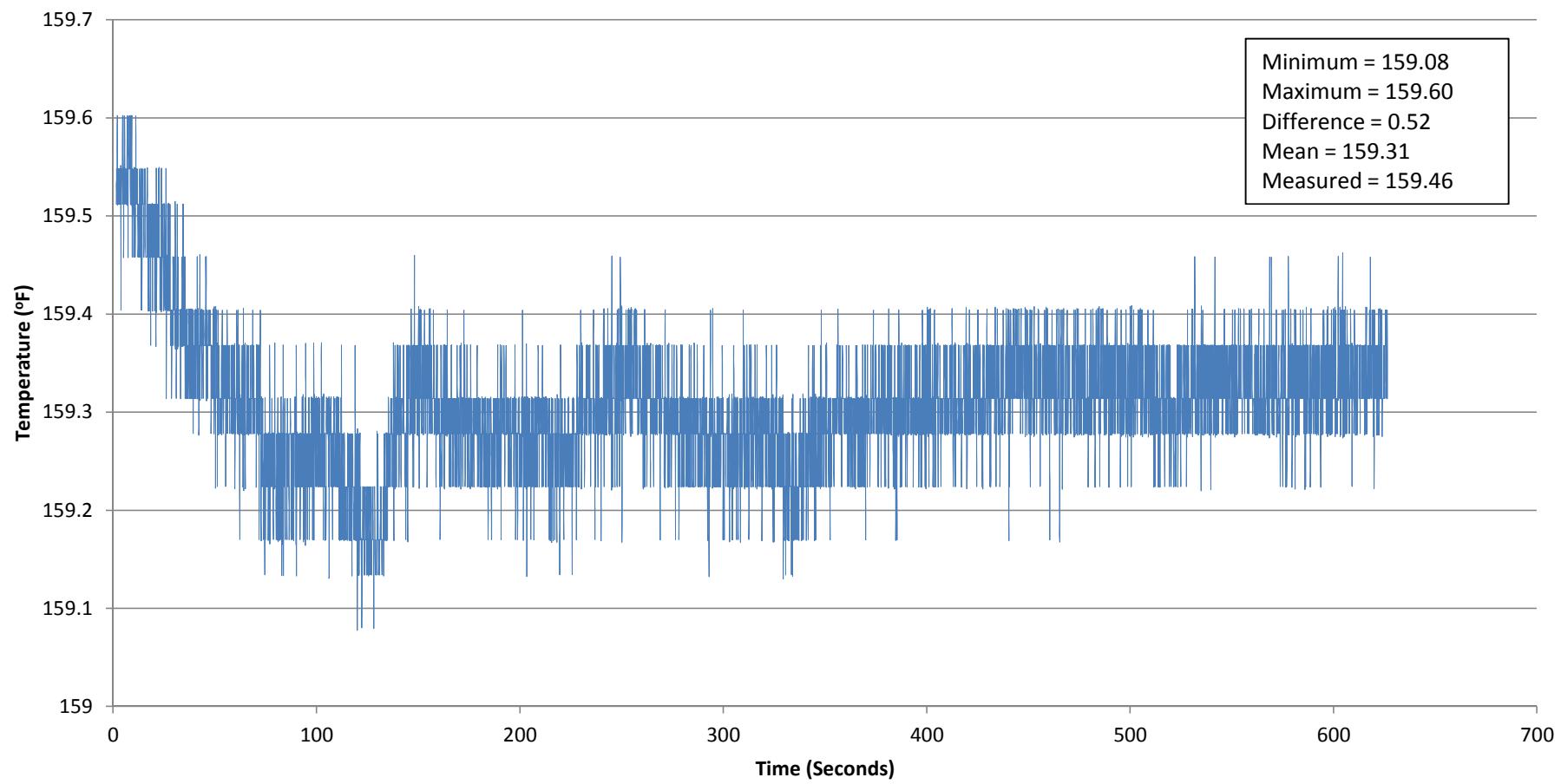
NDIC 9653
Cutlip 1
McKenzie County, ND
Station Stop at 5000 ft



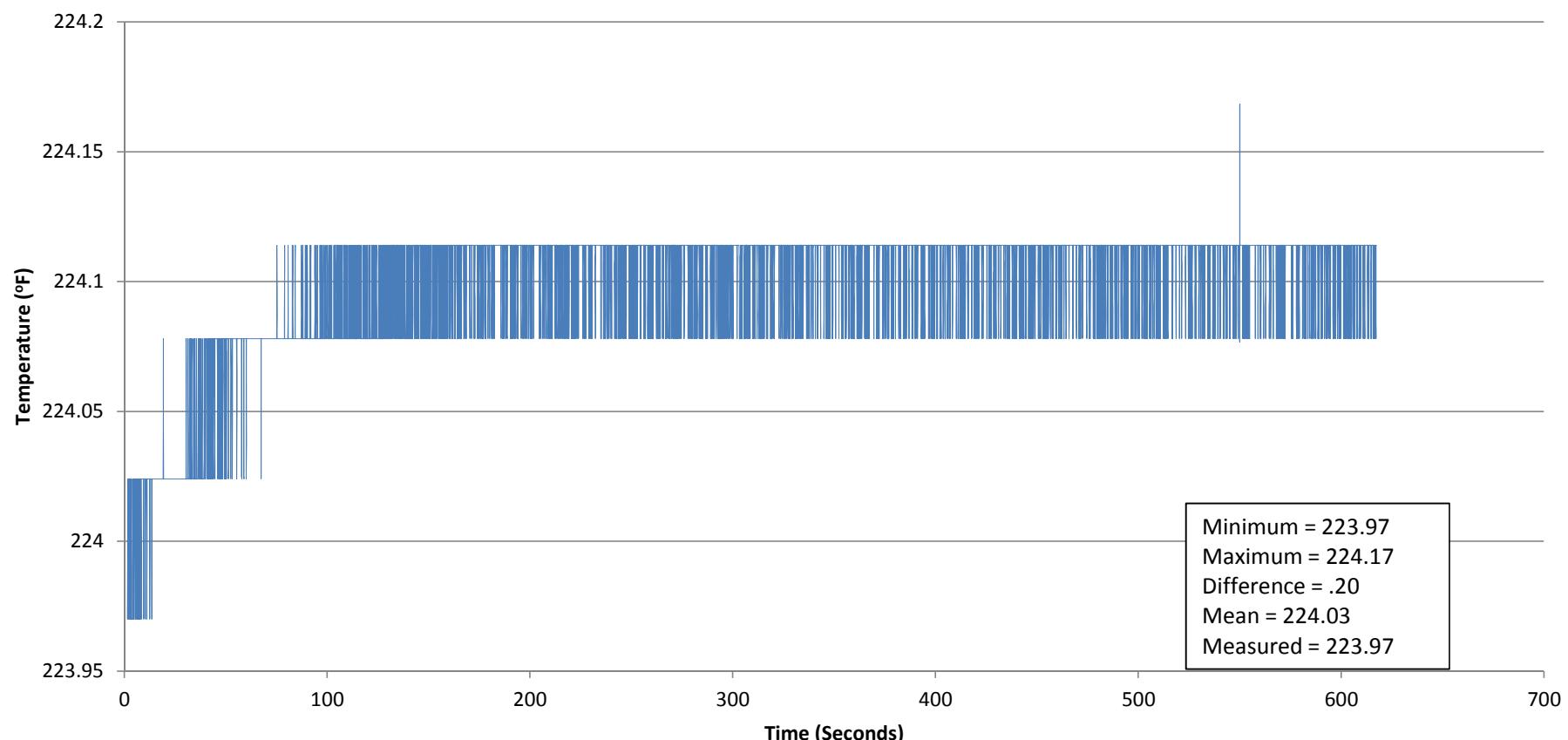
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Cutlip 1
McKenzie County, ND
Station Stop at 9300 ft



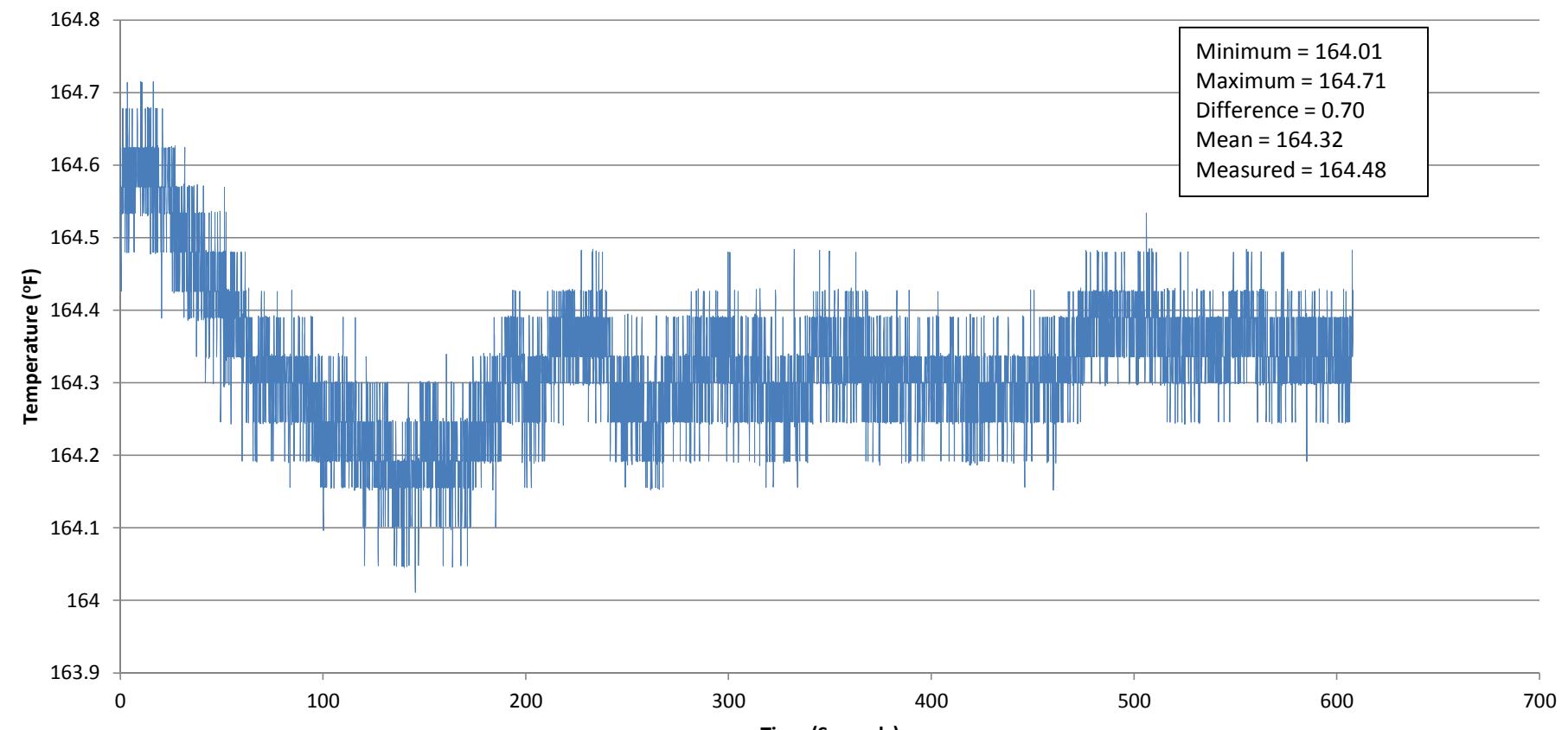
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McKenzie County, ND
Station Stop at 5000 ft



NDIC 10103
Iverson State A-1
McKenzie County, ND
Station Stop at 8700 ft

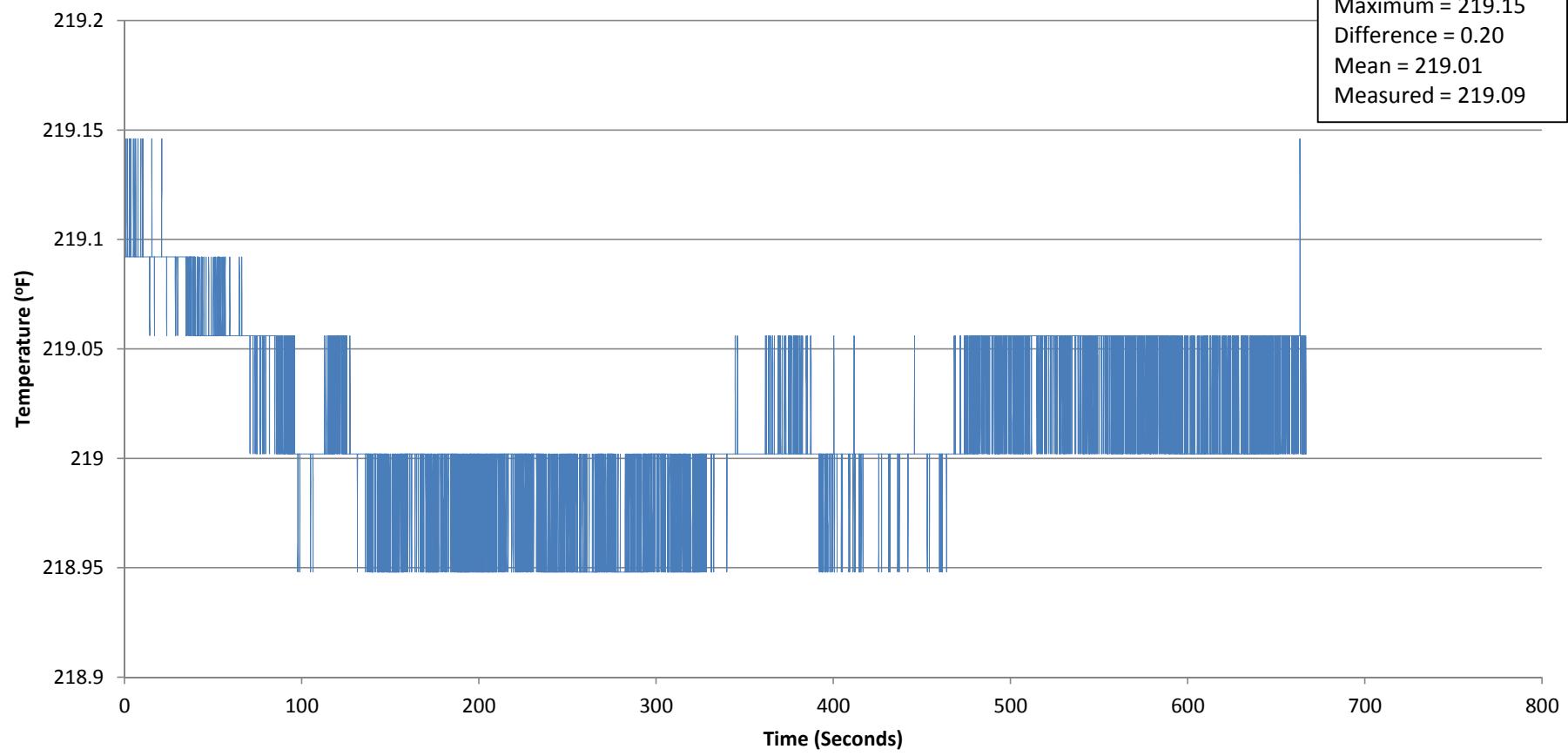


NDIC 10278
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Bowman County, ND
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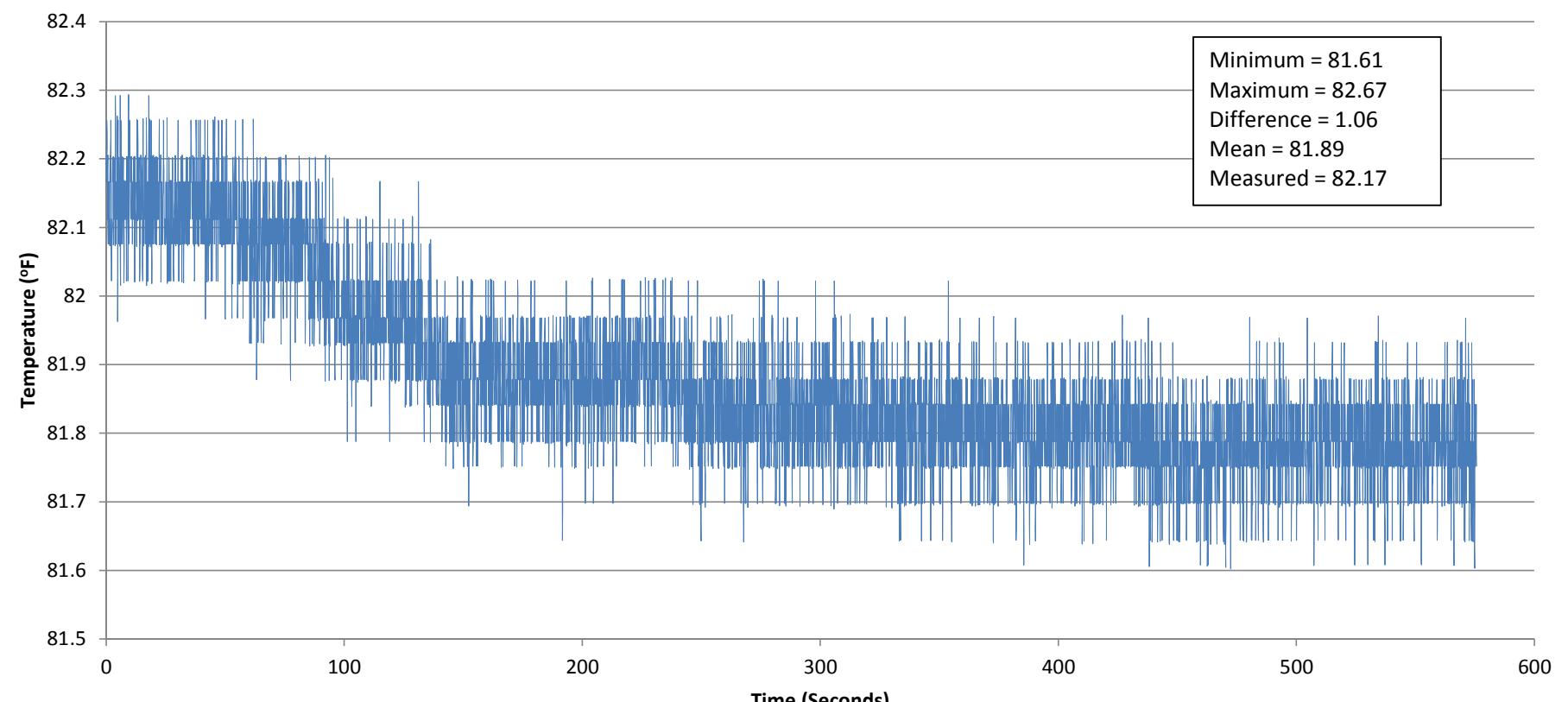


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Mud Buttes 1-36
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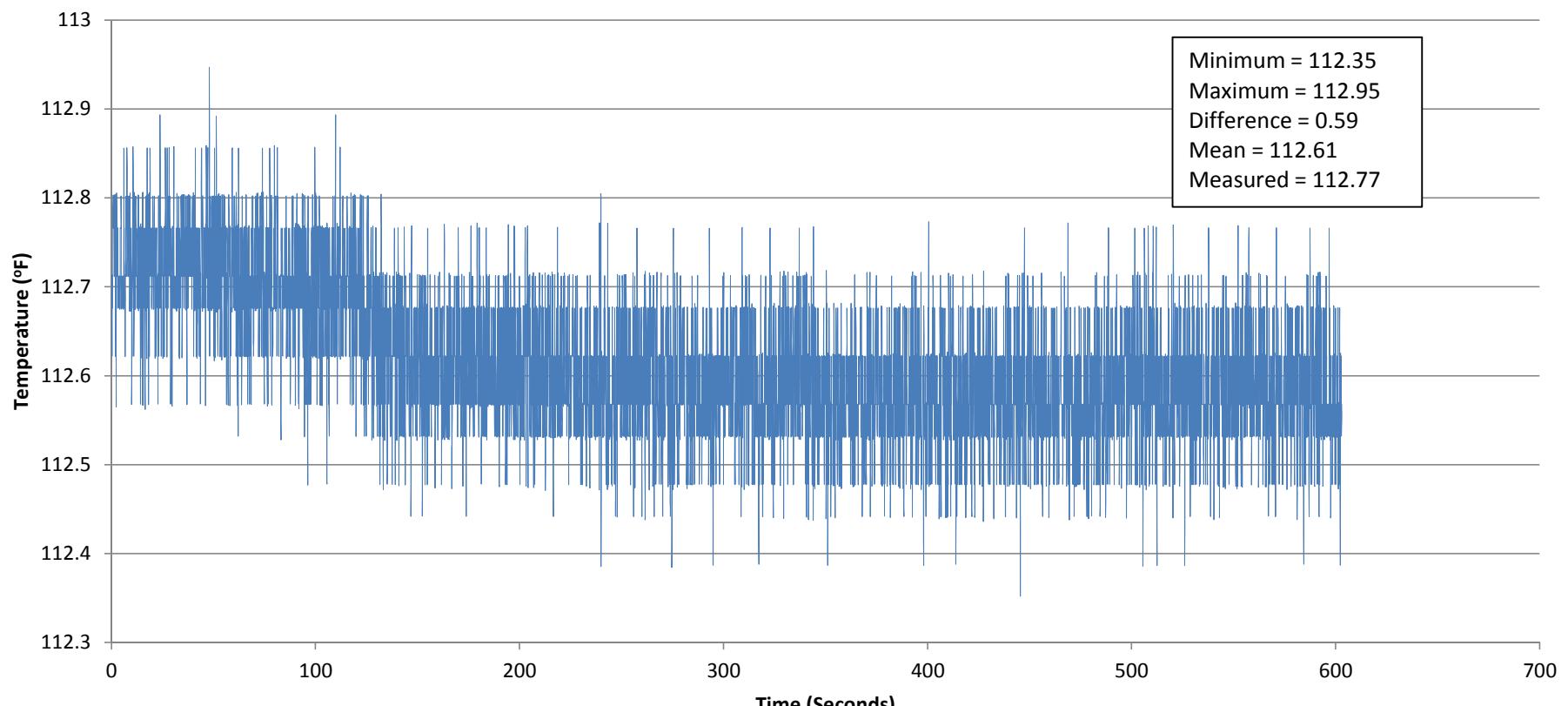
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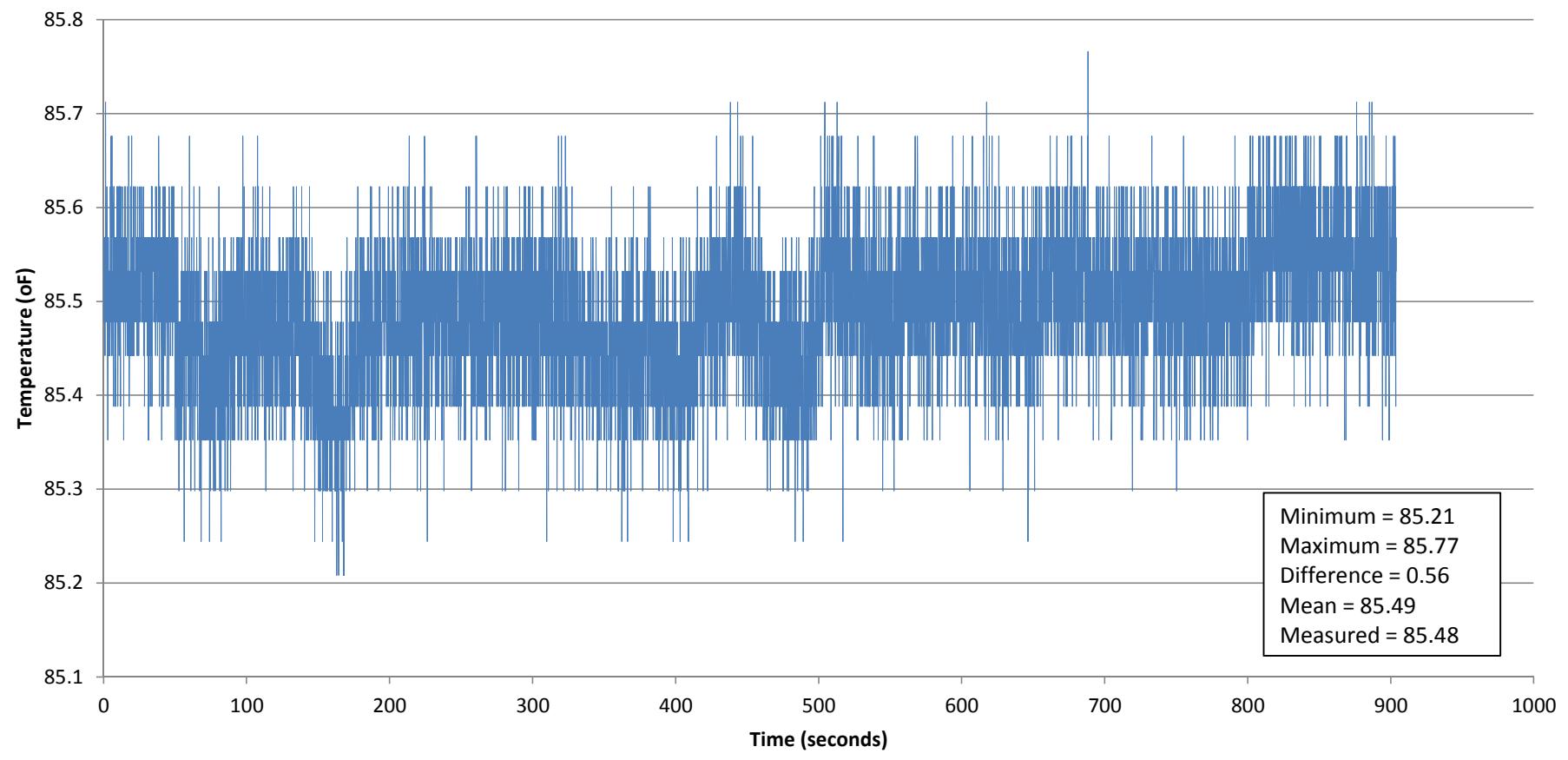
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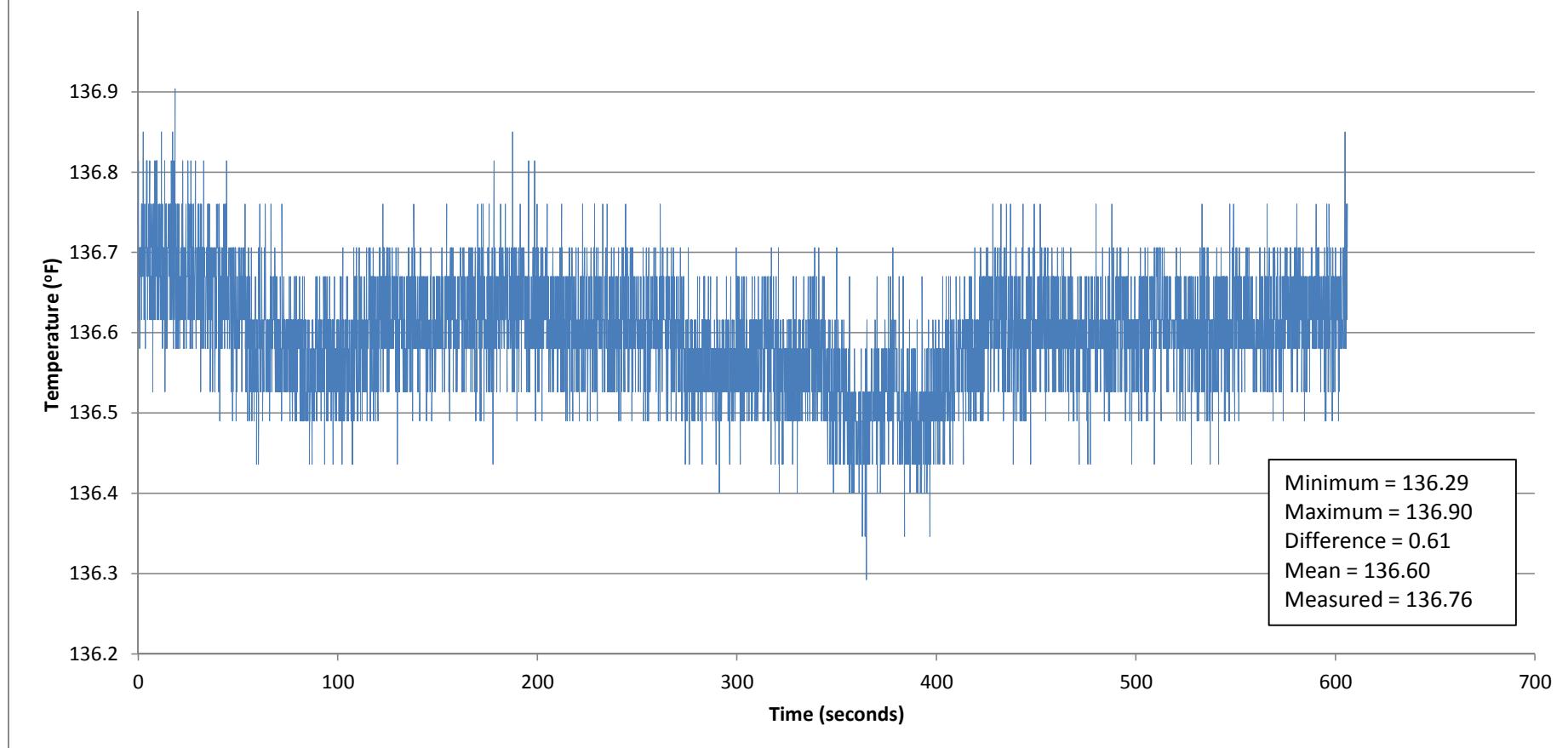
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Brandjord 1-20
Bottineau County, ND
Station Stop at 3000 ft



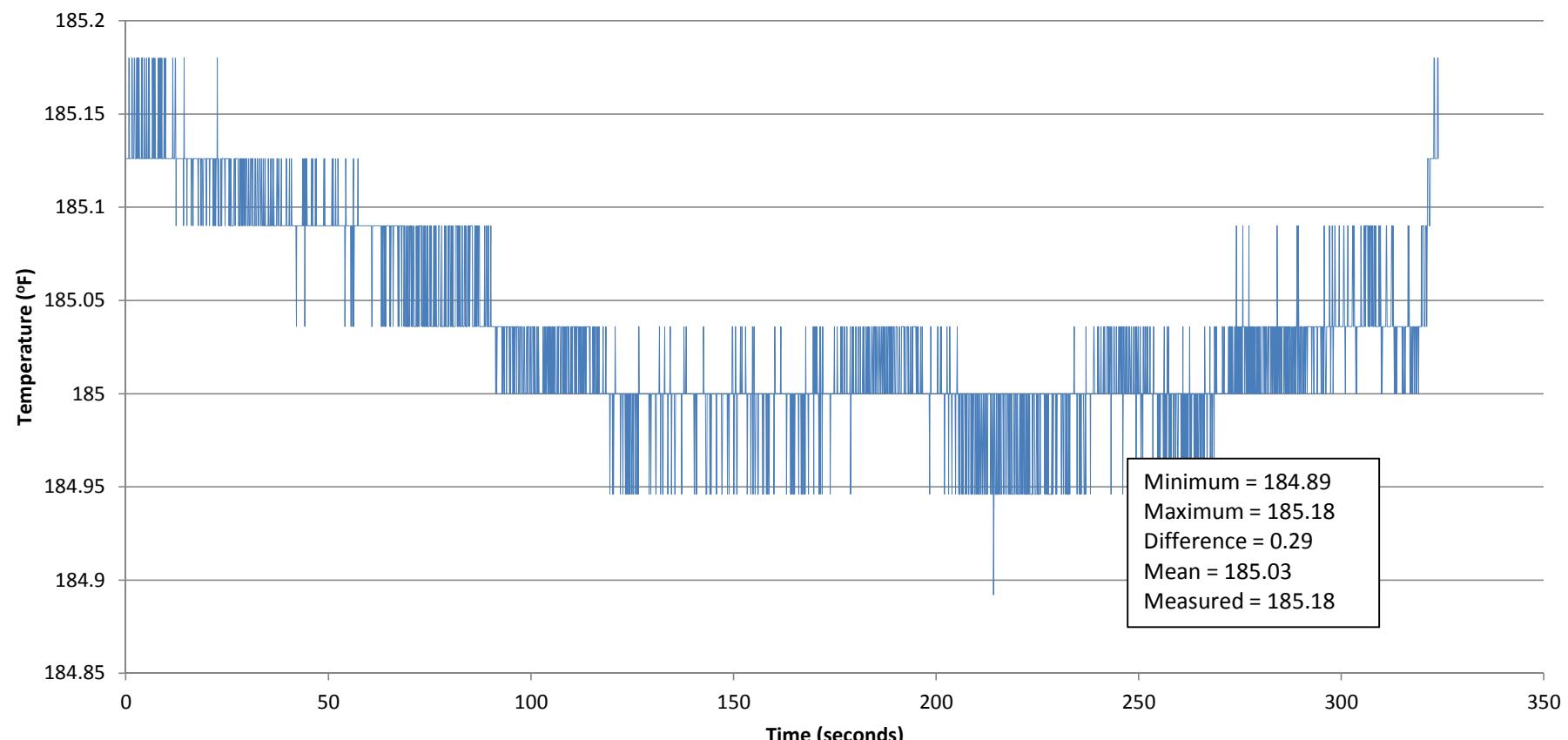
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Williams County, ND
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NDIC 12363
Astrid-Ongstad 14-22
Williams County, ND
Station Stop 4000 ft

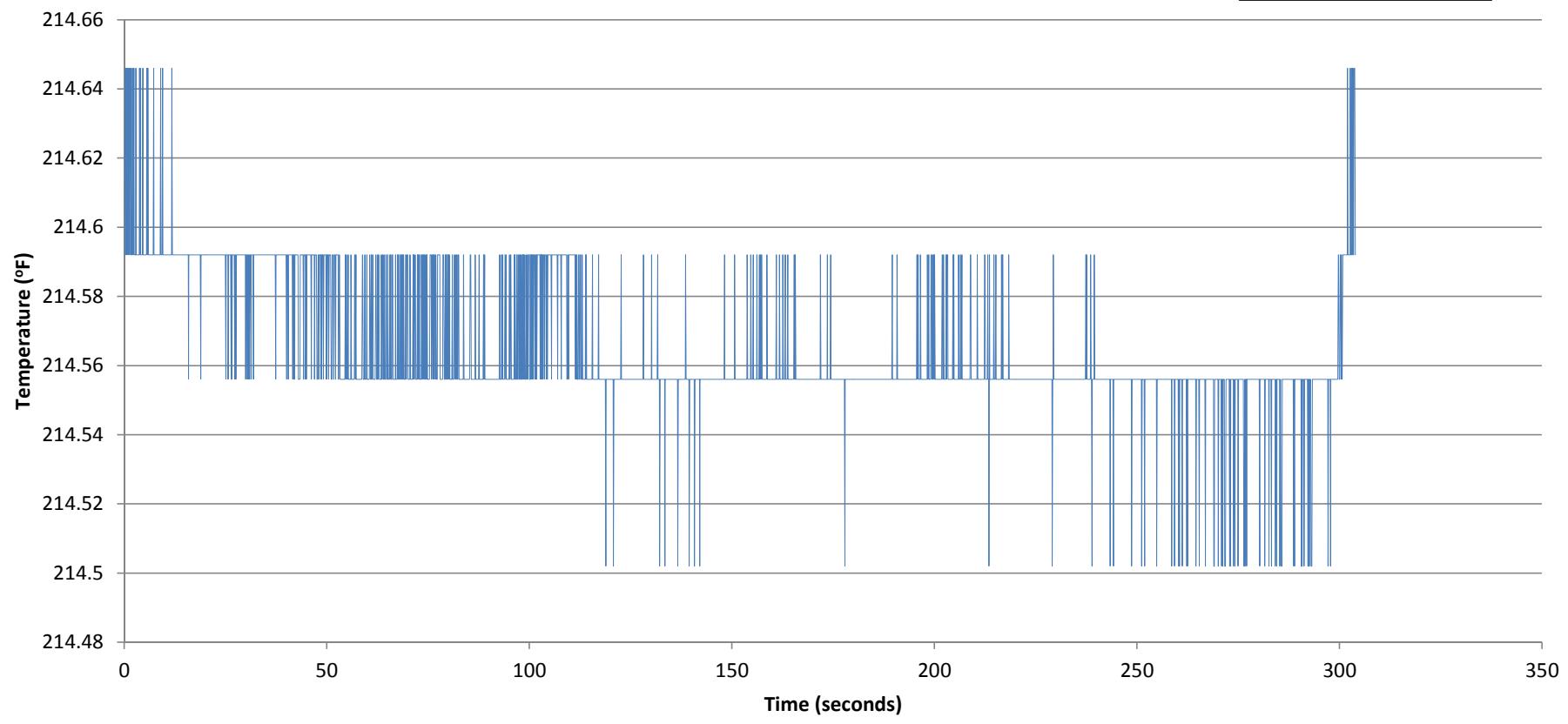


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Williams County, ND
Station Stop and 6000 ft



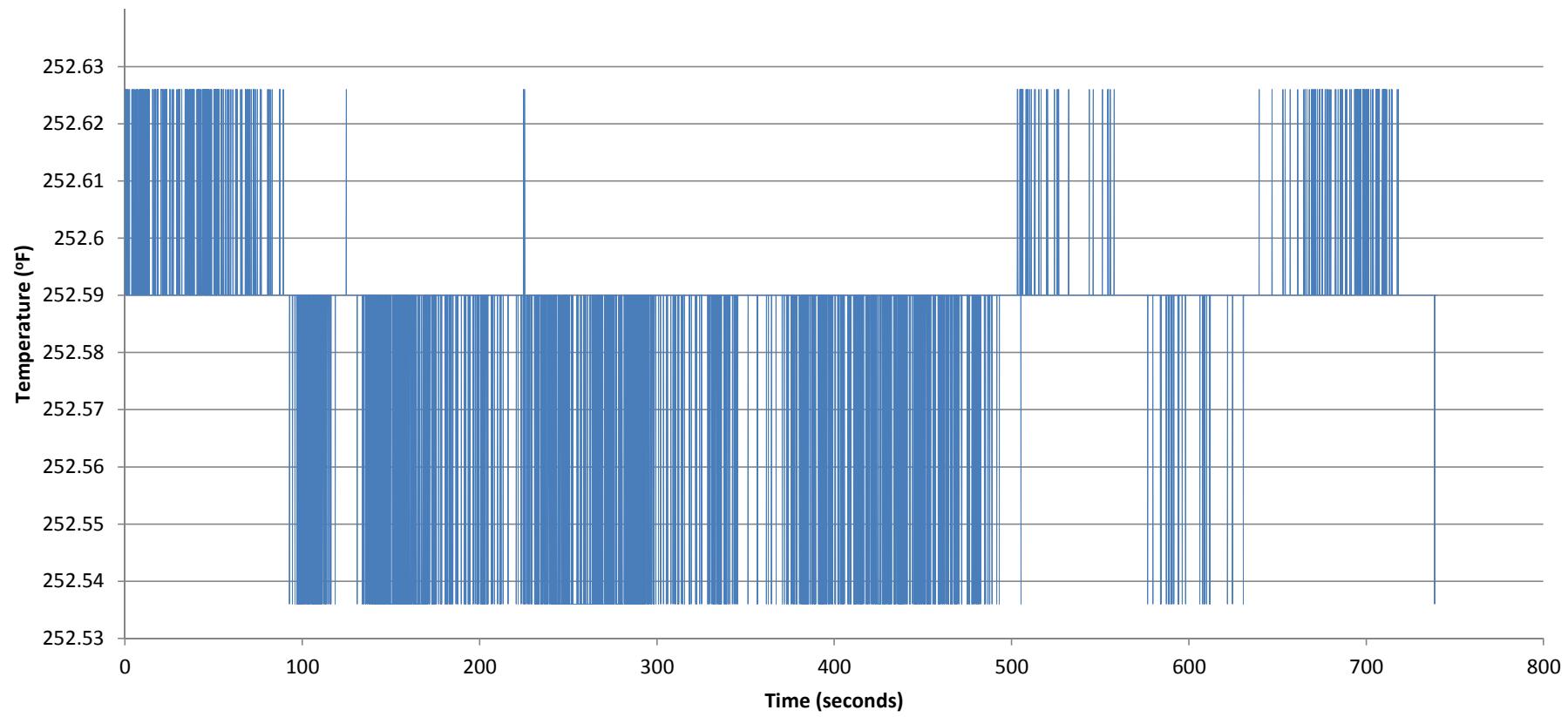
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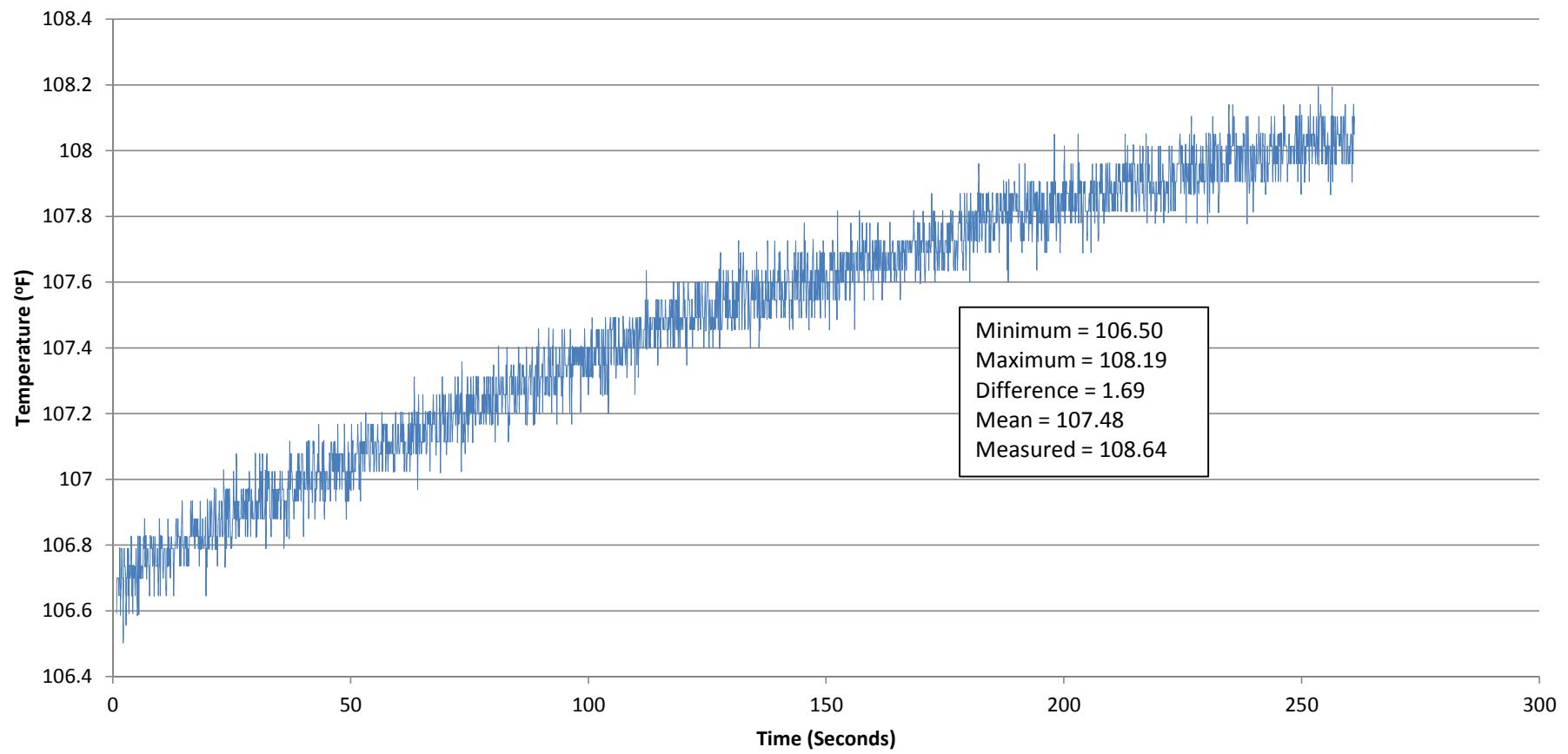


NDIC 12363
Astrid-Ongstad 14-22
Williams County, ND
Station Stop 11,000 ft

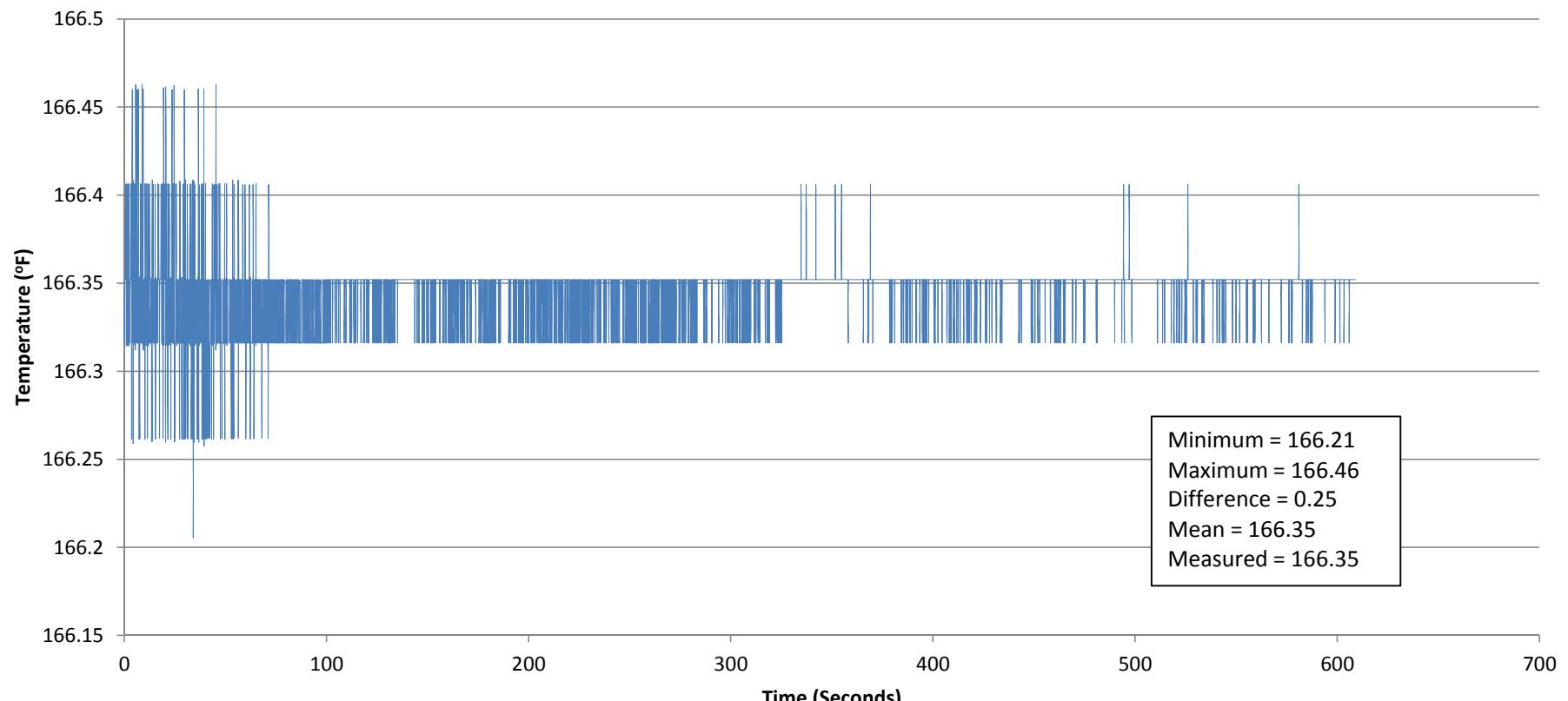
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McClean County, ND
Station Stop at 3800 ft

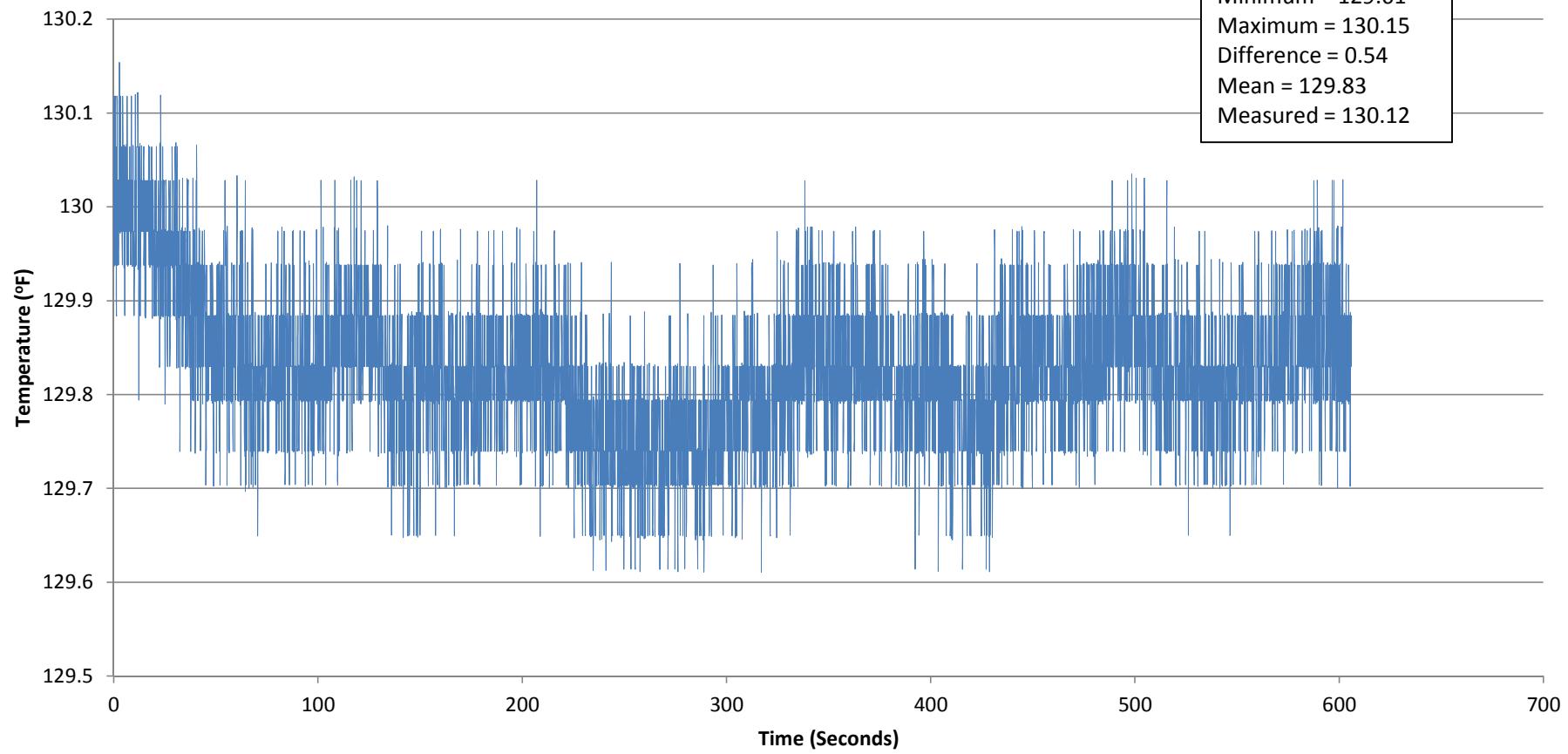


NDIC 13132
Frink 13-15
McClean County, ND
Station Stop at 7600 ft

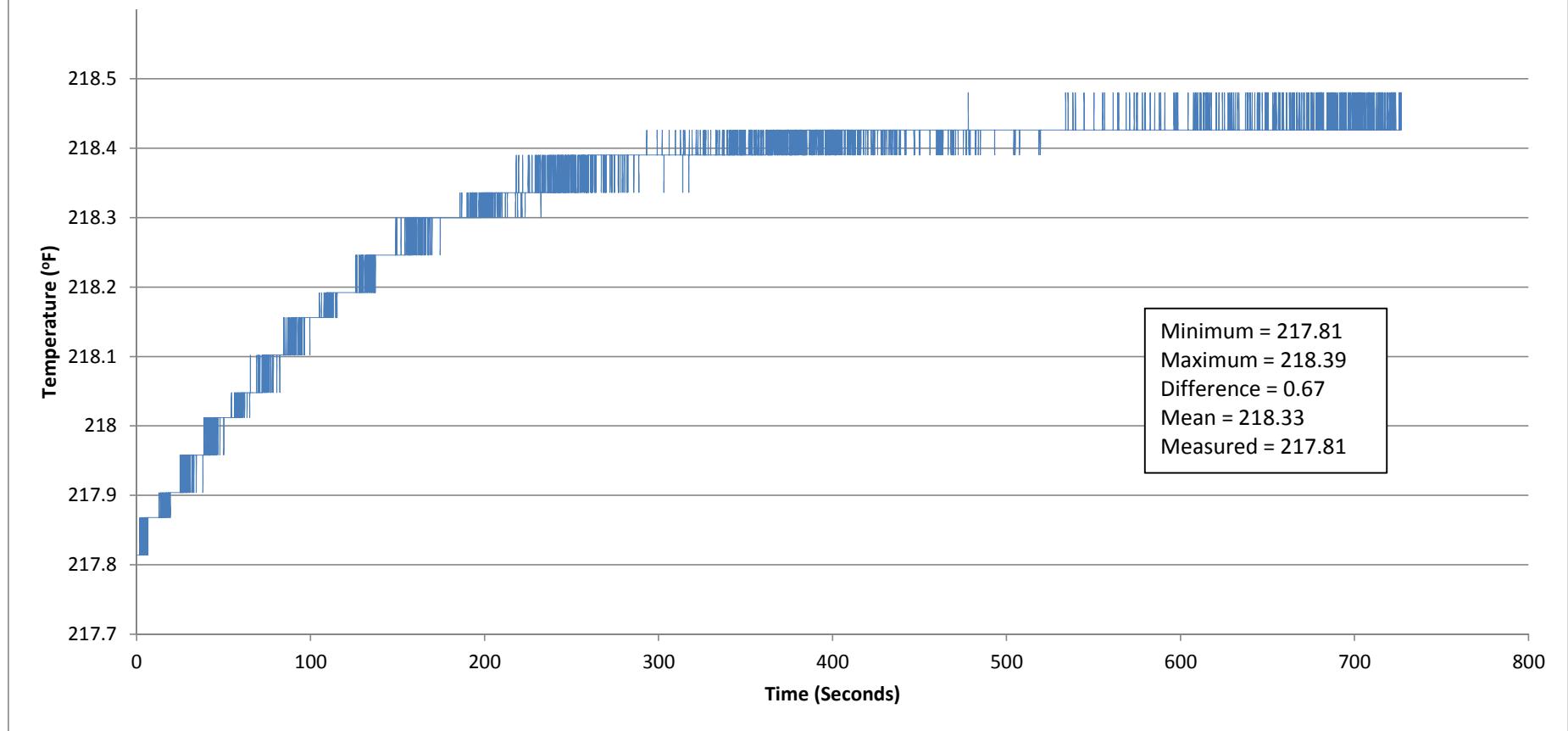


NDIC 13666
Rieder 1-9 SWD
Williams County, ND
Station Stop at 4000 ft

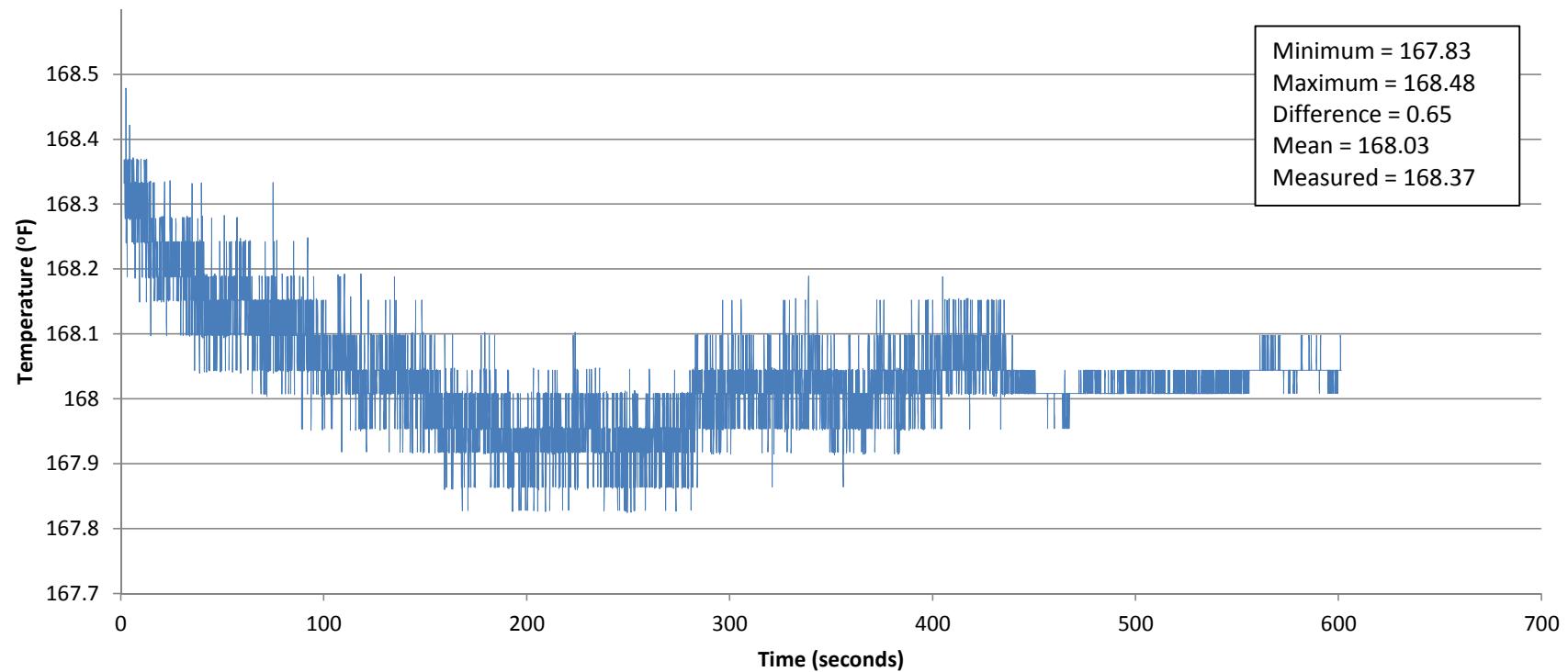
Minimum = 129.61
Maximum = 130.15
Difference = 0.54
Mean = 129.83
Measured = 130.12



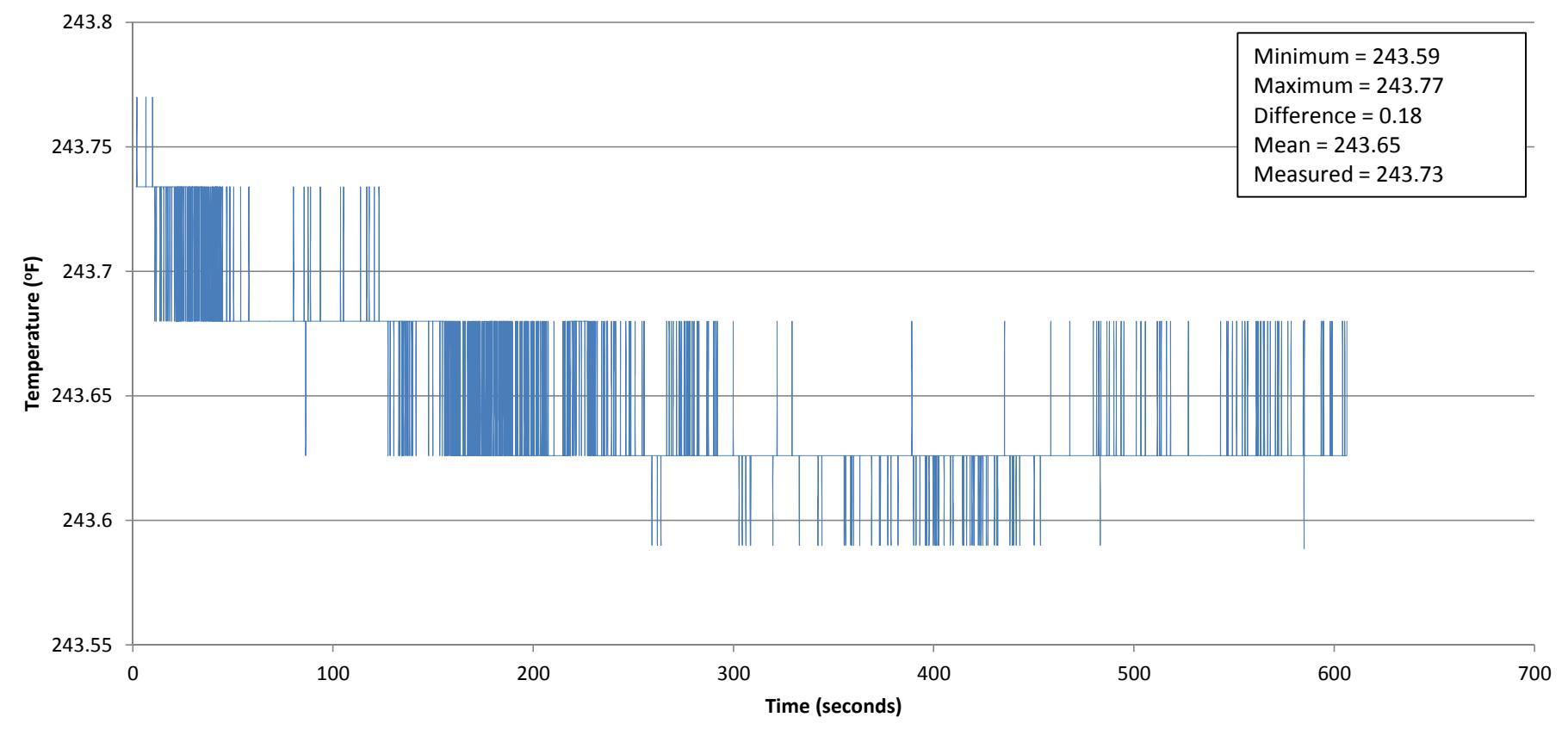
NDIC 13666
Rieder 1-9 SWD
Williams County, ND
Station Stop at 8800 ft



NDIC 15137
Holte 6-21
Burke County, ND
Station Stop at 5000 ft

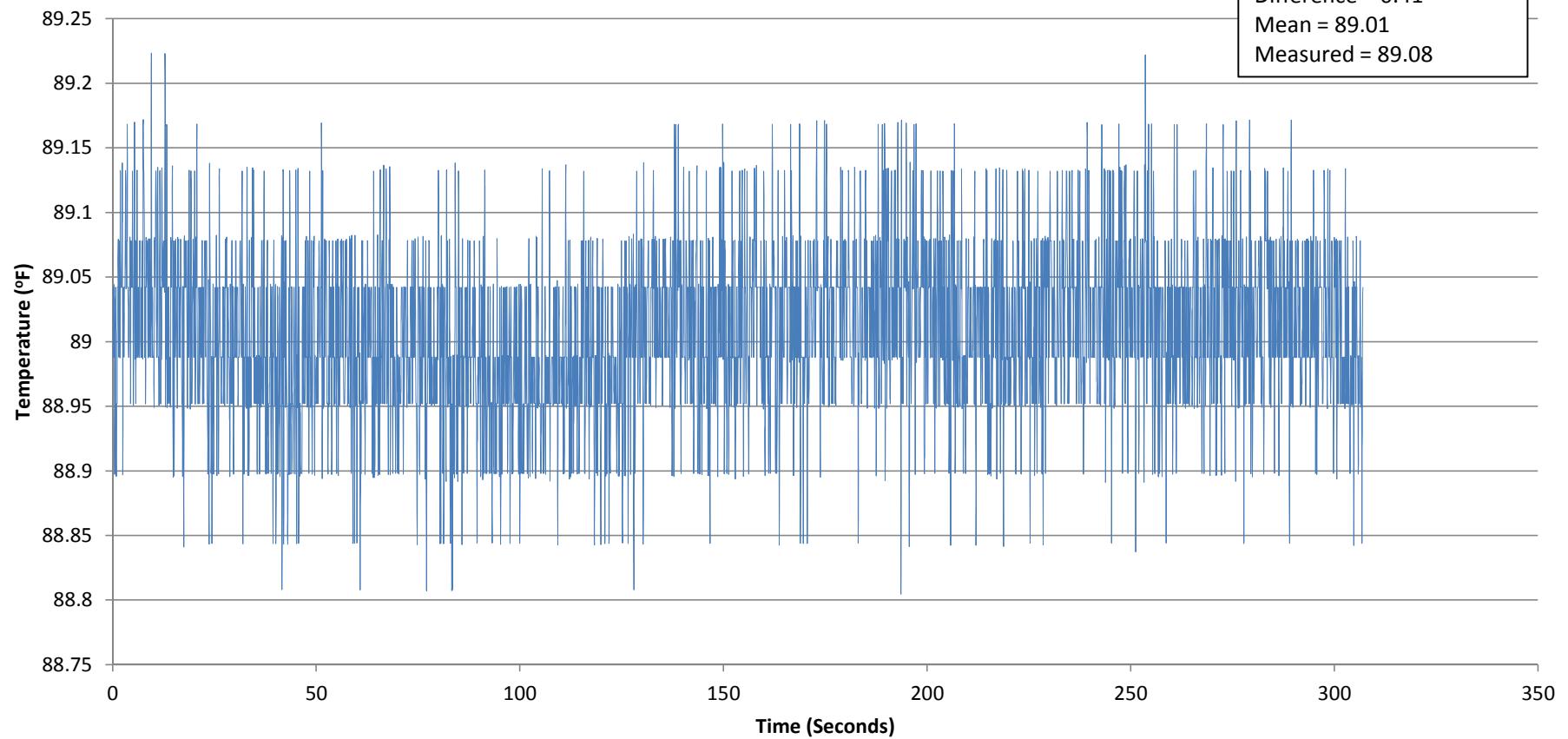


NDIC 15137
Holte 6-21
Burke County, ND
Station Stop at 10,200 ft



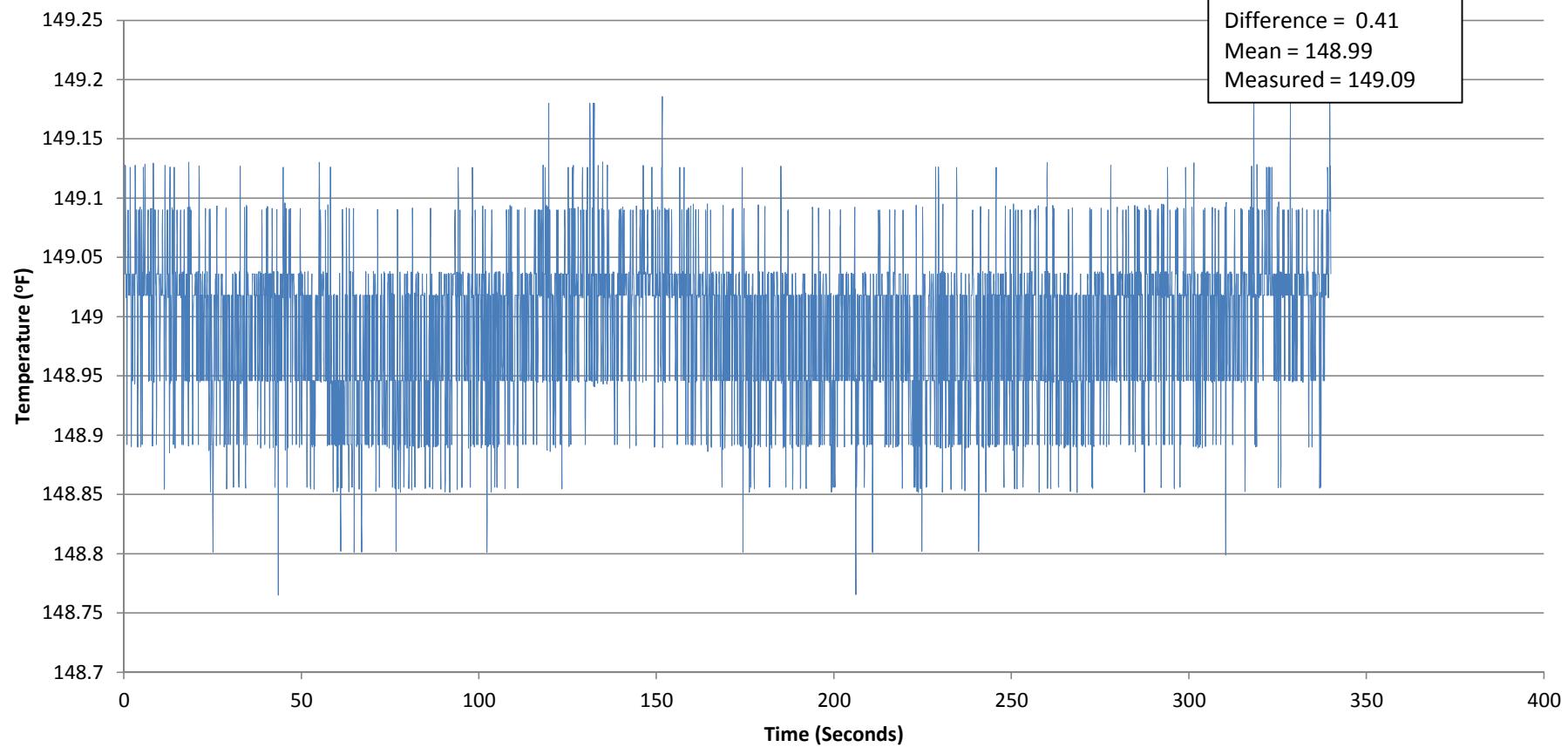
NDIC 15593
FHMU K-810
Billings County, ND
Station Stop at 2000 ft

Minimum = 88.81
Maximum = 89.22
Difference = 0.41
Mean = 89.01
Measured = 89.08



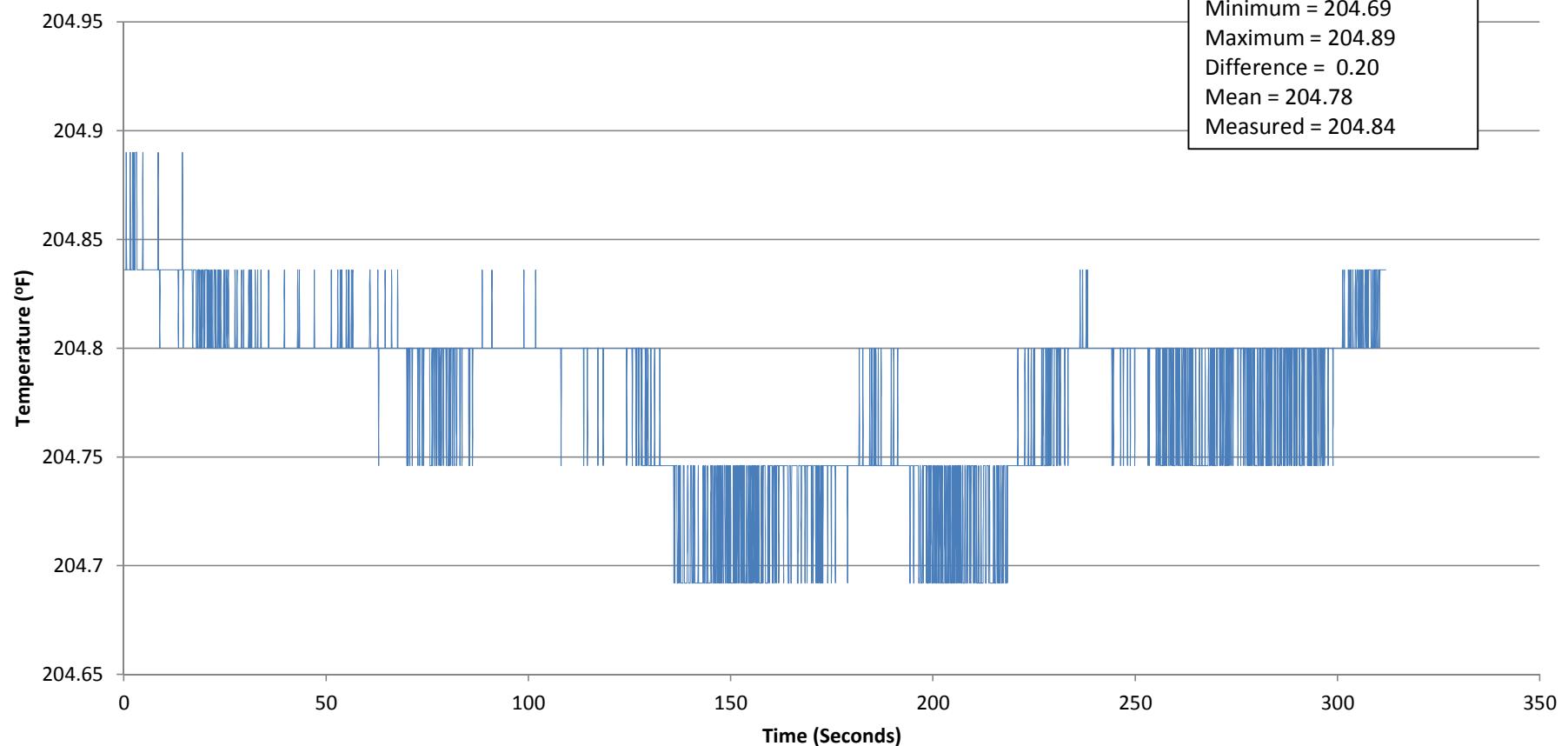
NDIC 15593
FHMU K-810
Billings County, ND
Station Stop at 4000 ft

Minimum = 148.77
Maximum = 149.18
Difference = 0.41
Mean = 148.99
Measured = 149.09

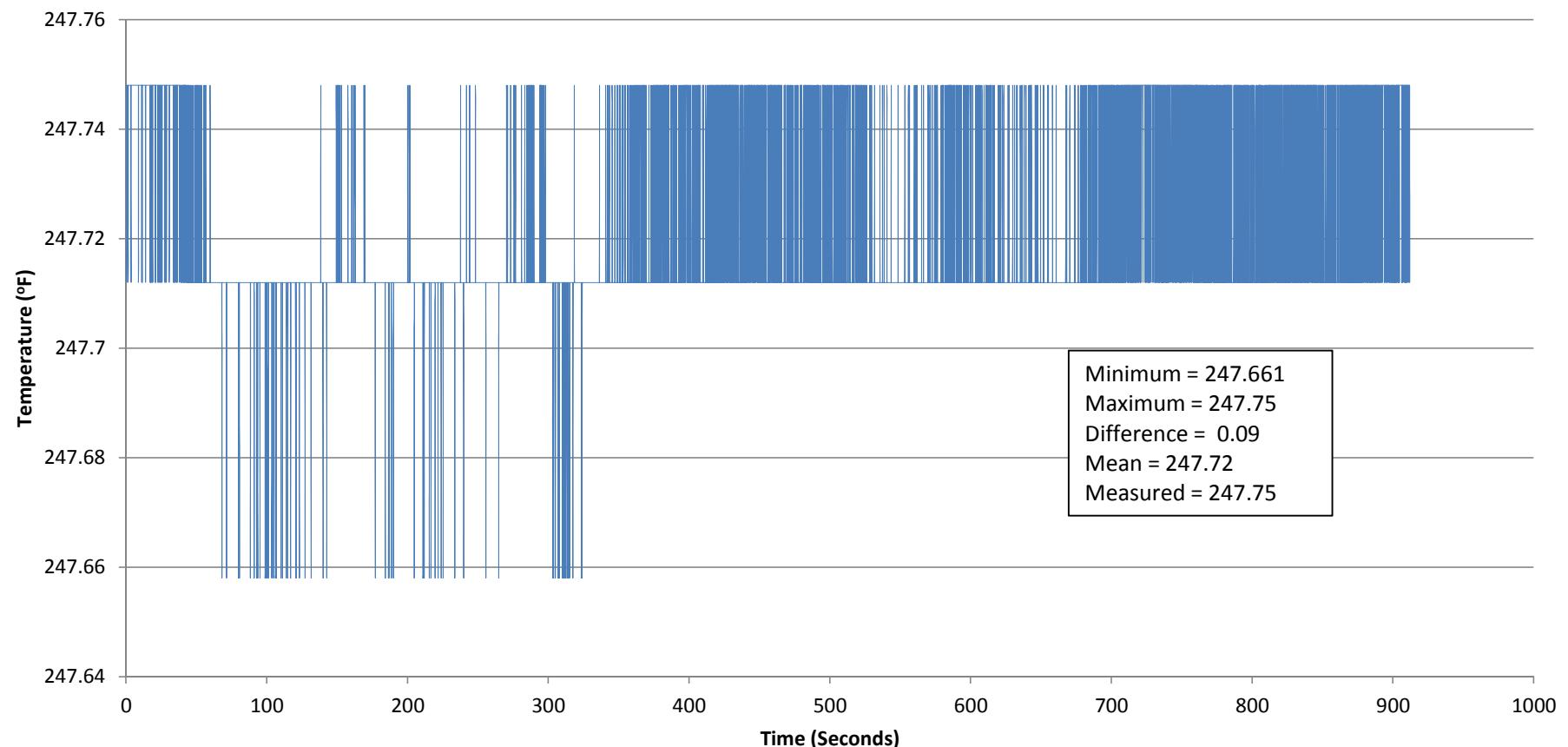


NDIC 15593
FHMU K-810
Billings County, ND
Station Stop at 6000 ft

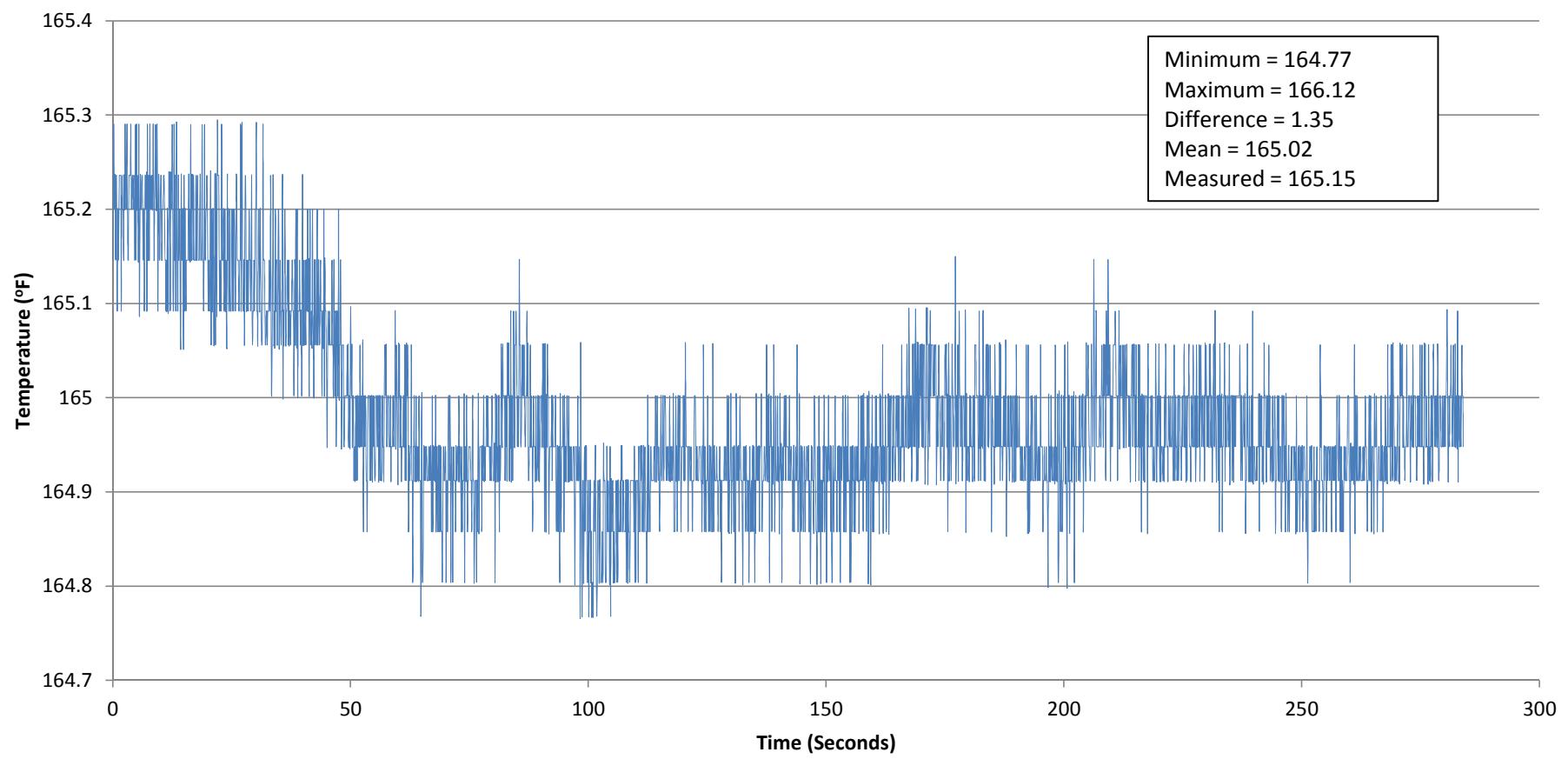
Minimum = 204.69
Maximum = 204.89
Difference = 0.20
Mean = 204.78
Measured = 204.84



NDIC 15593
FHMU K-810
Billings County, ND
Station Stop at 9000 ft

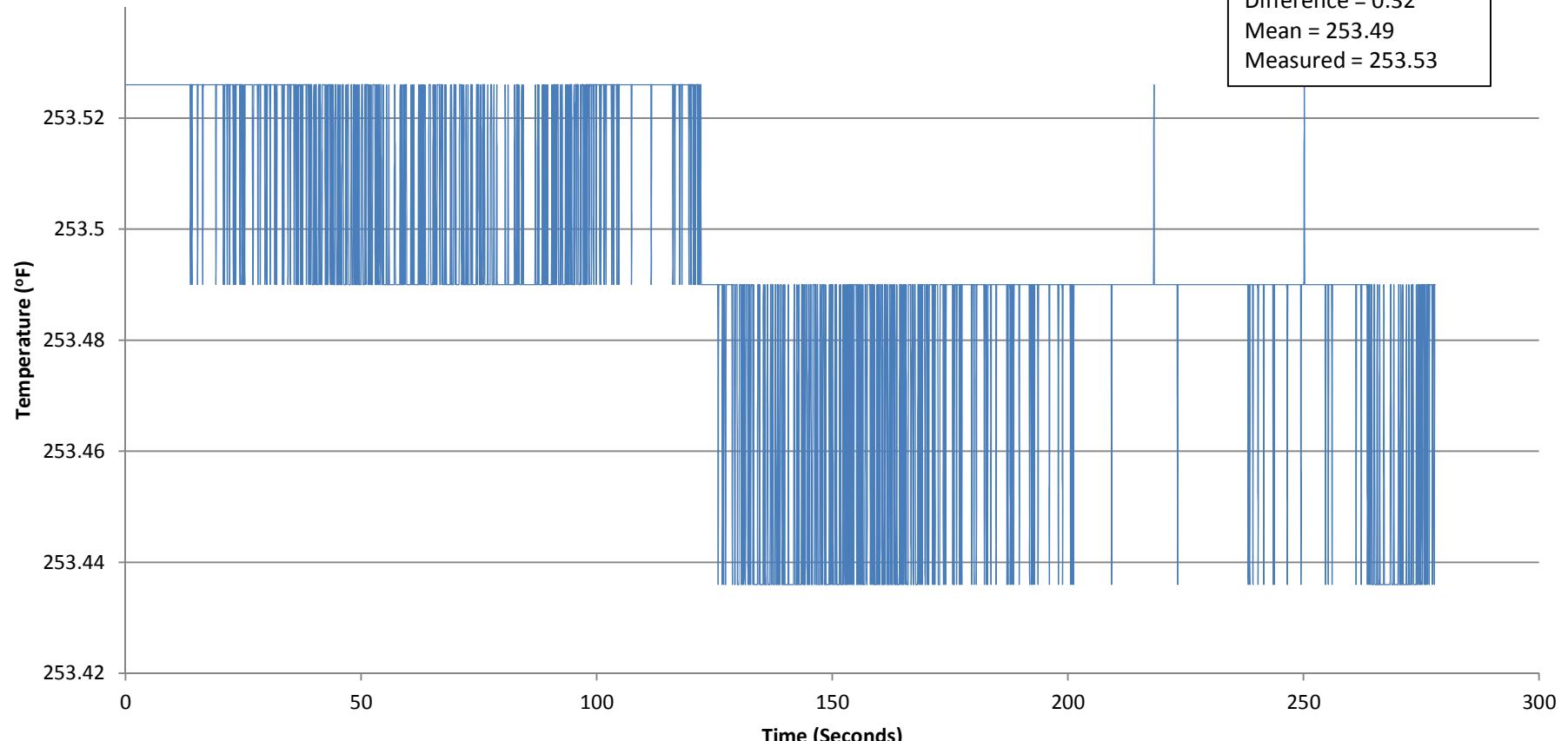


NDIC 15785
Ann 1
McKenzie County, ND
Station Stop at 5000 ft



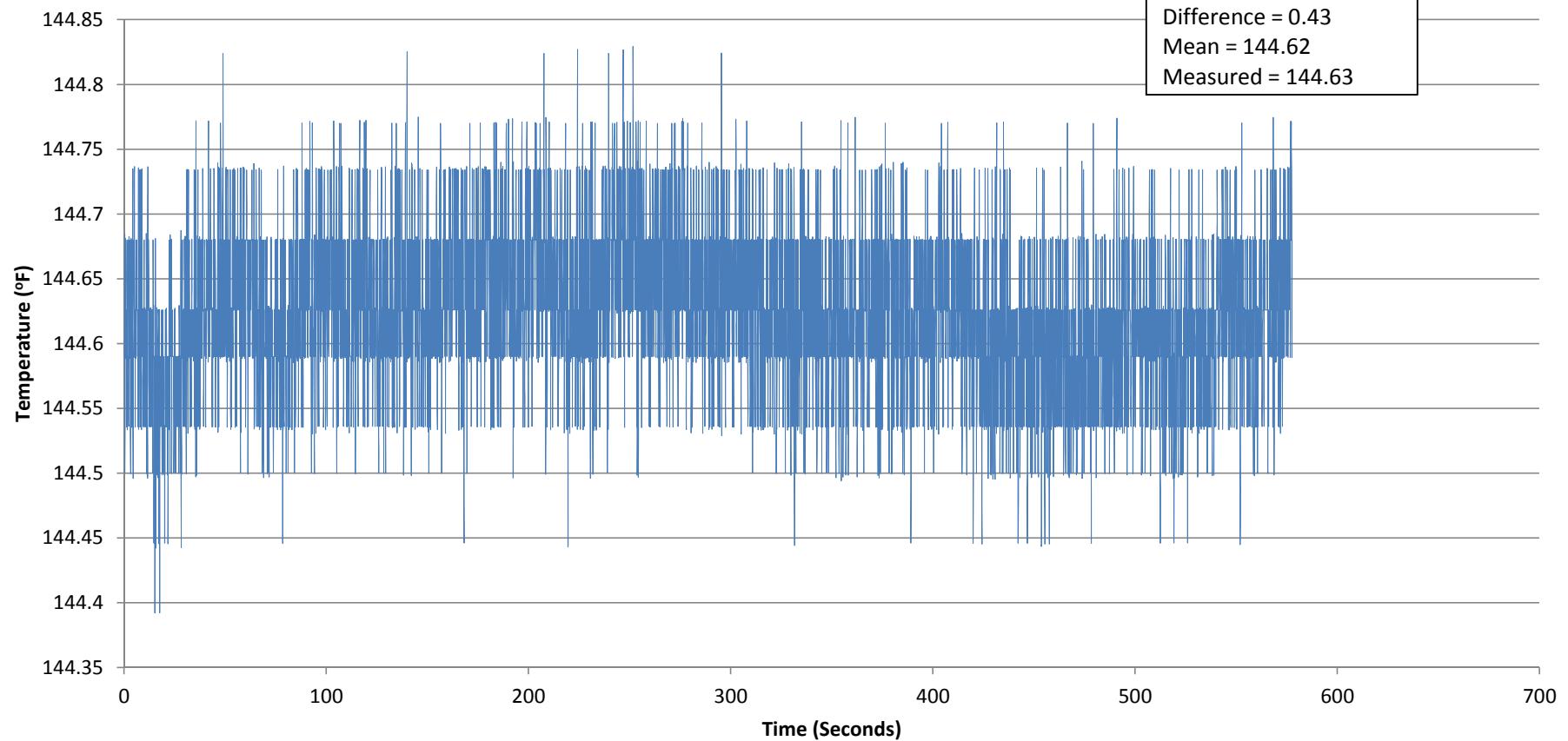
NDIC 15785
Ann 1
McKenzie County, ND
Station Stop 10,300 ft

Minimum = 253.20
Maximum = 253.53
Difference = 0.32
Mean = 253.49
Measured = 253.53

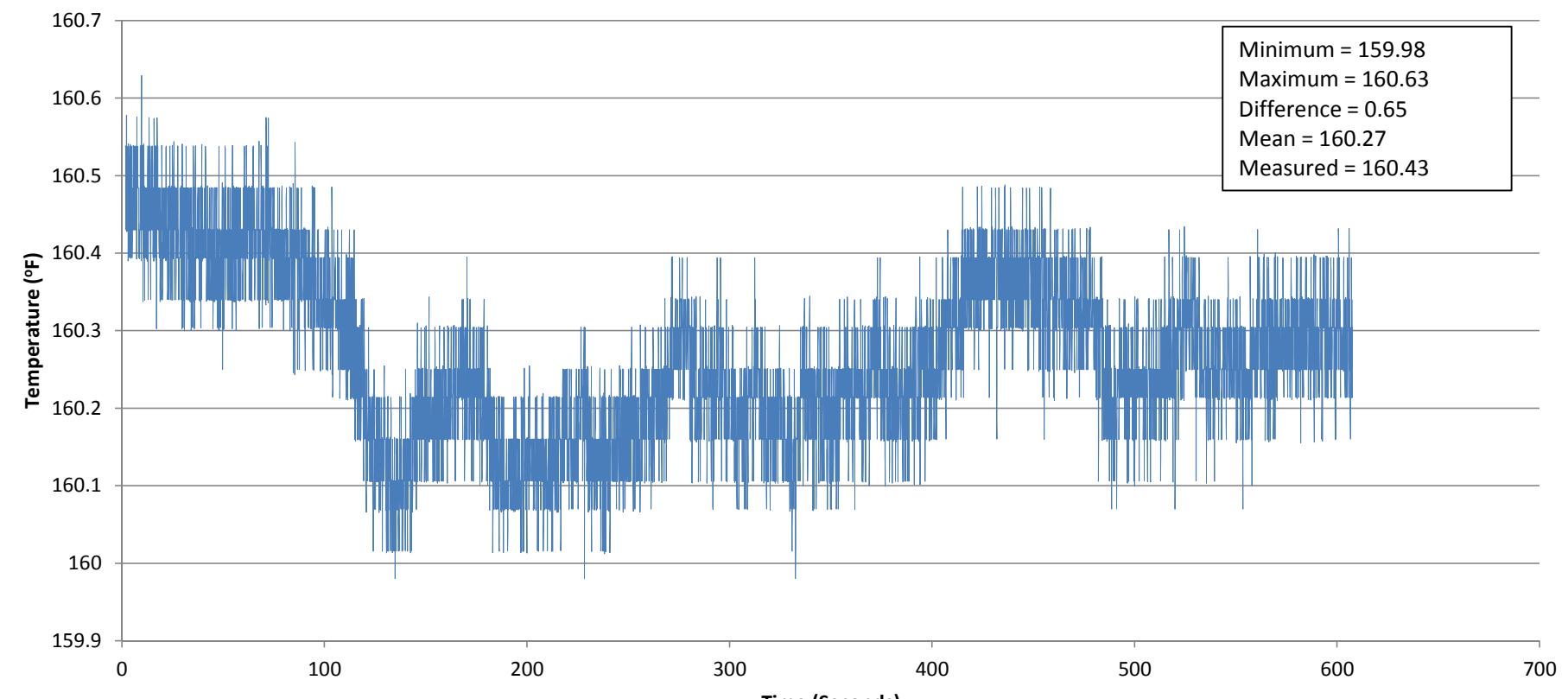


NDIC 16160
Nelson 1-11H
Mountrail County, ND
Station Stop at 4500 ft

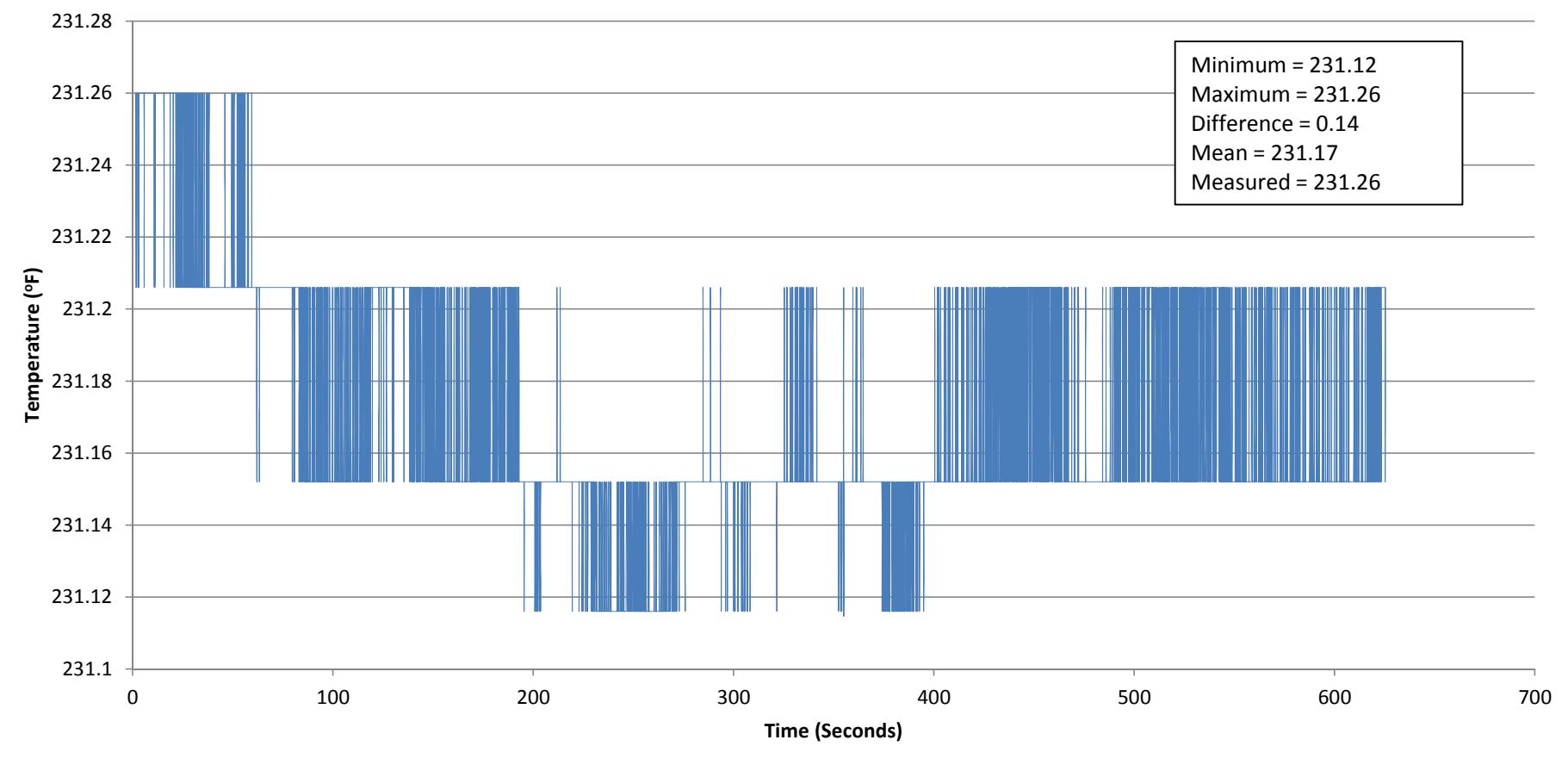
Minimum = 144.39
Maximum = 144.82
Difference = 0.43
Mean = 144.62
Measured = 144.63



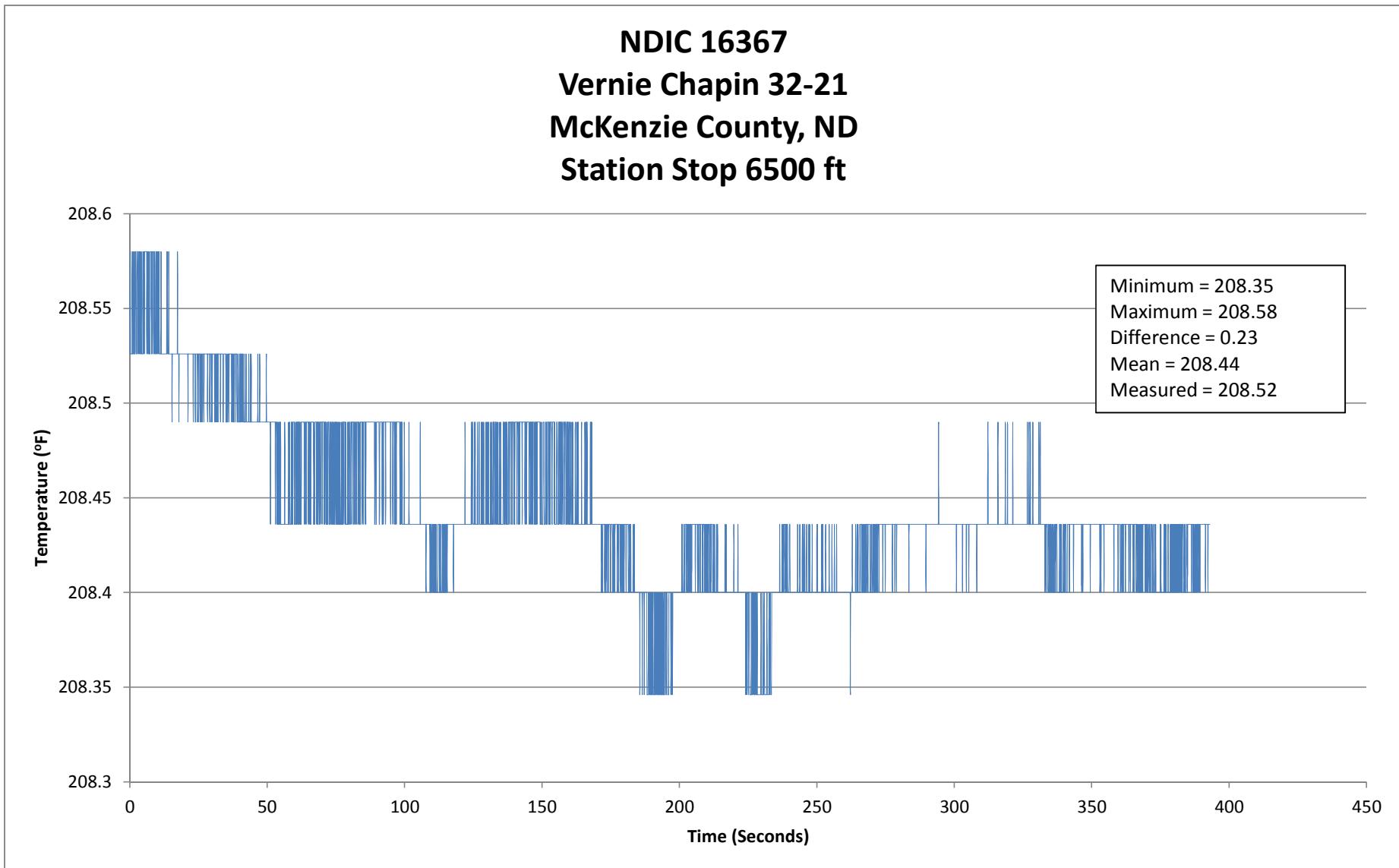
NDIC 16182
2004 JV-P NDCA-7
Williams County, ND
Station Stop at 5000 ft



NDIC 16182
2004 JV-P NDCA-7
Williams County, ND
Station Stop at 9500 ft

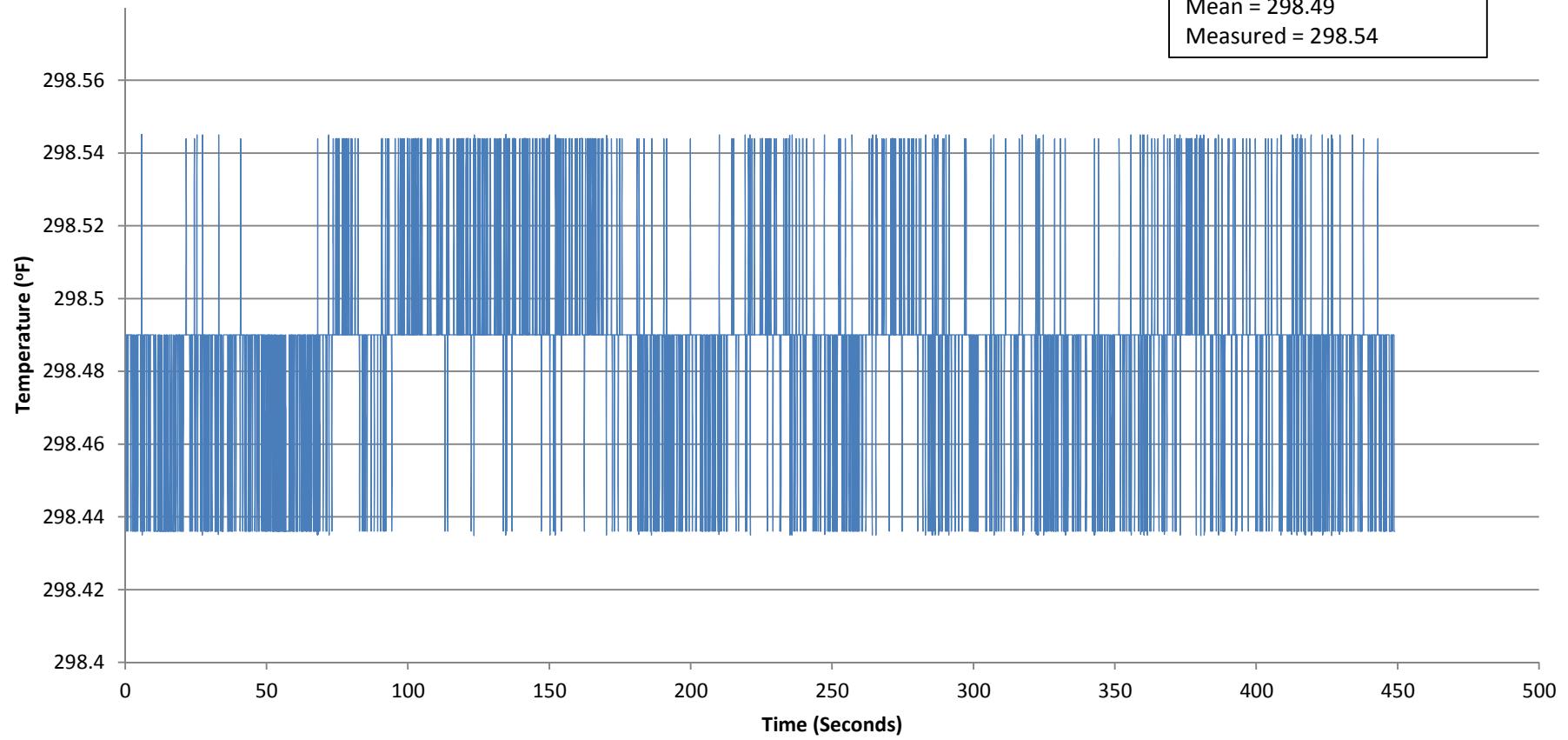


NDIC 16367
Vernie Chapin 32-21
McKenzie County, ND
Station Stop 6500 ft



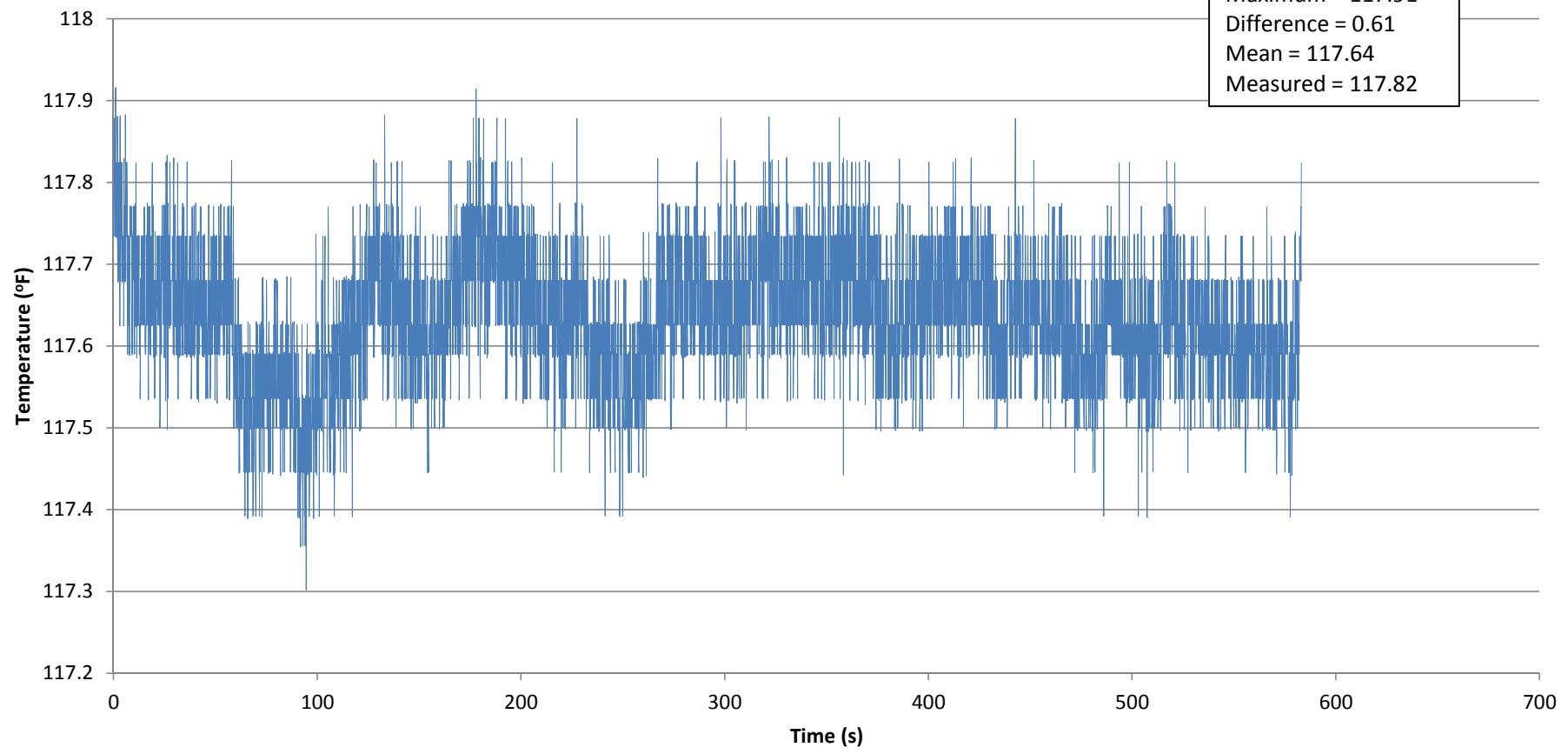
NDIC 16376
Vernie Chapin 32-21
McKenzie County, ND
Station Stop 13,000 ft

Minimum = 298.44
Maximum = 298.54
Difference = 0.11
Mean = 298.49
Measured = 298.54

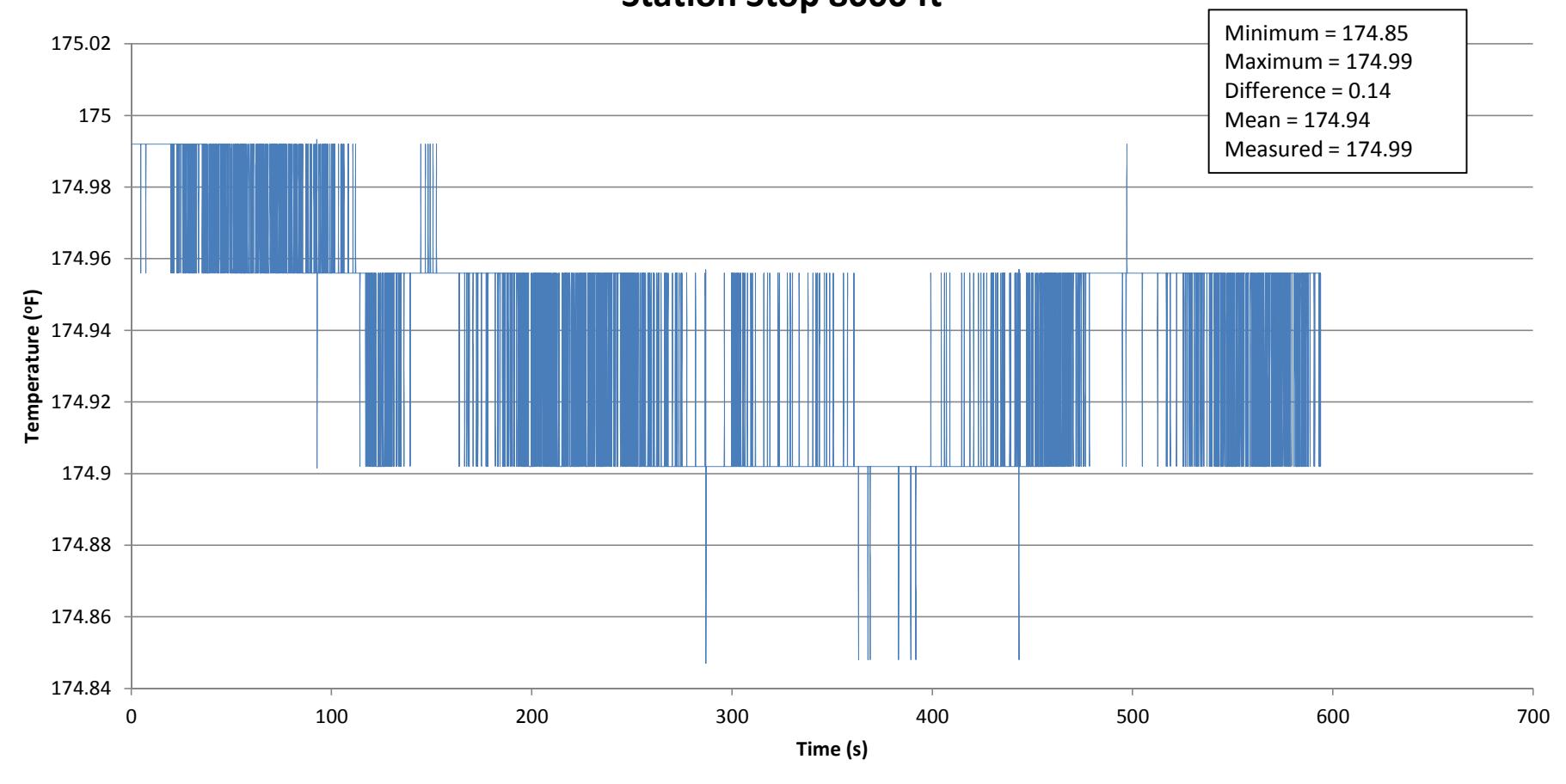


NDIC 17014
Edwards 1-33BH
Mountrail County, ND
Station Stop 4000 ft

Minimum = 117.30
Maximum = 117.91
Difference = 0.61
Mean = 117.64
Measured = 117.82

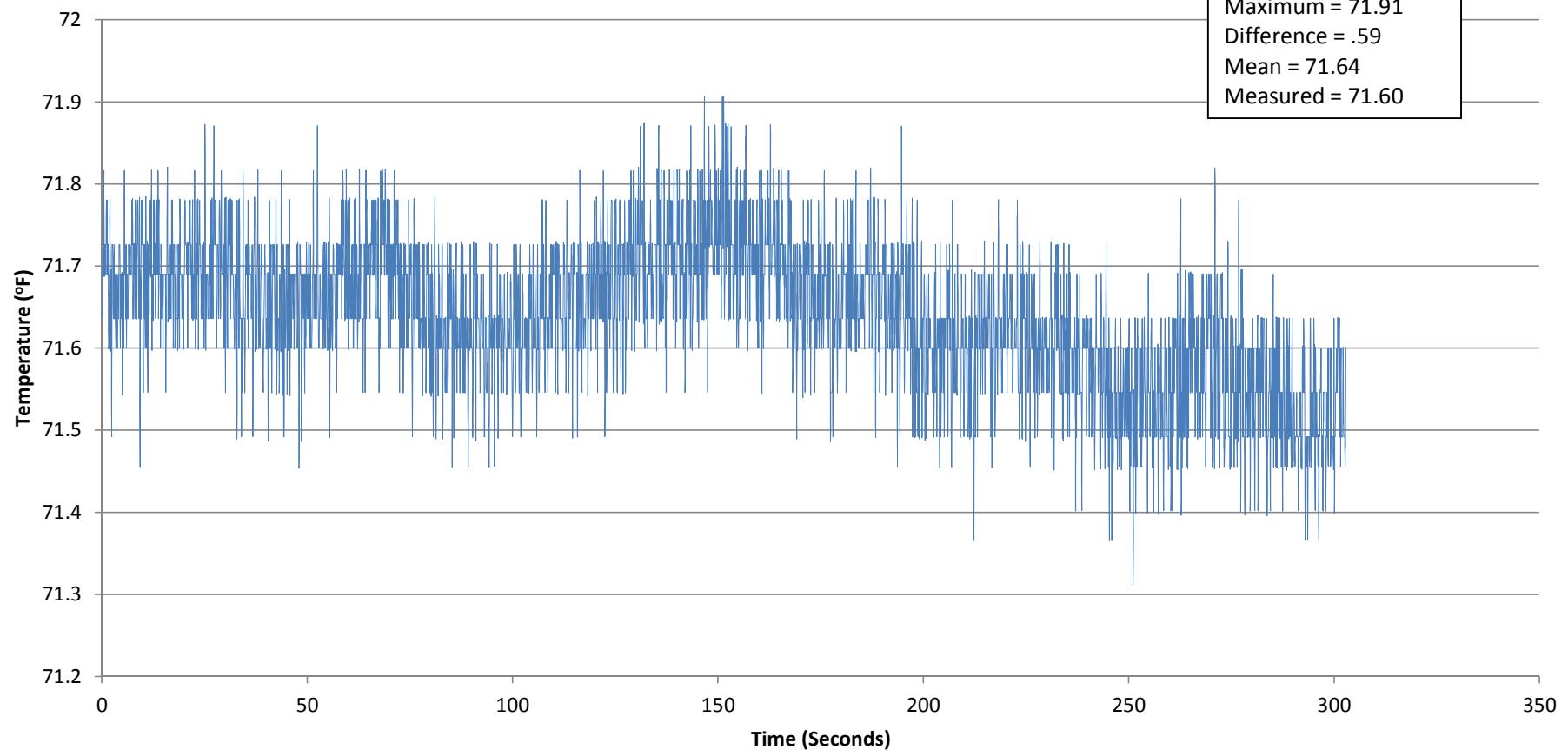


NDIC 17014
Edwards 1-33BH
Mountrail County, ND
Station Stop 8000 ft

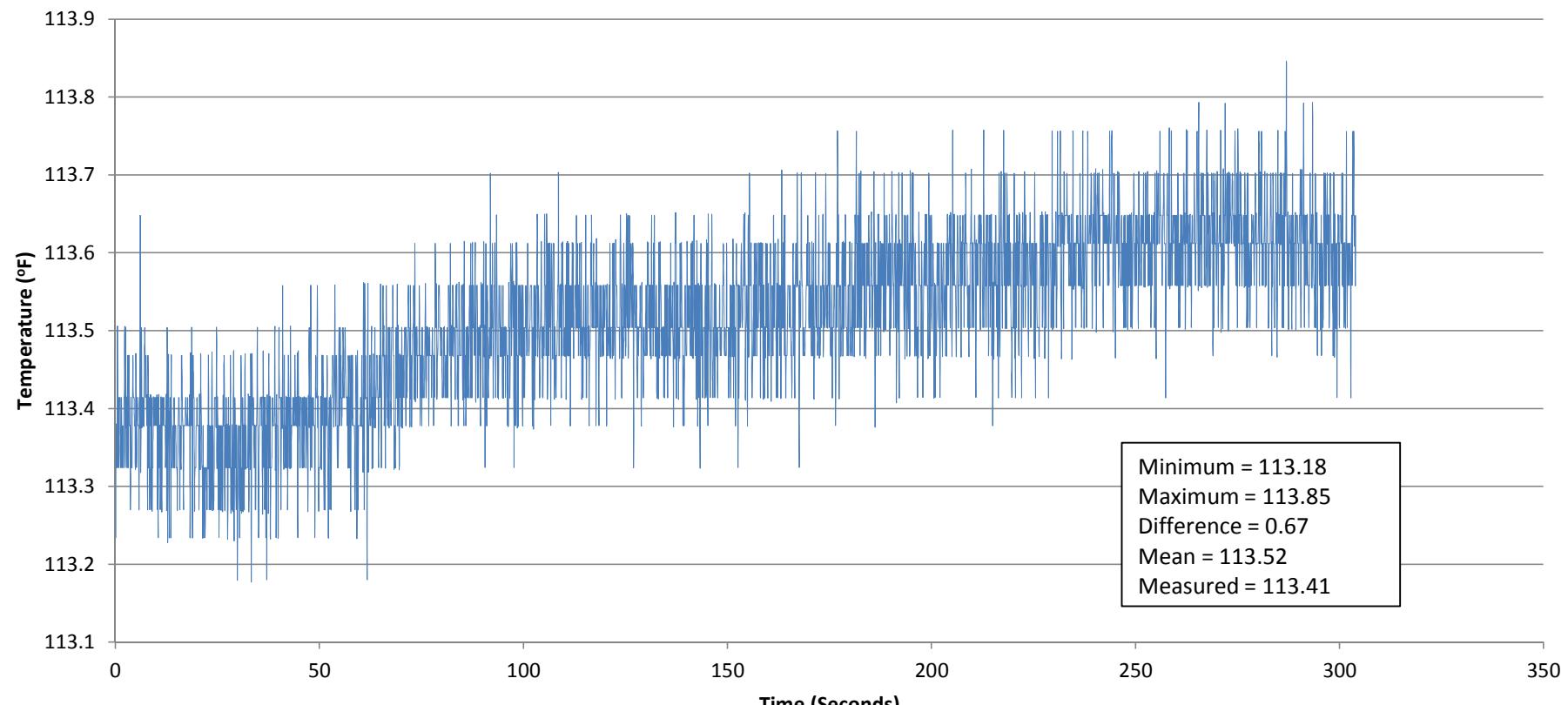


NDIC 17043
St. Andes 151-89-2413H-1
Mountrail County, ND
Station Stop at 2000 ft

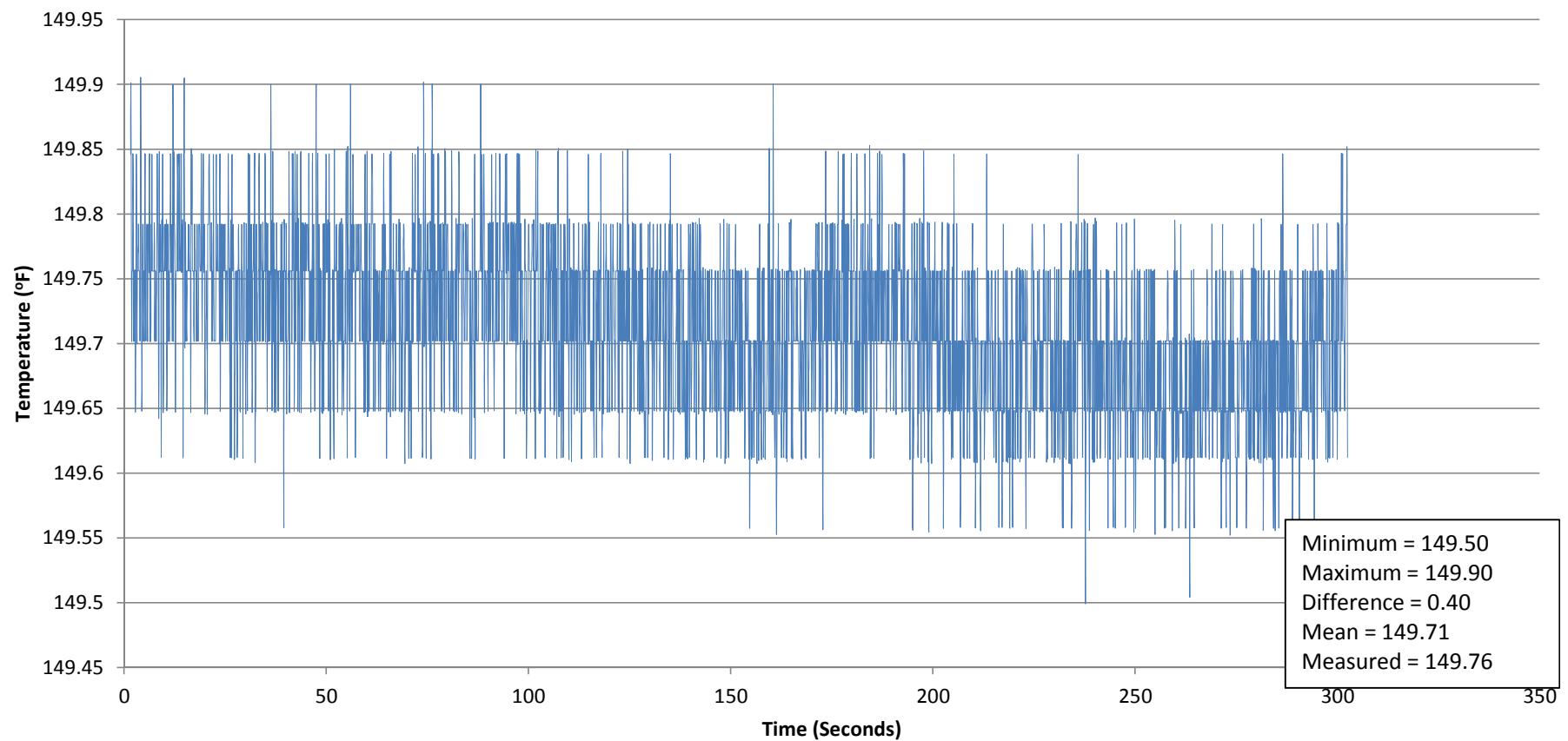
Minimum = 71.31
Maximum = 71.91
Difference = .59
Mean = 71.64
Measured = 71.60



NDIC 17043
St. Andes 151-89-2414H-1
Mountrail County, ND
Sation Stop at 4000 ft

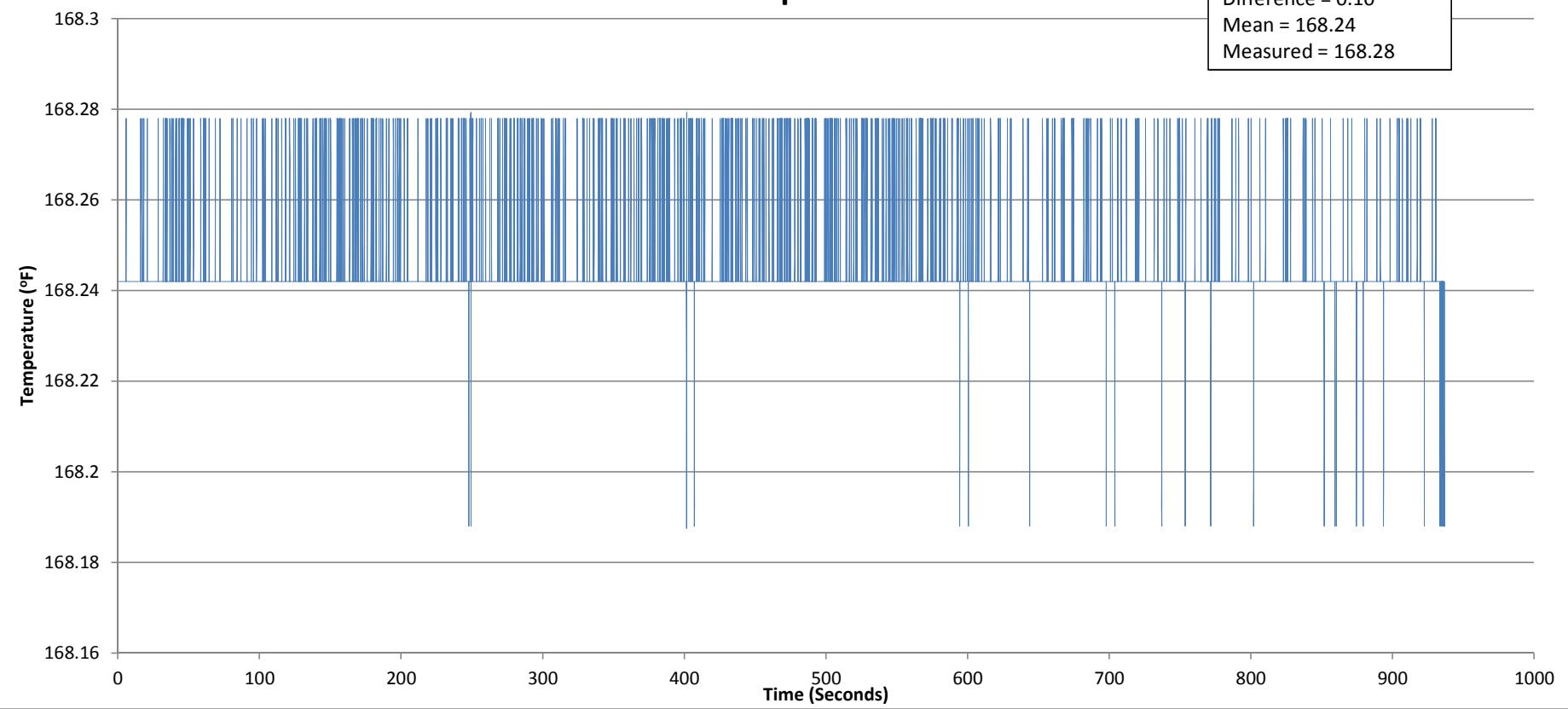


NDIC 17043
St. Andes 151-89-2413H-1
Mountrail County, ND
Station Stope at 6000 ft

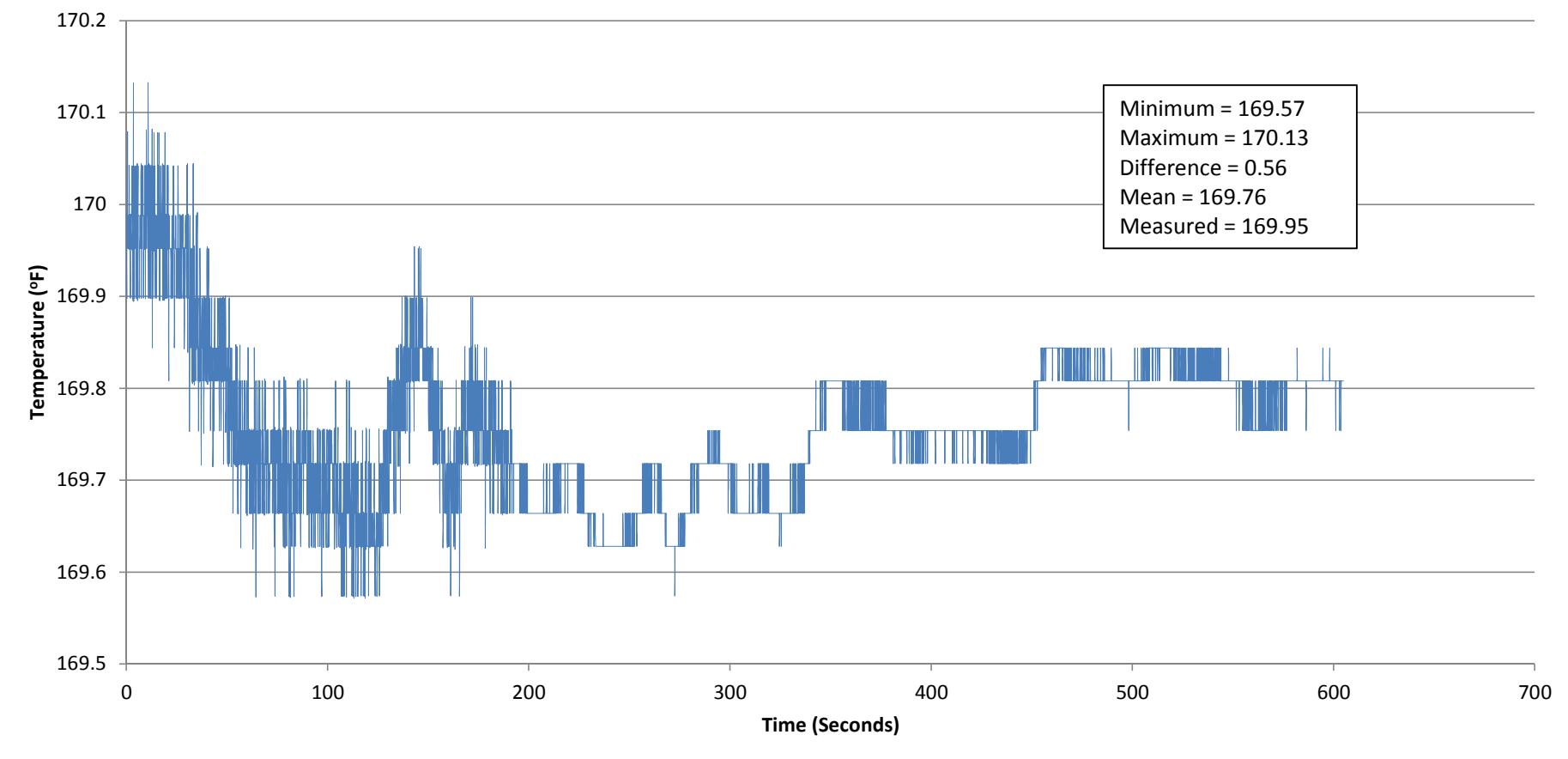


NDIC 17043
St. Andes 151-89-2413H-1
Mountrail County, ND
Station Stop at 8000 ft

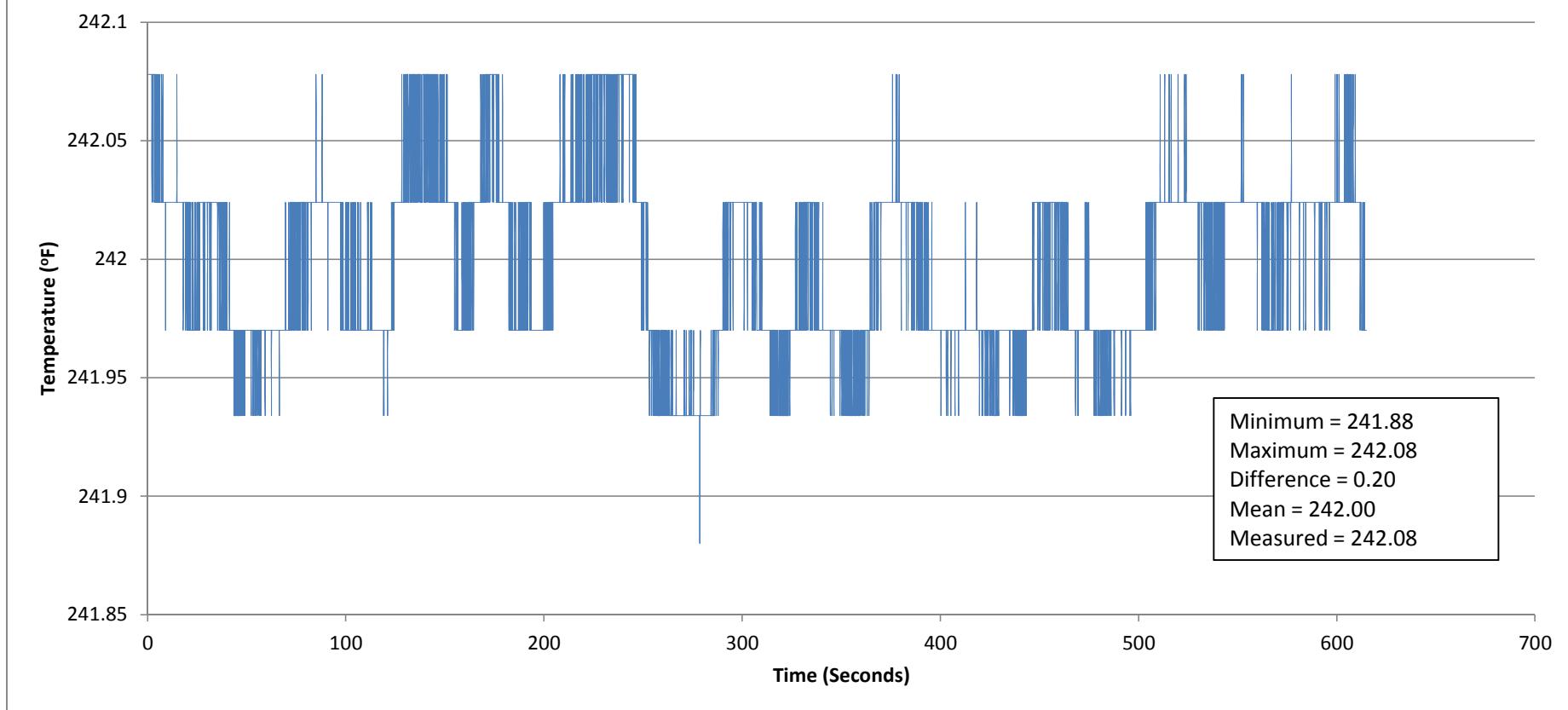
Minimum = 168.19
Maximum = 168.28
Difference = 0.10
Mean = 168.24
Measured = 168.28



NDIC 17230
Roosevelt Federal 2-4h
Billings County, ND
Station Stop 5000 ft

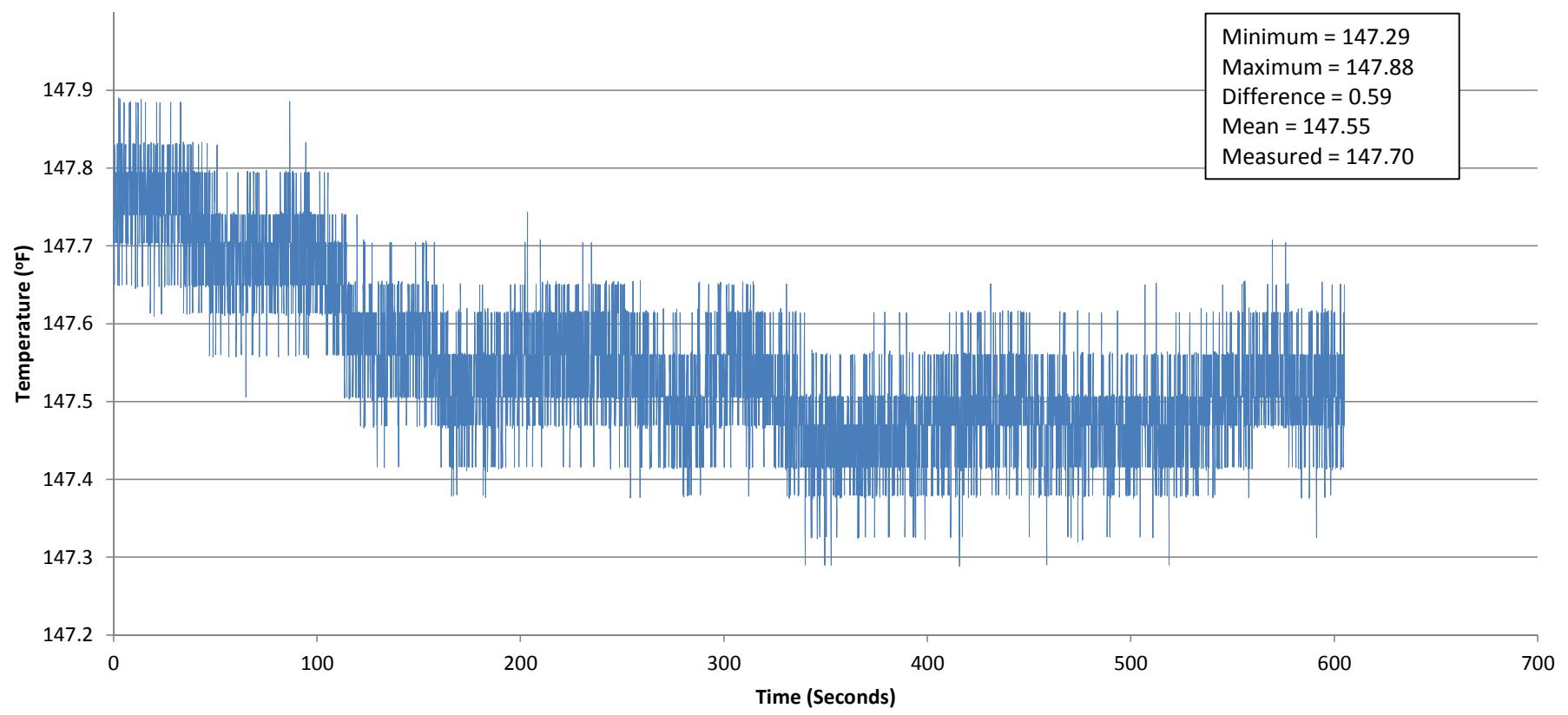


NDIC 17230
Roosevelt Federal 2-4H
Billings County, ND
Station Stop at 10,000 ft

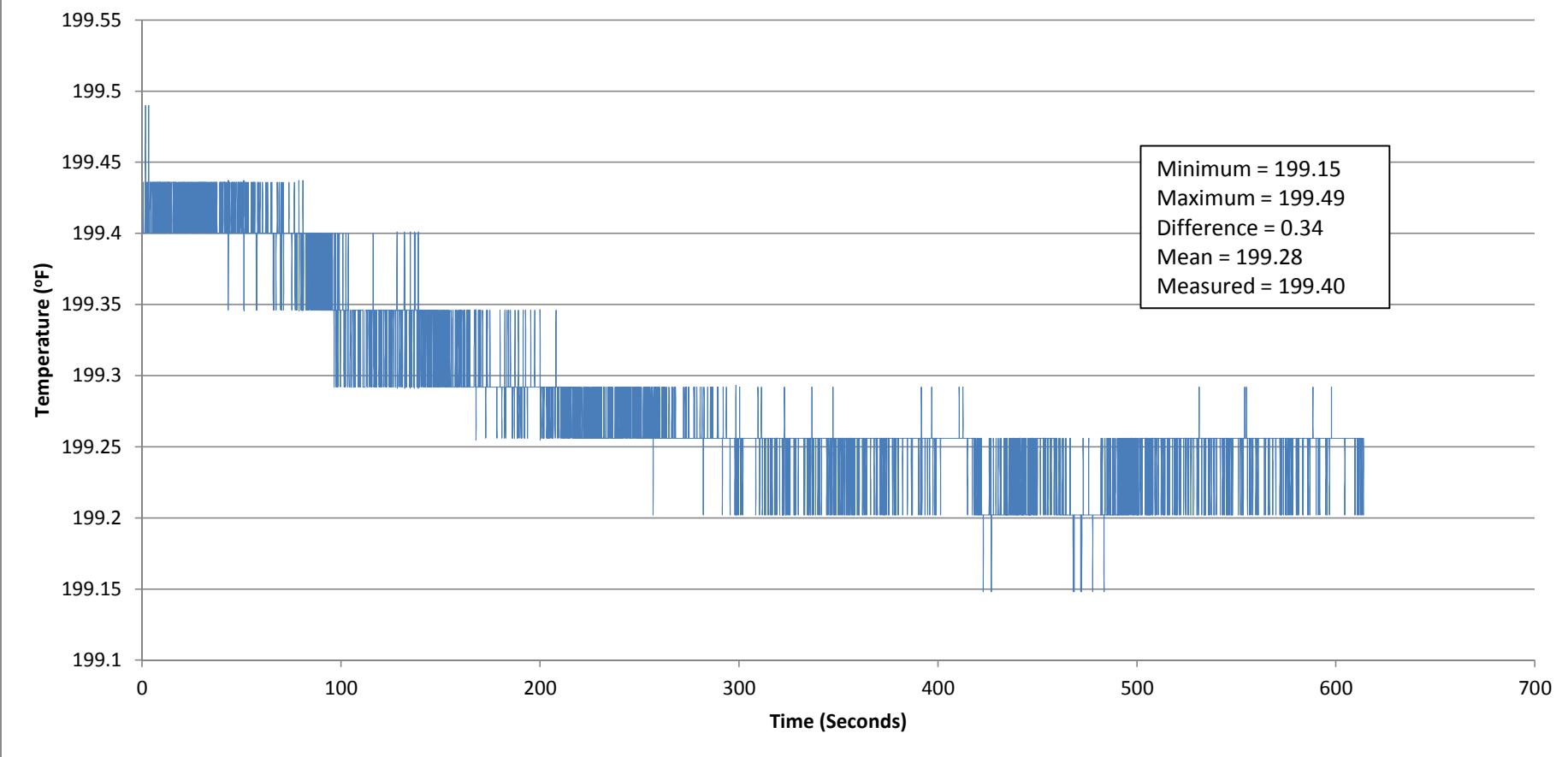


NDIC 17317
E-M Emmel 10-3
Renville County, ND
Station Stop at 4400 ft

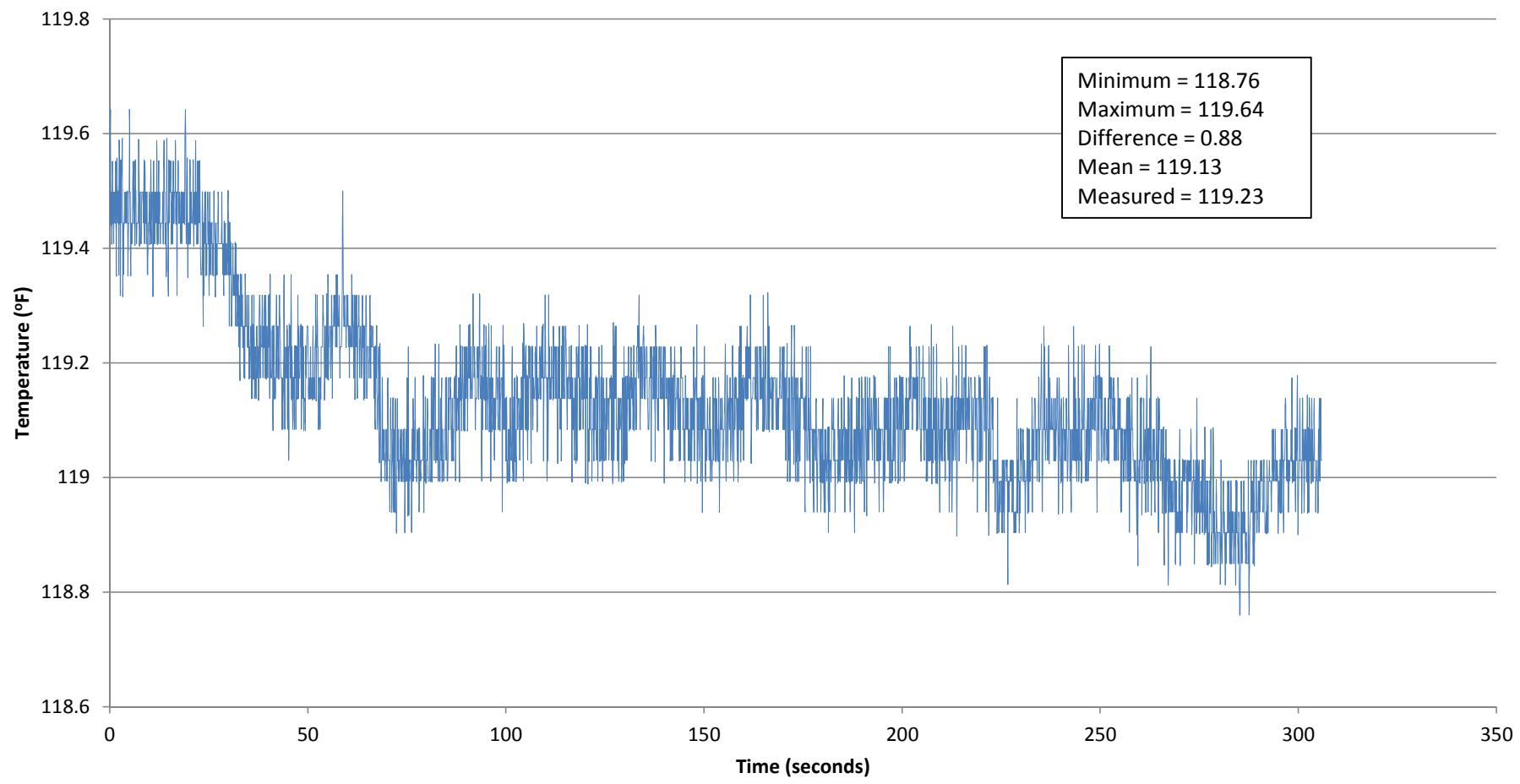
Minimum = 147.29
Maximum = 147.88
Difference = 0.59
Mean = 147.55
Measured = 147.70



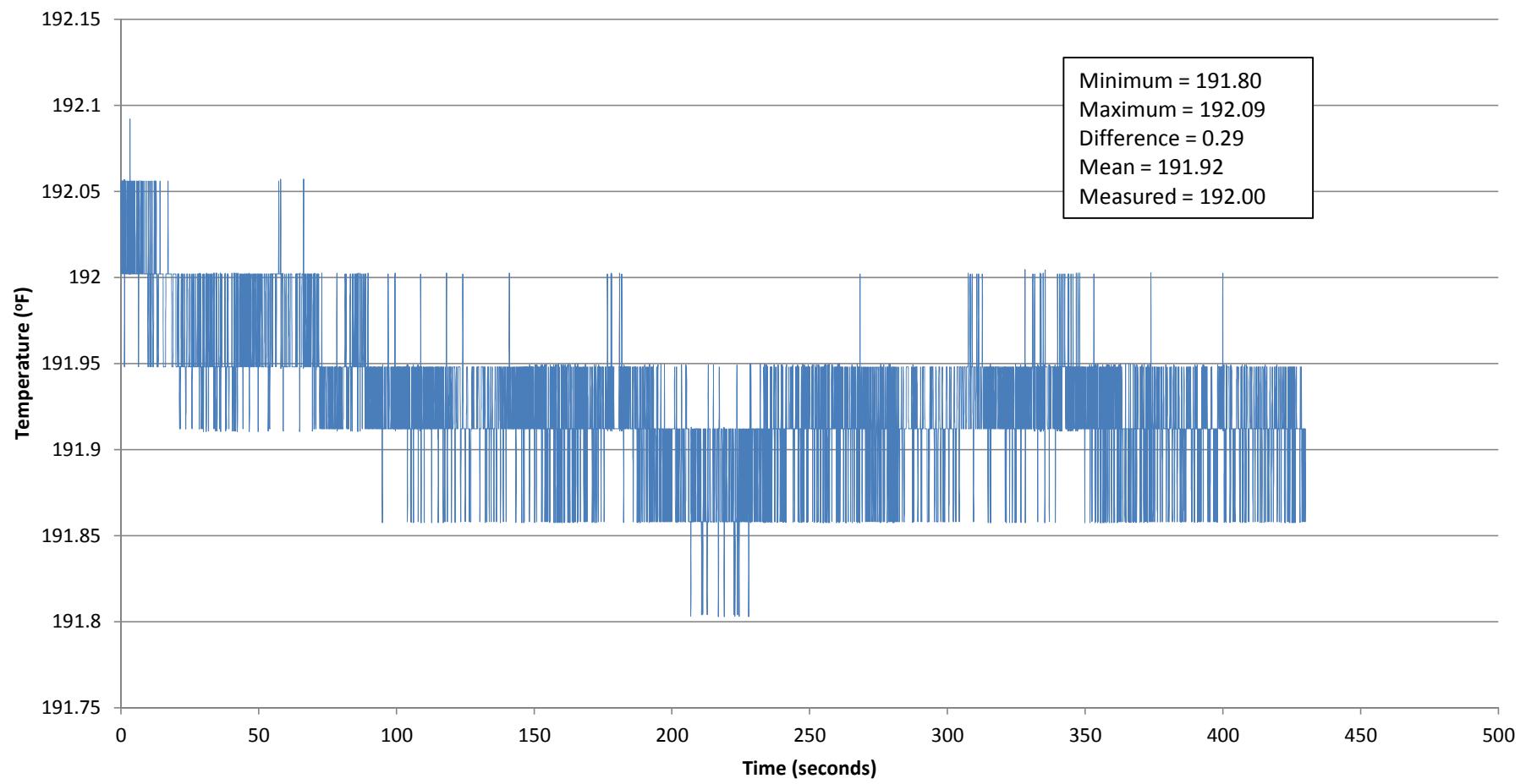
NDIC 17317
E-M Emmel 10-3
Renville County, ND
Station Stop at 8800 ft



NDIC 3090
Grenora-Madison Unit 08
Williams County, ND
Station Stop 3750 ft

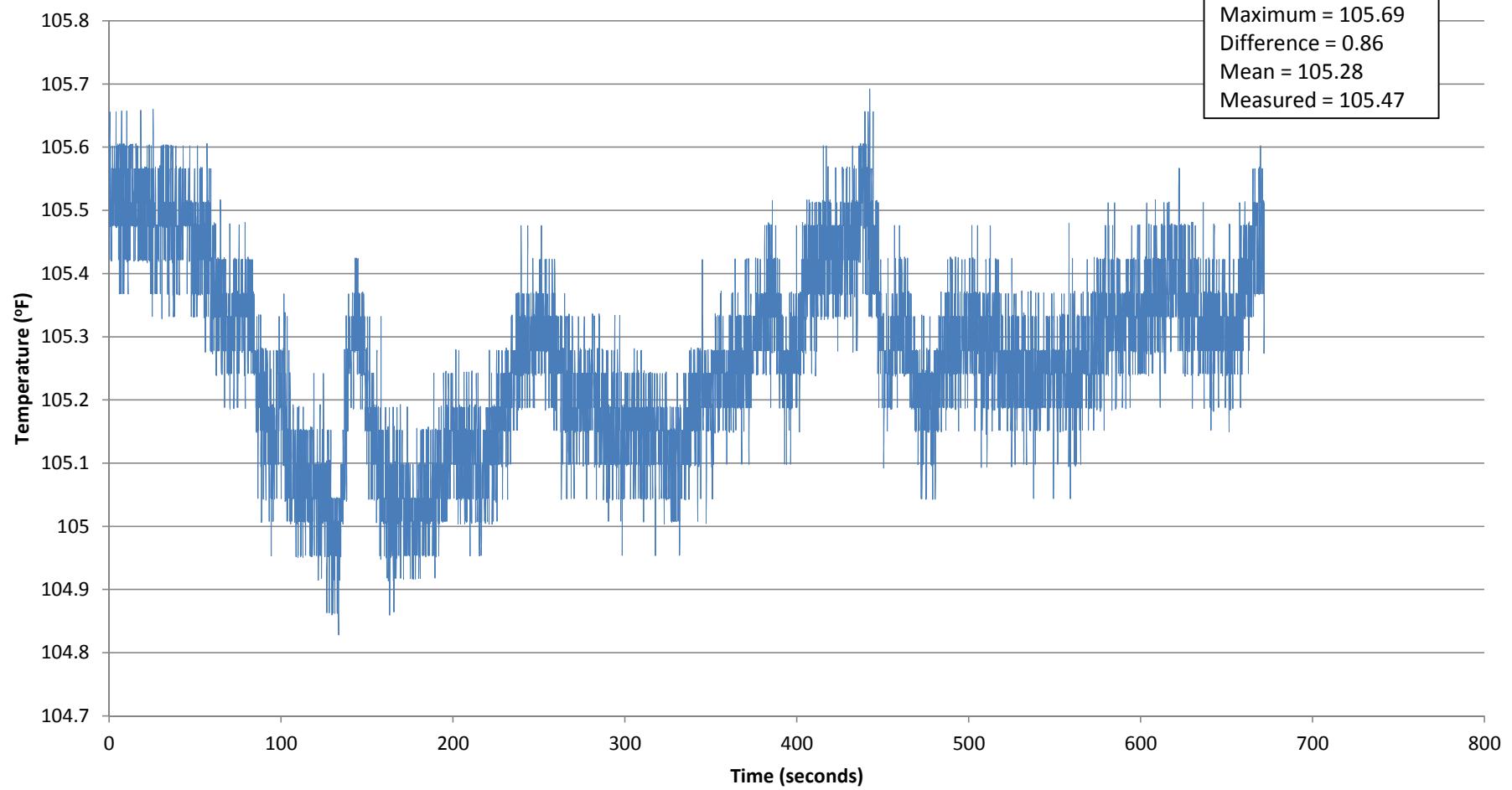


NDIC 3090
Grenora-Madison Unit 08
Williams County, ND
Station Stop 7500 ft



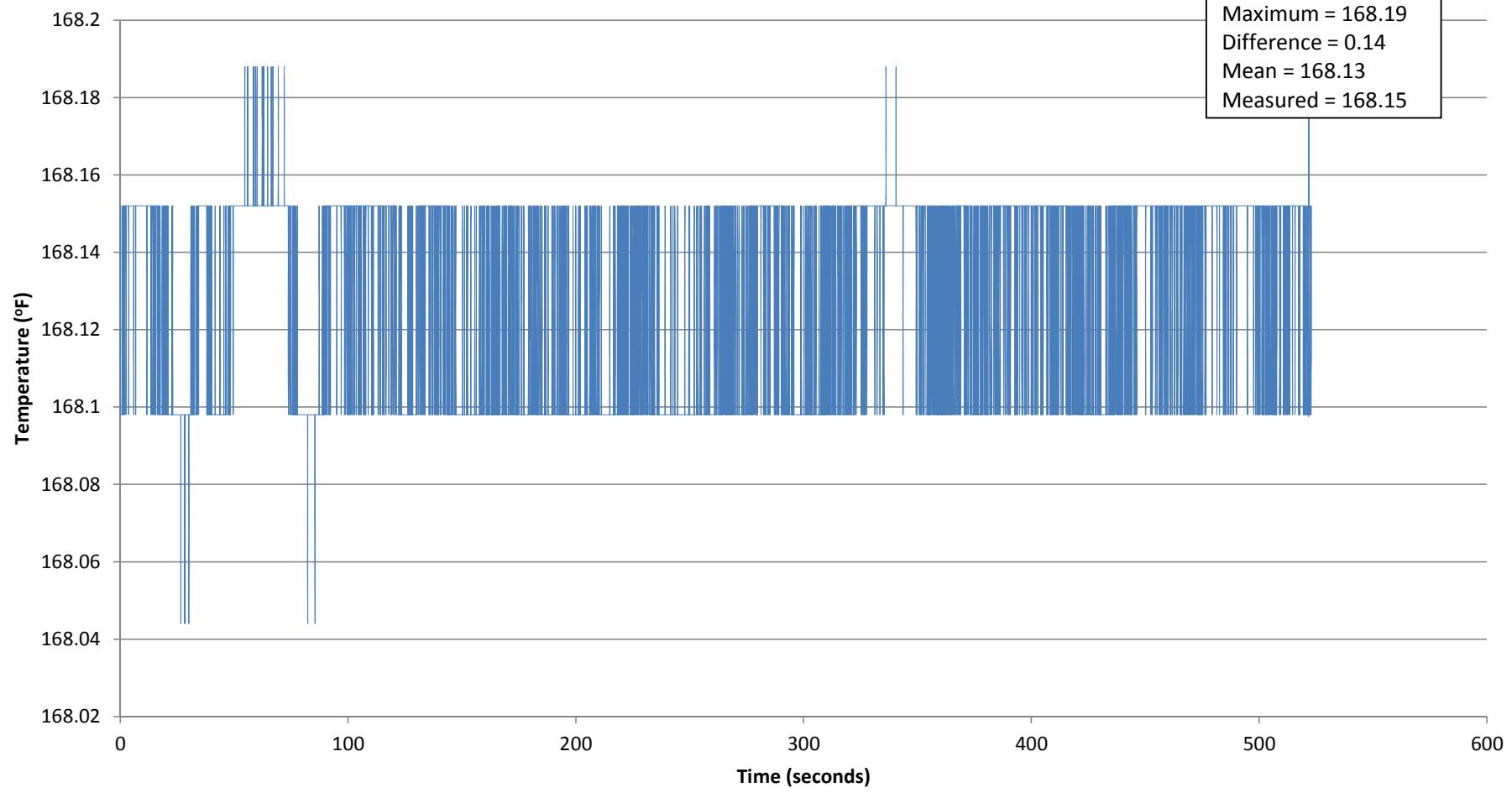
NDIC 13725
JC Woods 26H-1
Burke County, ND
Station Stop 2750 ft

Minimum = 104.83
Maximum = 105.69
Difference = 0.86
Mean = 105.28
Measured = 105.47



NDIC 13725
JC Woods 26H-1
Burke County, ND
Station Stop 5450 ft

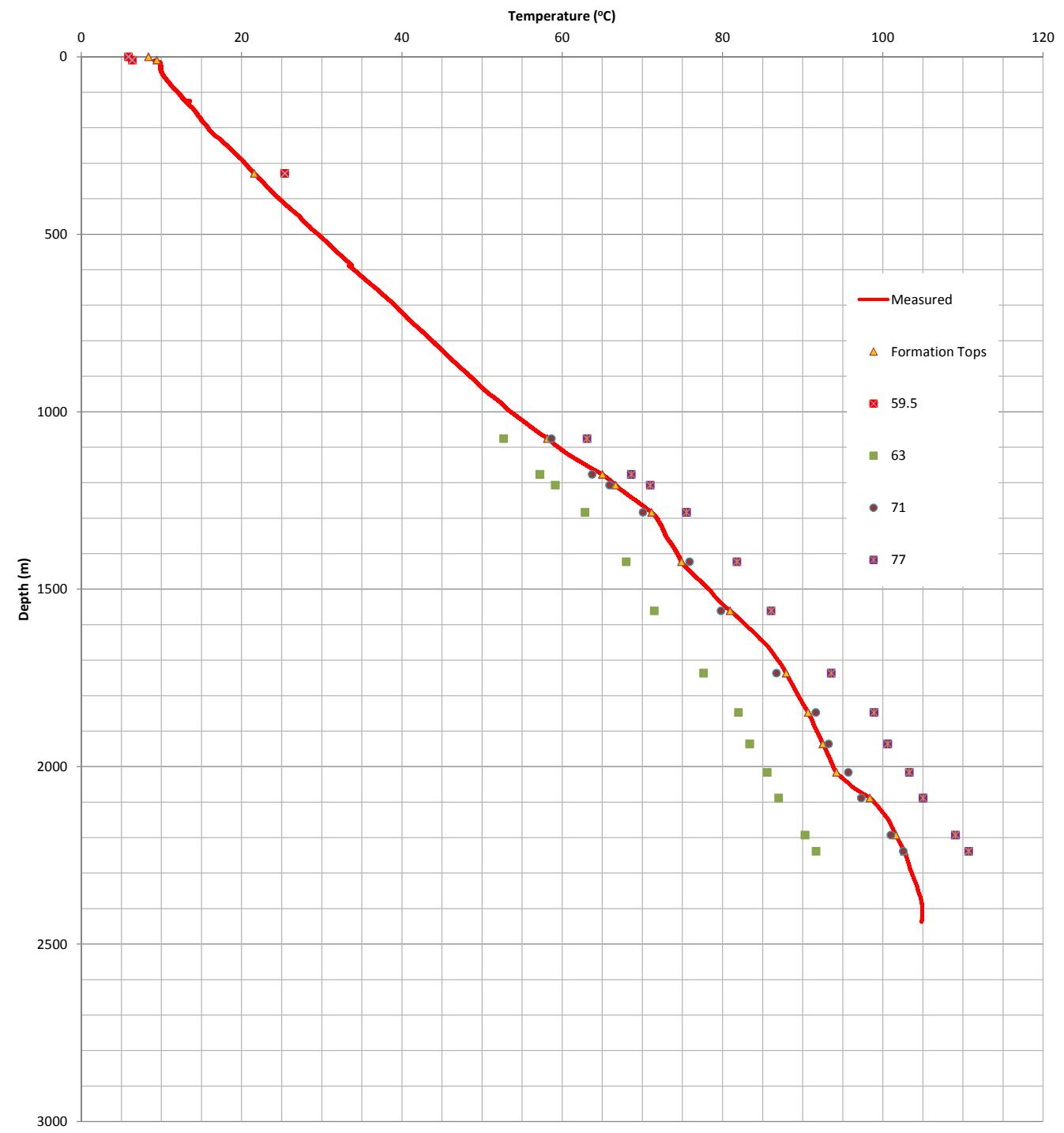
Minimum = 168.04
Maximum = 168.19
Difference = 0.14
Mean = 168.13
Measured = 168.15



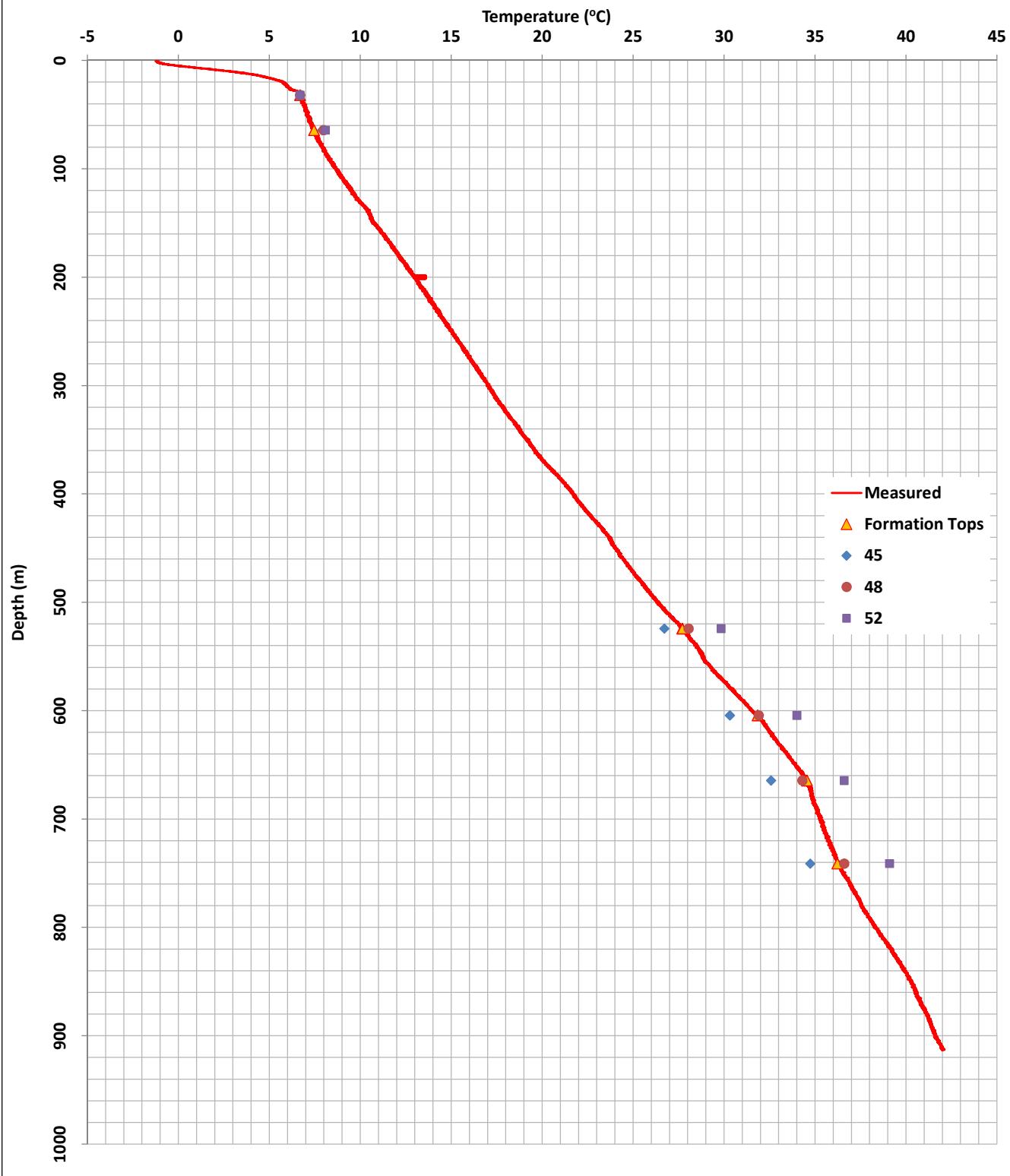
APPENDIX C

TEMPERATURE PROFILES AND MODELED HEAT FLOW

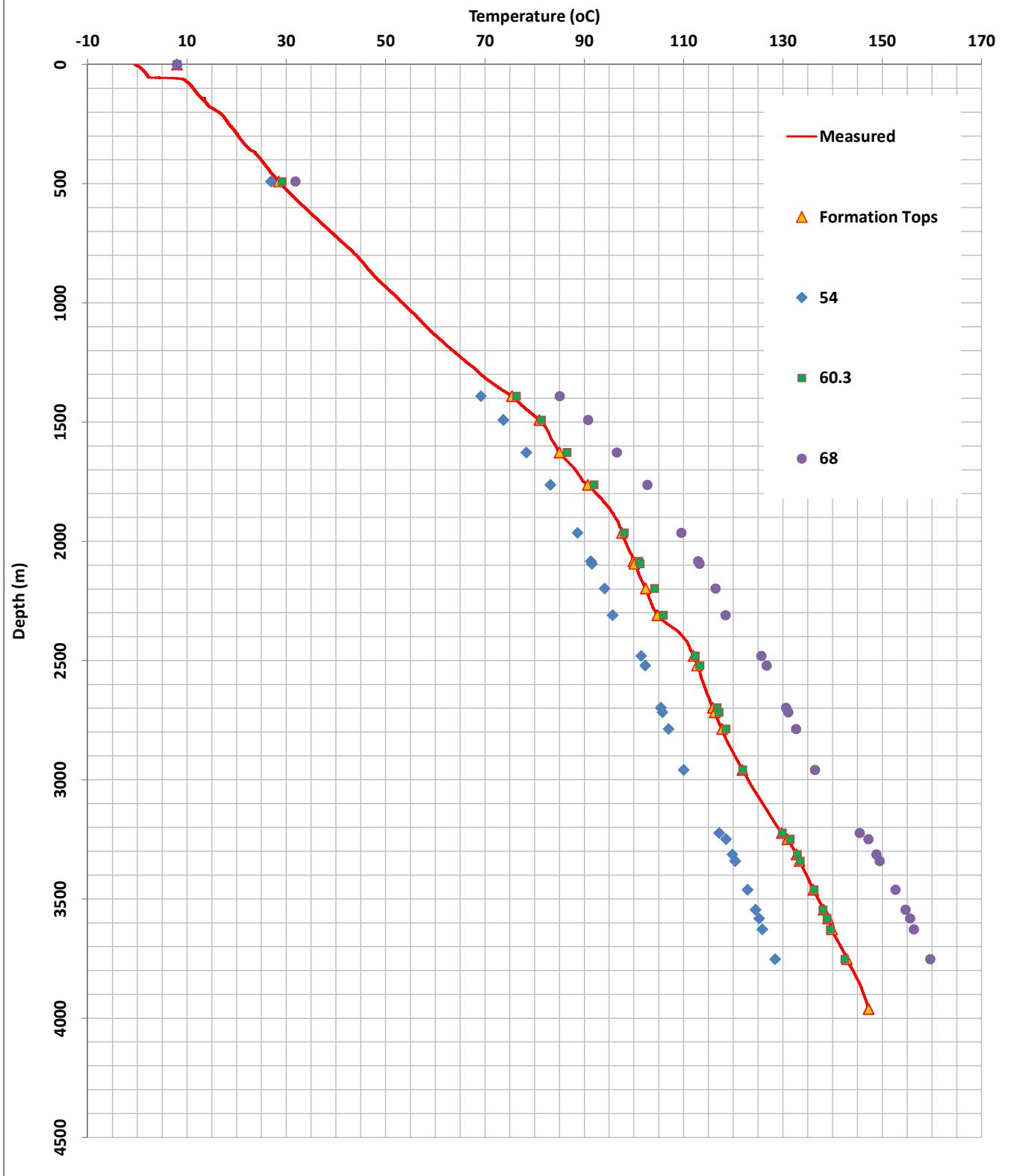
Temperature Profile and Modeled Heat Flow
NDIC 1140 - Capa Madison Unit H-205
Williams County, ND



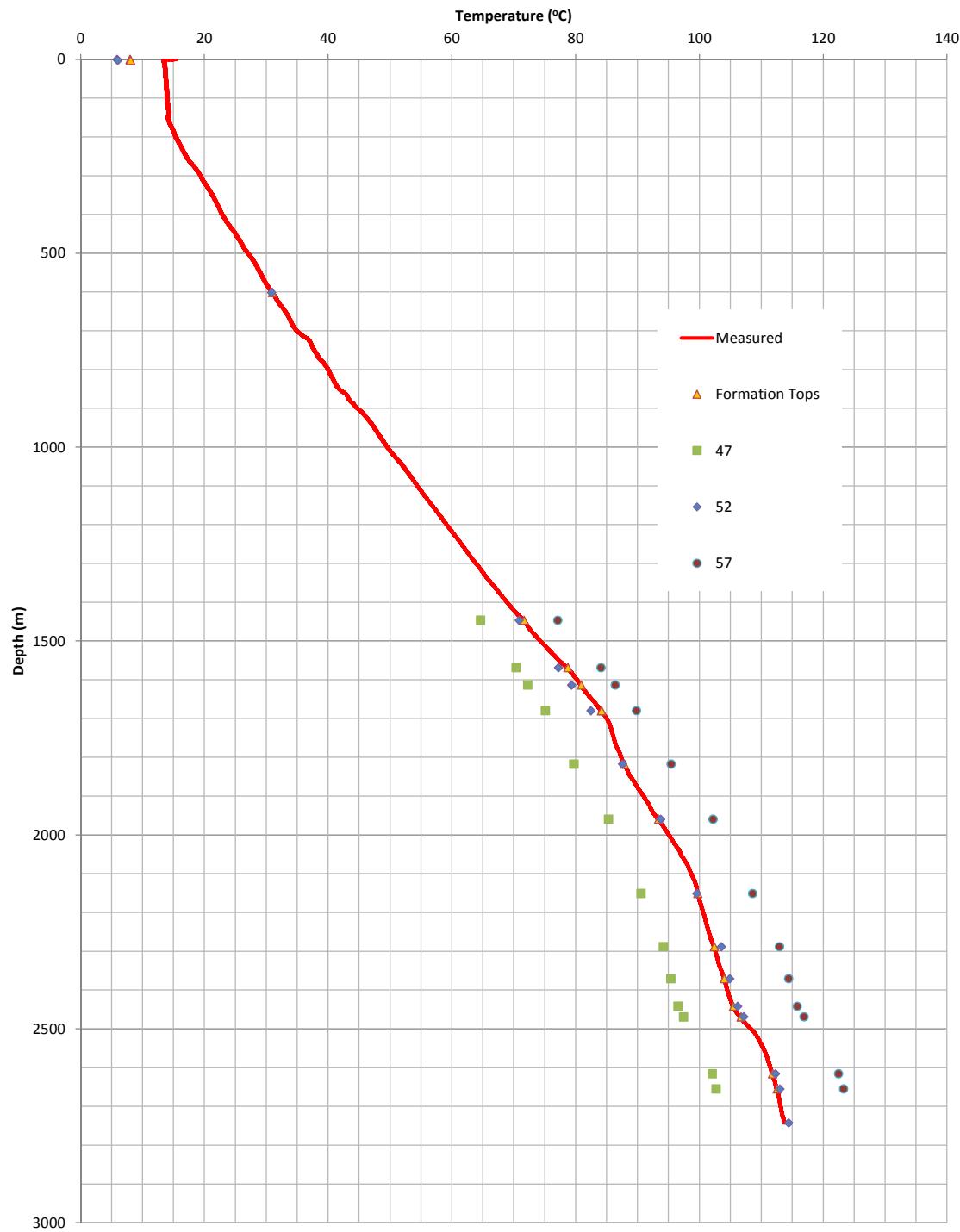
Temperature Profile and Model Heat Flow
NDIC 2139 NSCU V-706
Bottineau County, ND



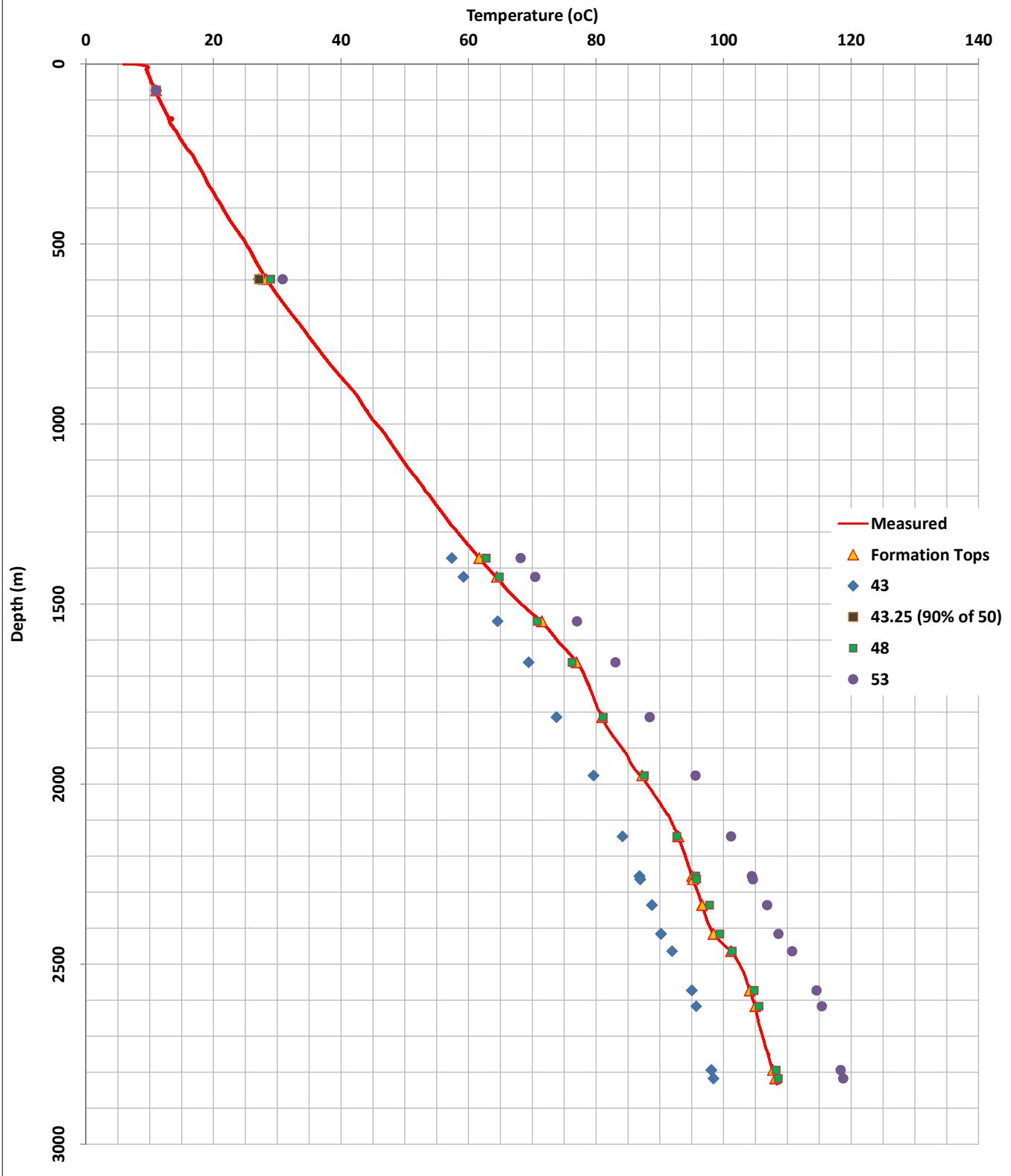
Temperature Profile and Modeled Heat Flow
NDIC 8005 - Sivertson 29-23R1
McKenzie County, ND



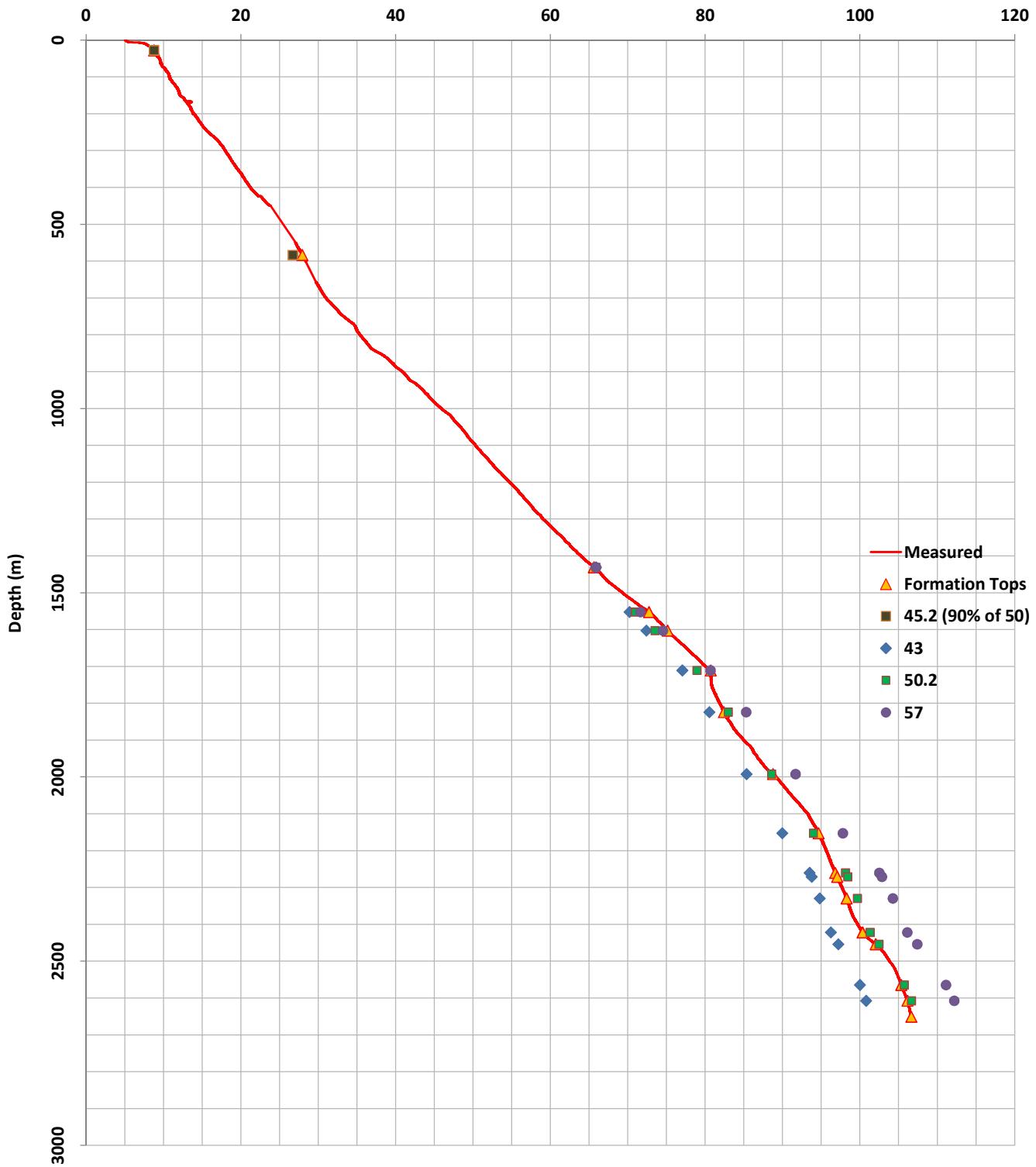
Temperature Profile and Modeled Heat Flow
NDIC 8706 - Berge C-1
McKenzie County, ND



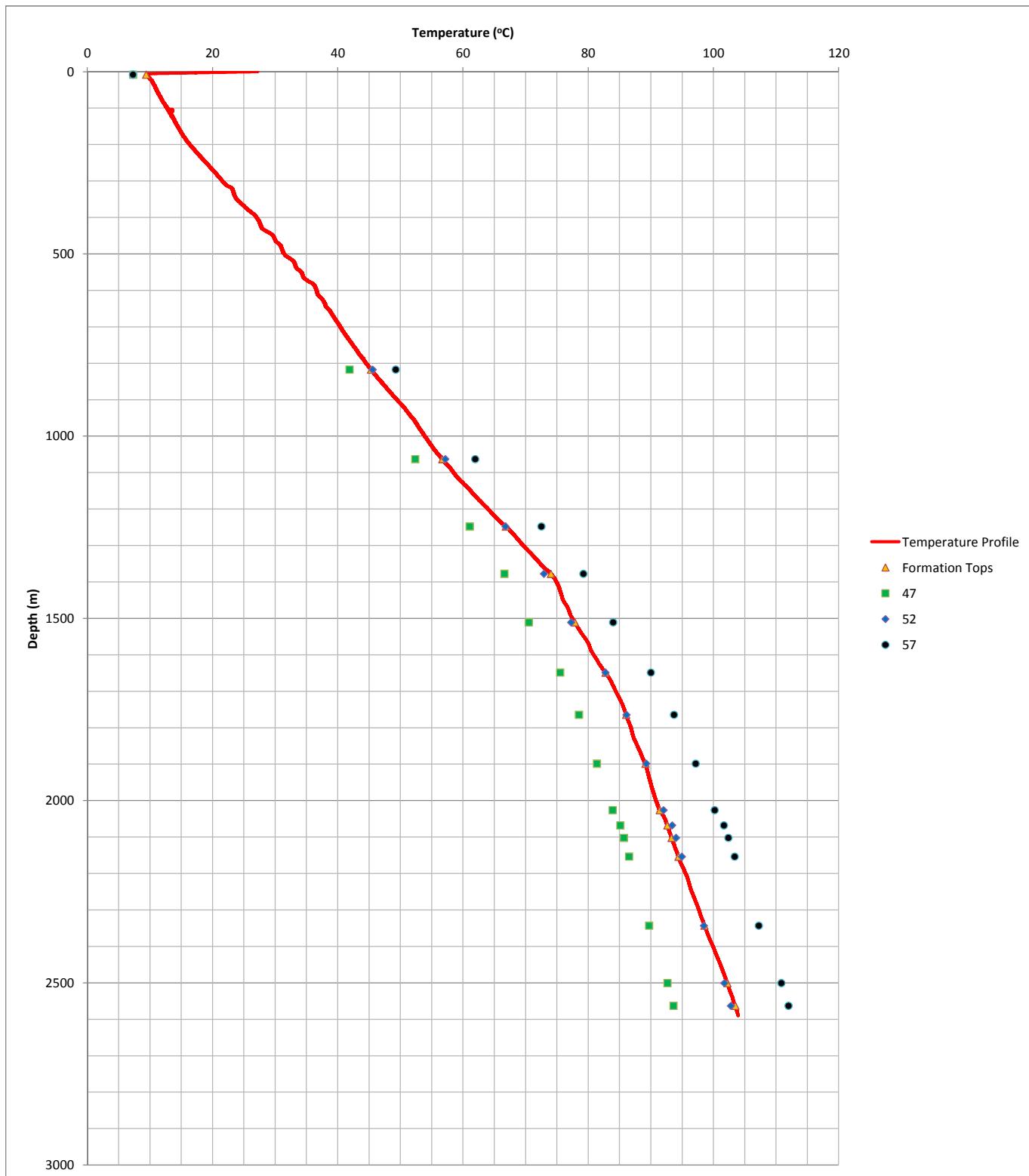
Temperature Profile and Modeled Heat Flow
NDIC 9653 - Cutlip 1
McKenzie County, ND



Temperature Profile and Modeled Heat Flow
NDIC 10103 - Iverson State A-1
McKenzie County, ND
Temperature (°C)



Temperature Profile and Modeled Heat Flow
NDIC 10278 - Mud Buttes State 1-36
Bowman County, ND



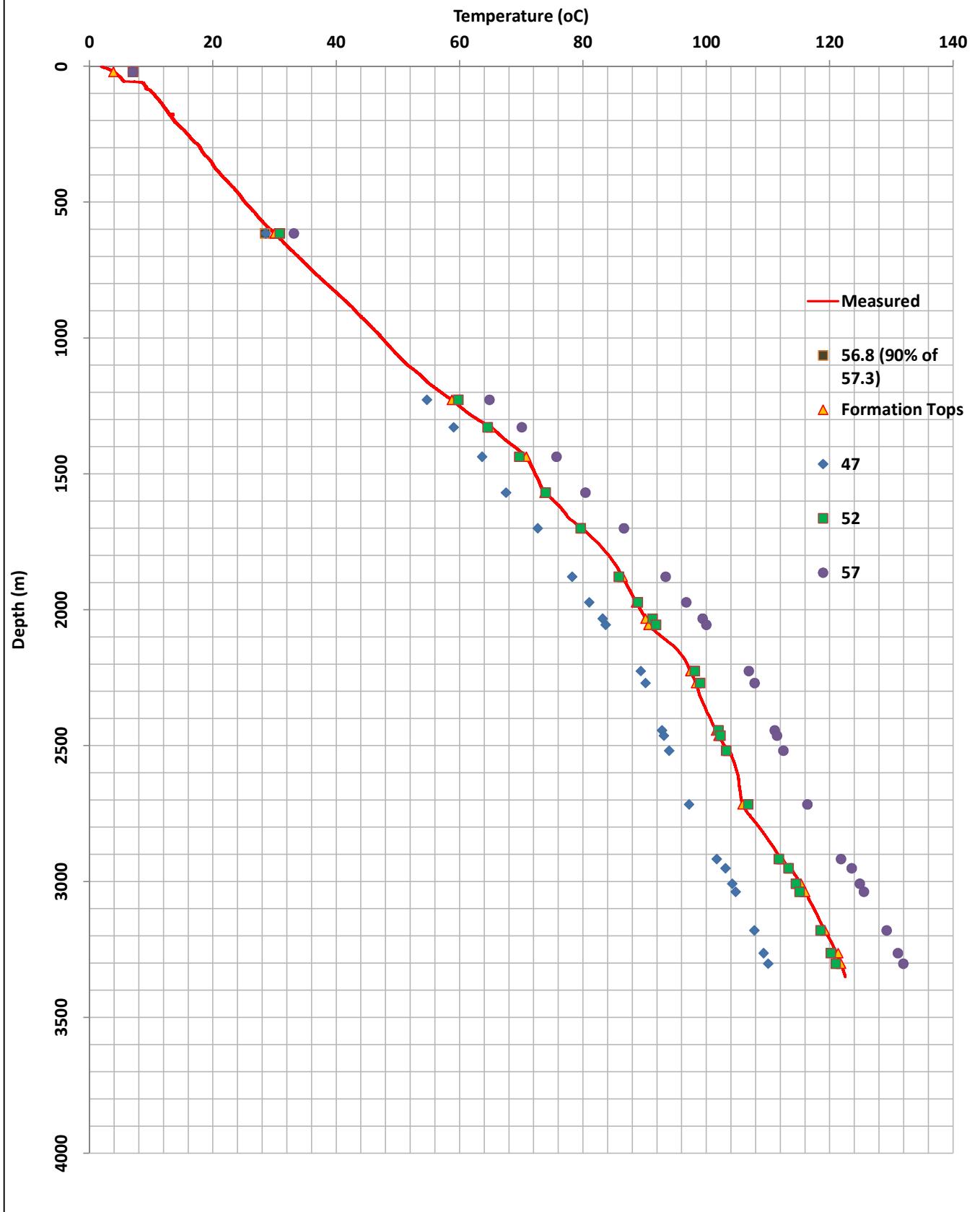
Temperature Profile and Modeled Heat Flow
NDIC 12280
Brandjord 1-20
Bottineau County, ND



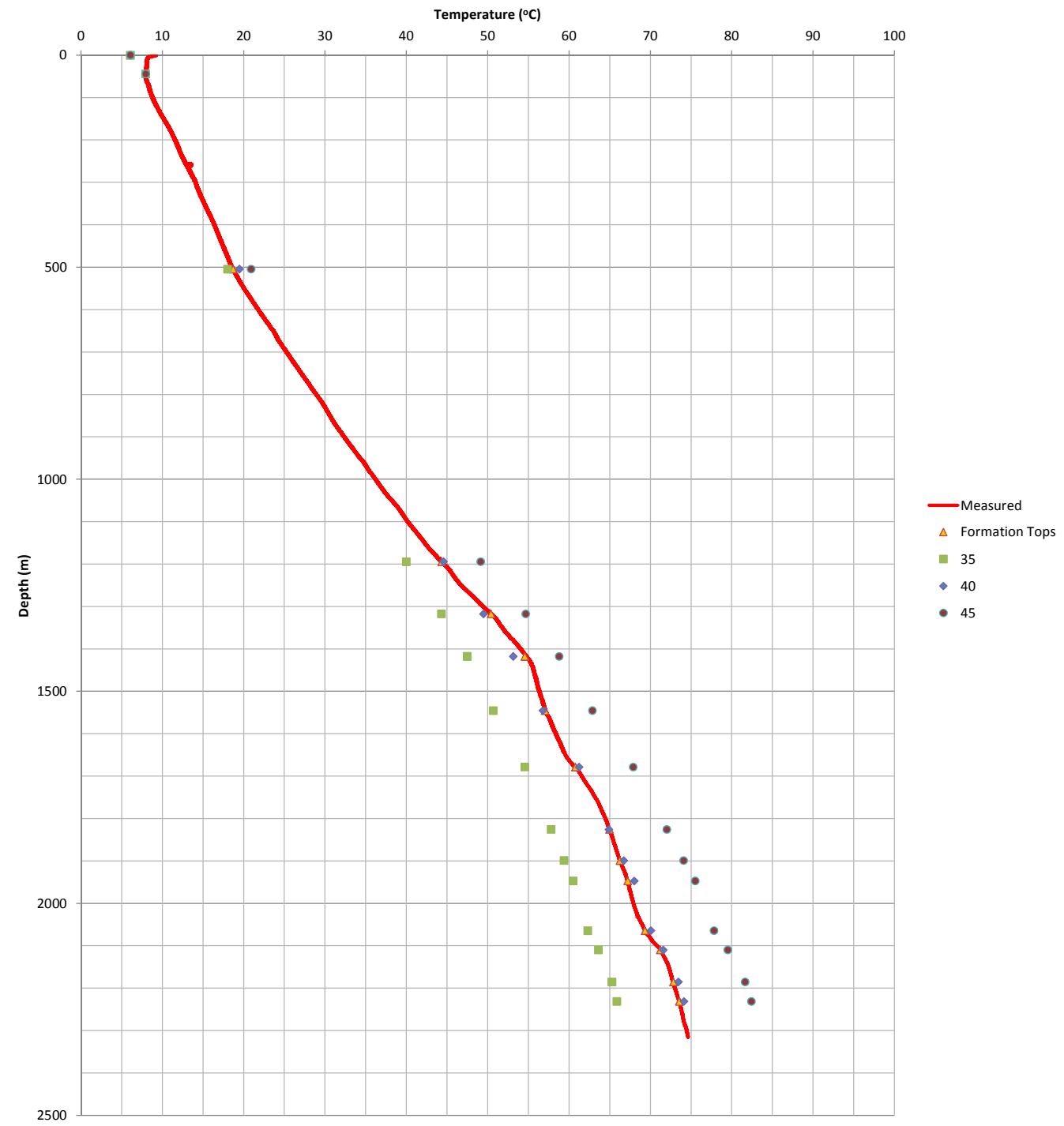
Temperature Profile and Modeled Heat Flow

NDIC 12363 - Astrid Ongstad 14-22

Williams County, ND



Temperature Profile and Modeled Heat Flow
NDIC 13132 - Frink 13-15
McClean County, ND

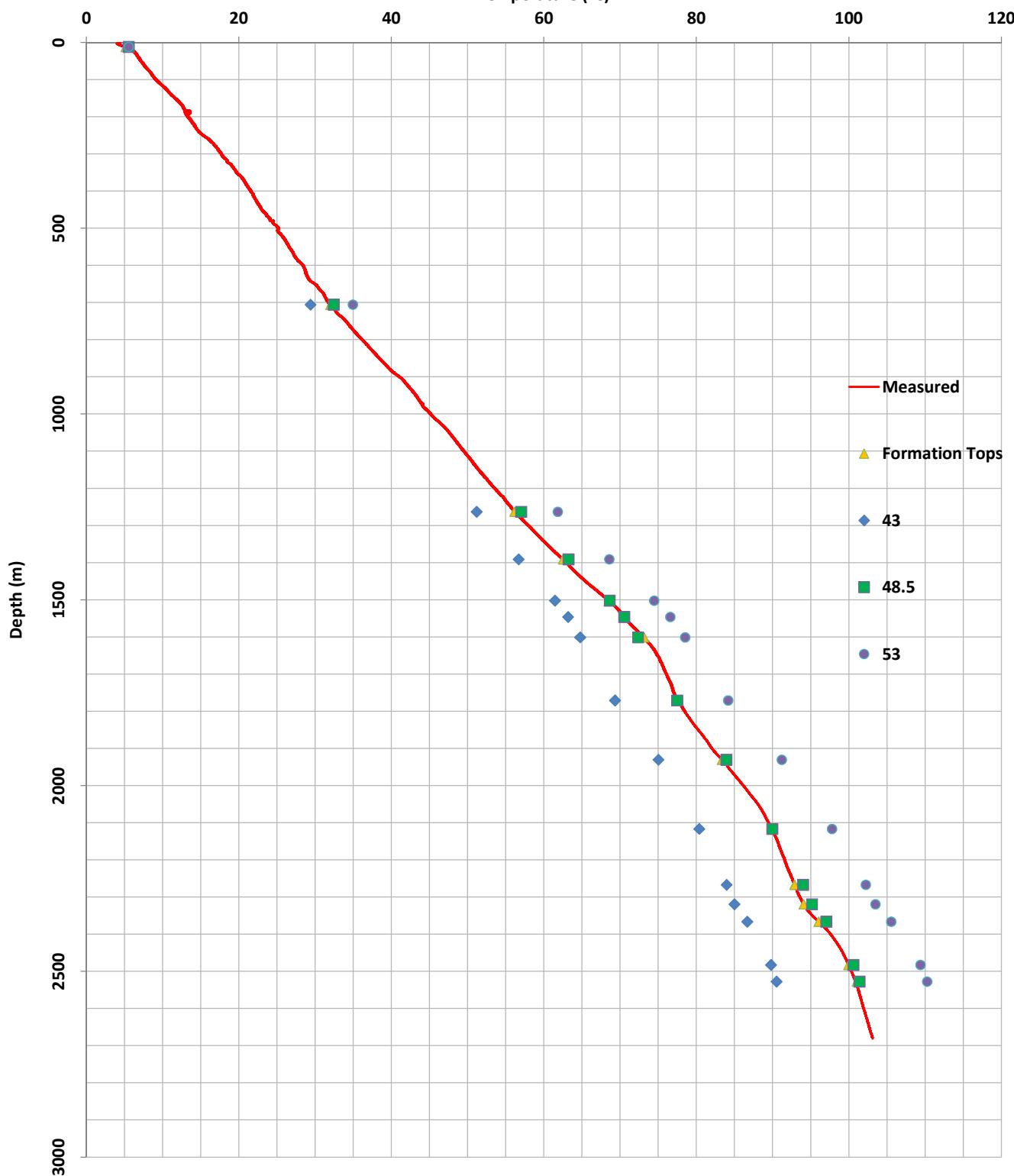


Temperature Profile and Modeled Heat Flow

NDIC 13666 - Rieder 1-9 SWD

Williams County, ND

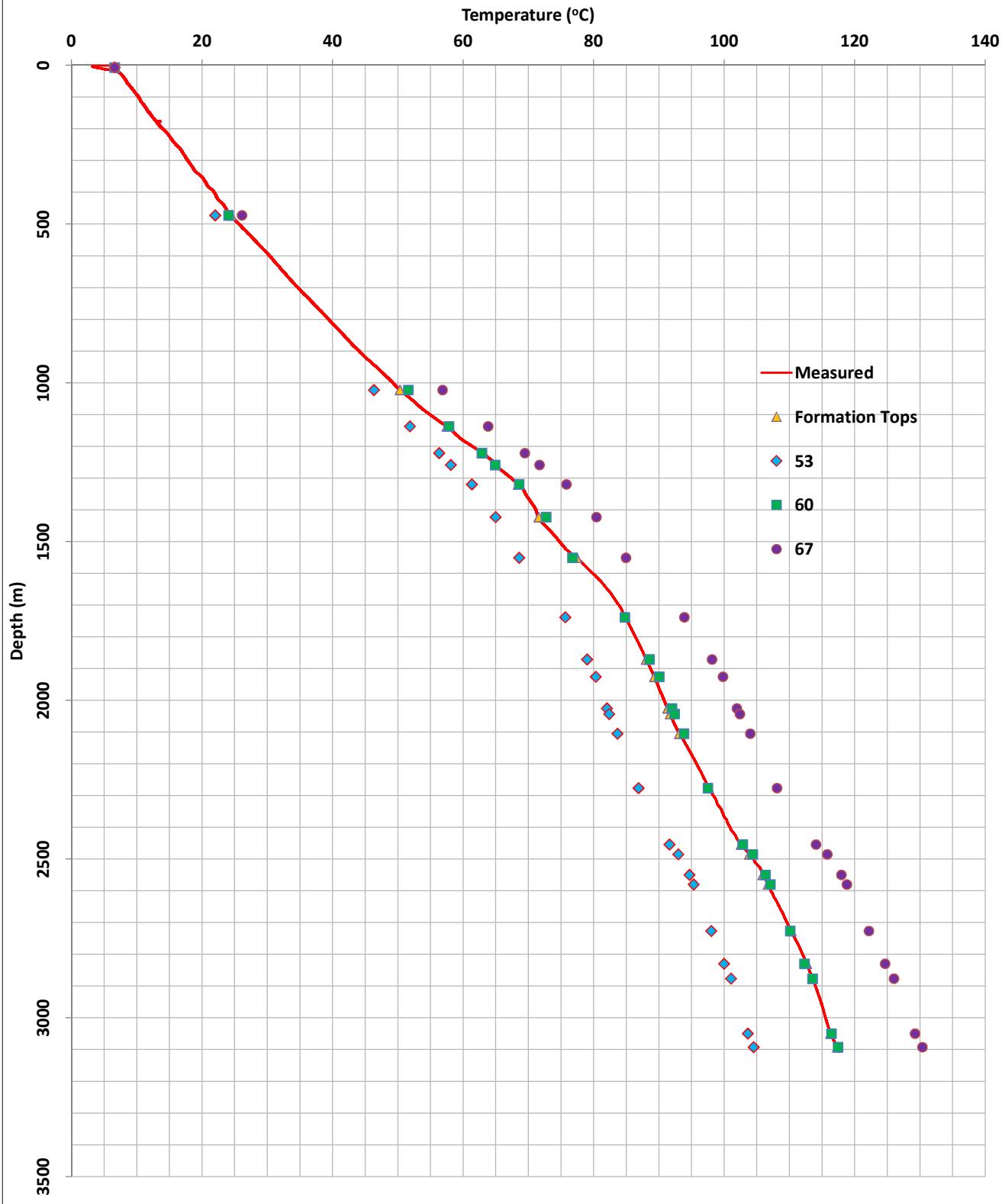
Temperature ($^{\circ}\text{C}$)



Temperature Profile and Modeled Heat Flow

NDIC # 15137 - Holte 6-21

Burke County, ND

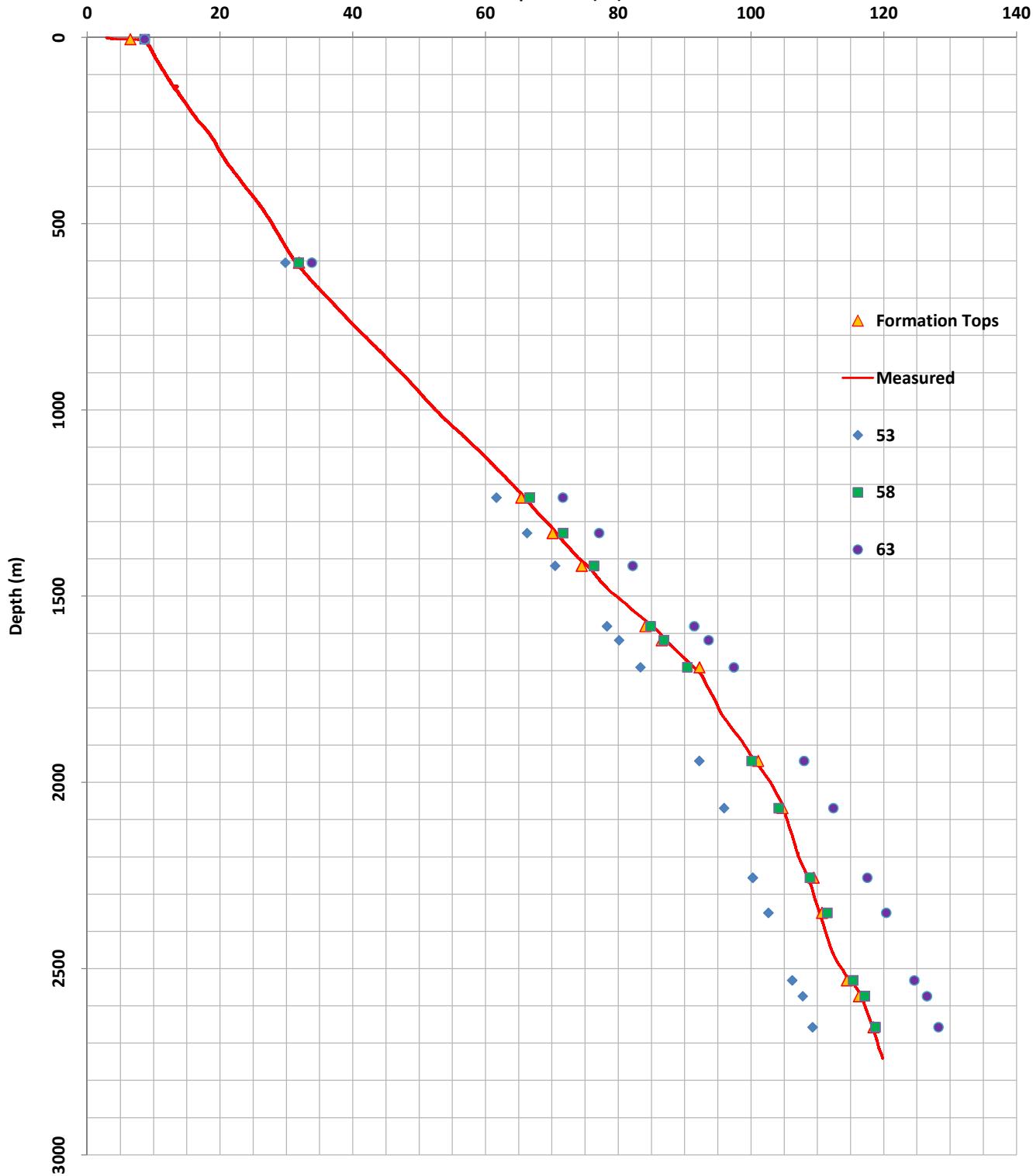


Temperature Profile and Modeled Heat Flow

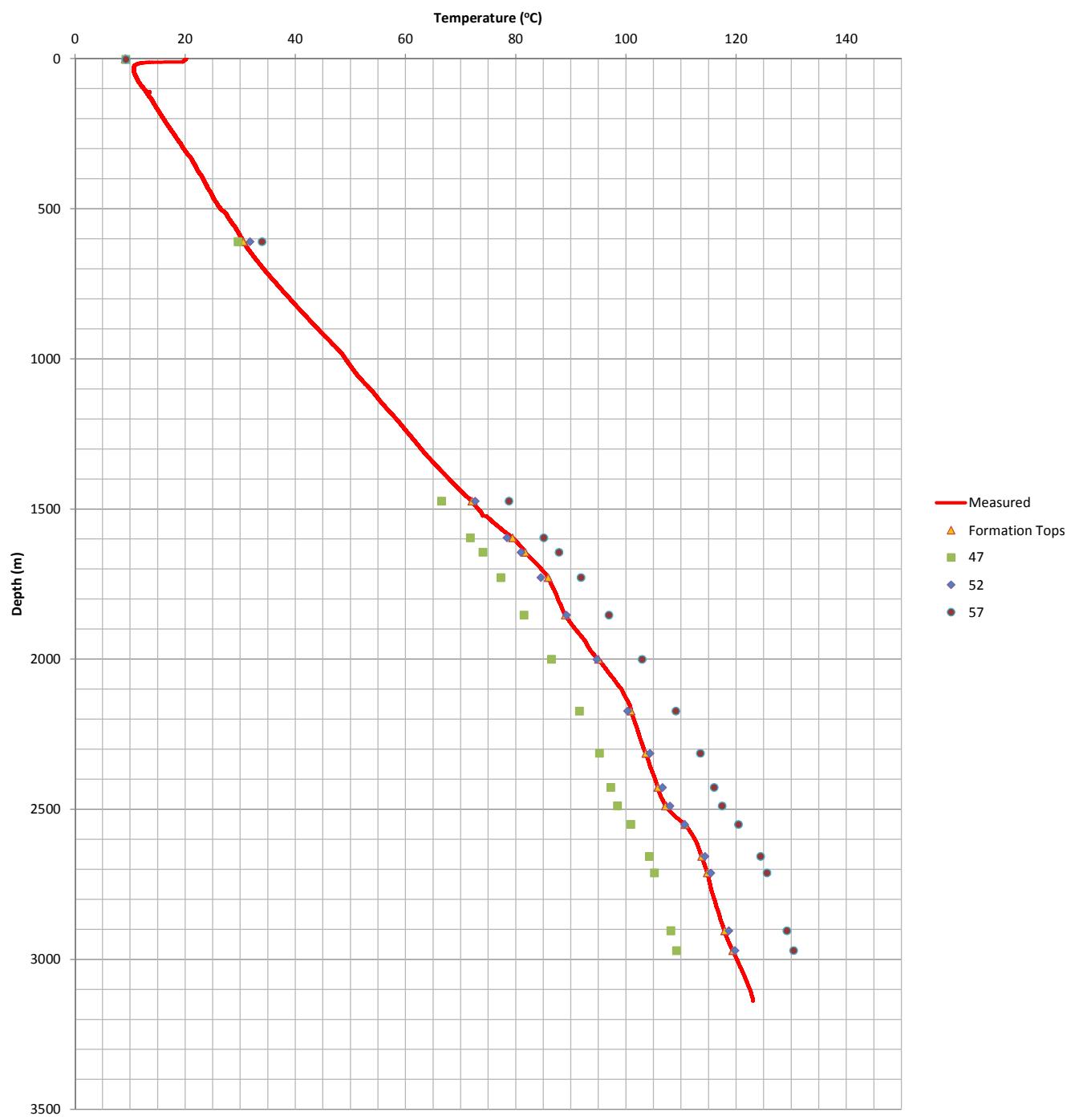
NDIC 15593 - FHMU K-810

Billings County, ND

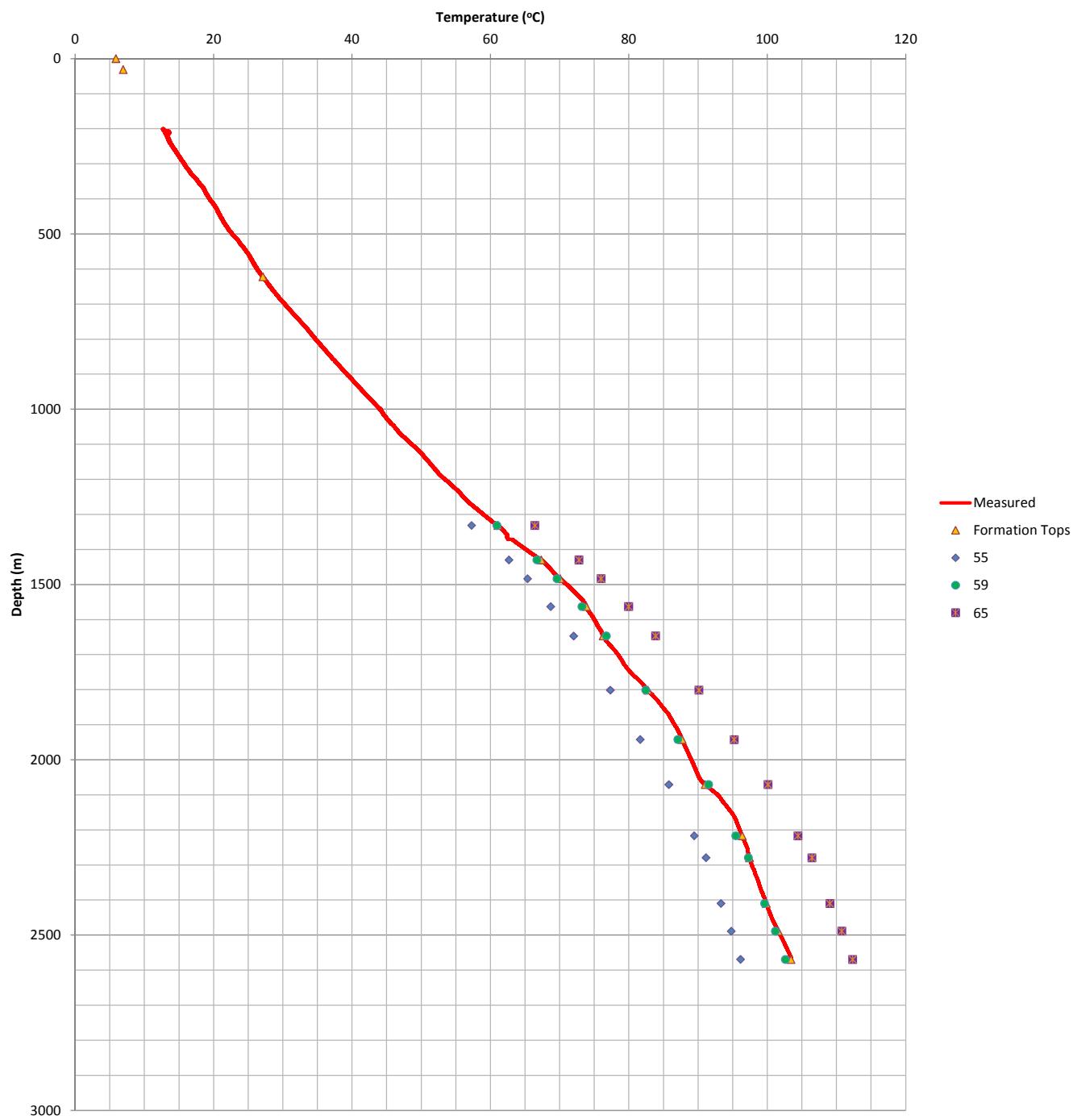
Temperature (oC)



Temperature Profile and Modeled Heat Flow
NDIC 15875 - Ann 1
McKenzie County, ND



Temperature Profile and Modeled Heat Flow
NDIC 16160 - Nelson 1-11H
McClean County, ND

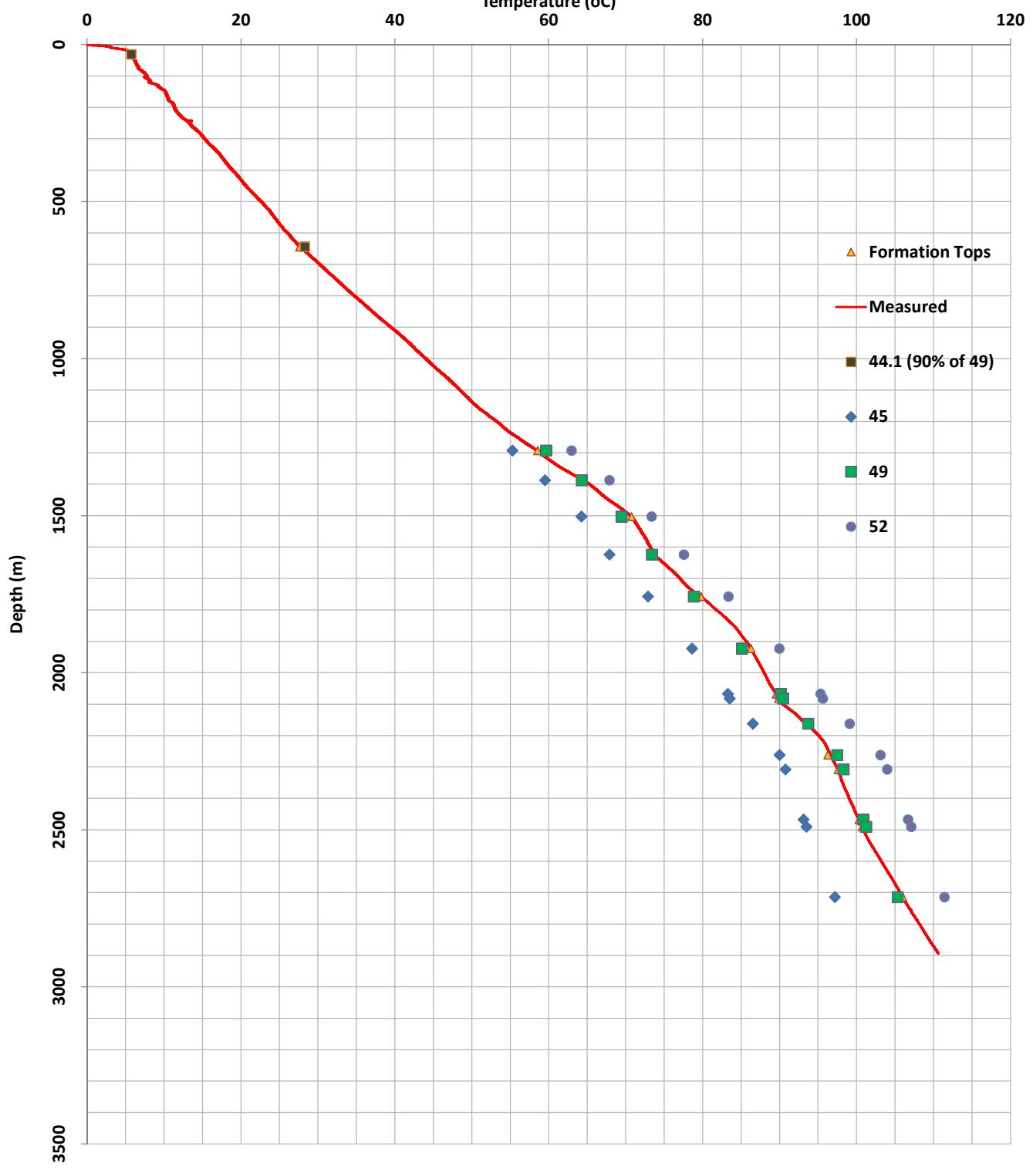


Temperature Profile and Modeled Heat Flow

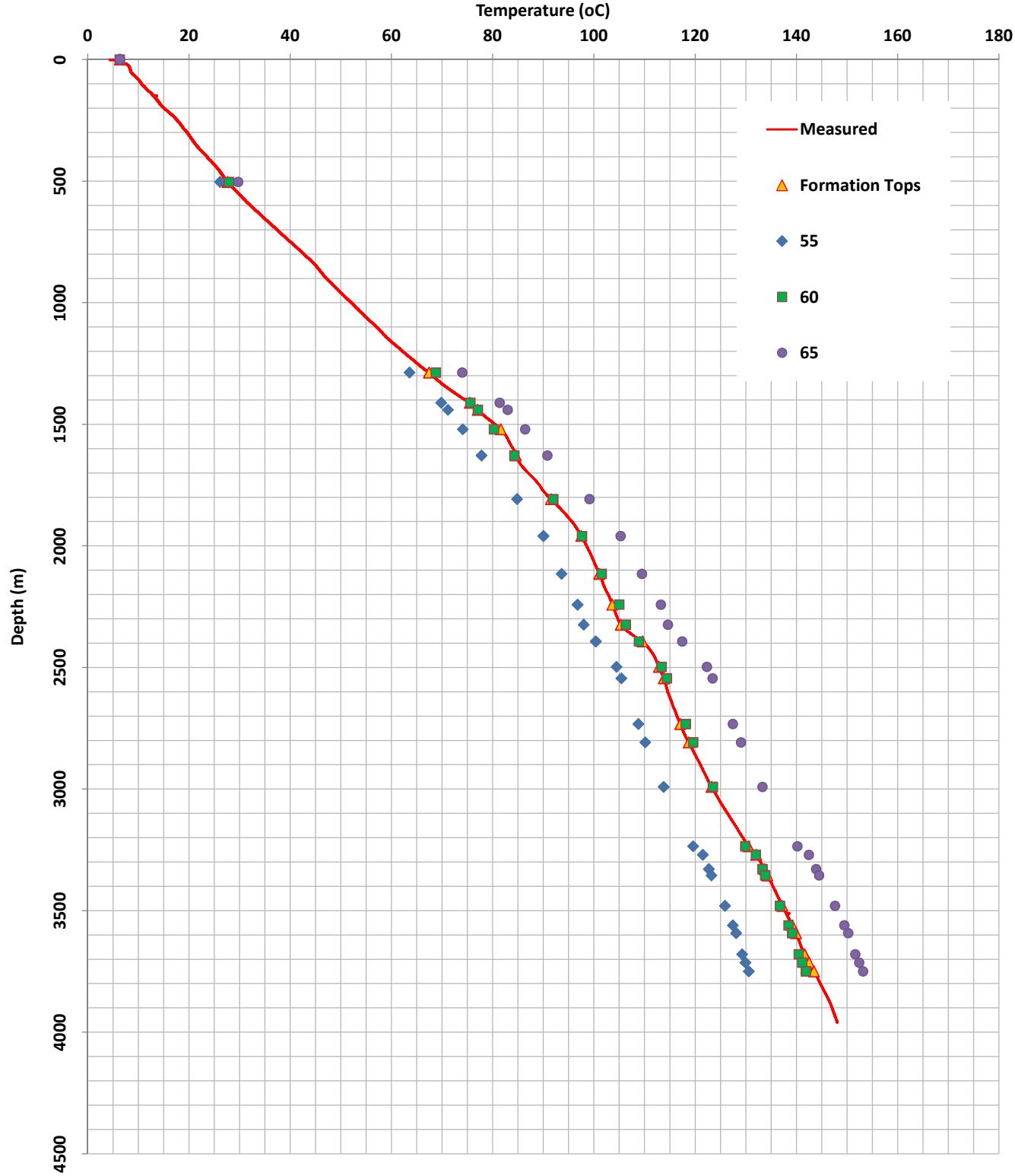
NDIC 16182 - NDCA7

Williams County, ND

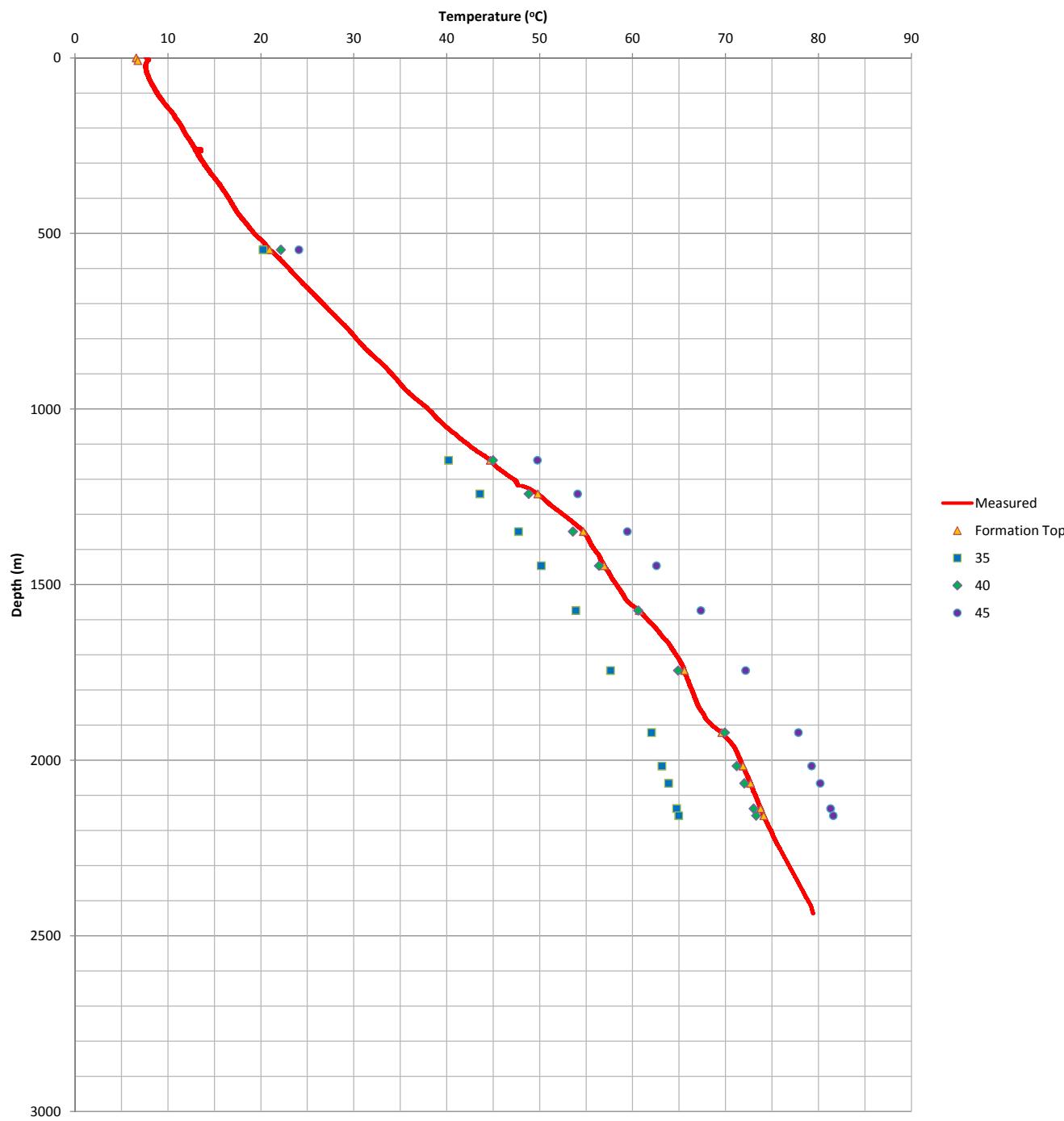
Temperature (°C)



Temperature Profile and Modeled Heat Flow
NDIC 16376 - Vernie Chapin 32-21
McKenzie County, ND



Temperature Profile and Modeled Heat Flow
NDIC 17014 - Edwards 1-33BH
Mountrail County, ND

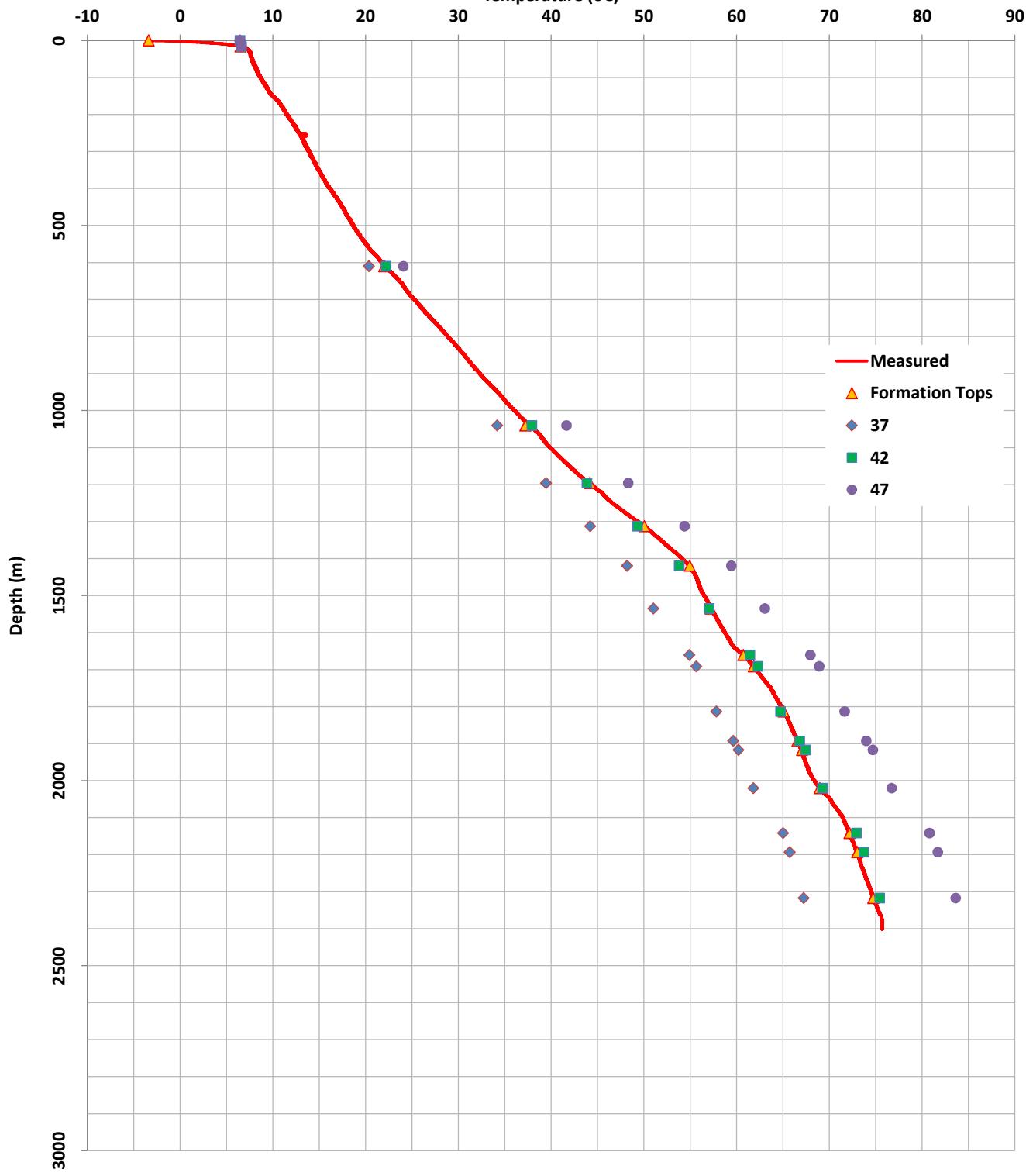


Temperature Profile and Modeled Heat Flow

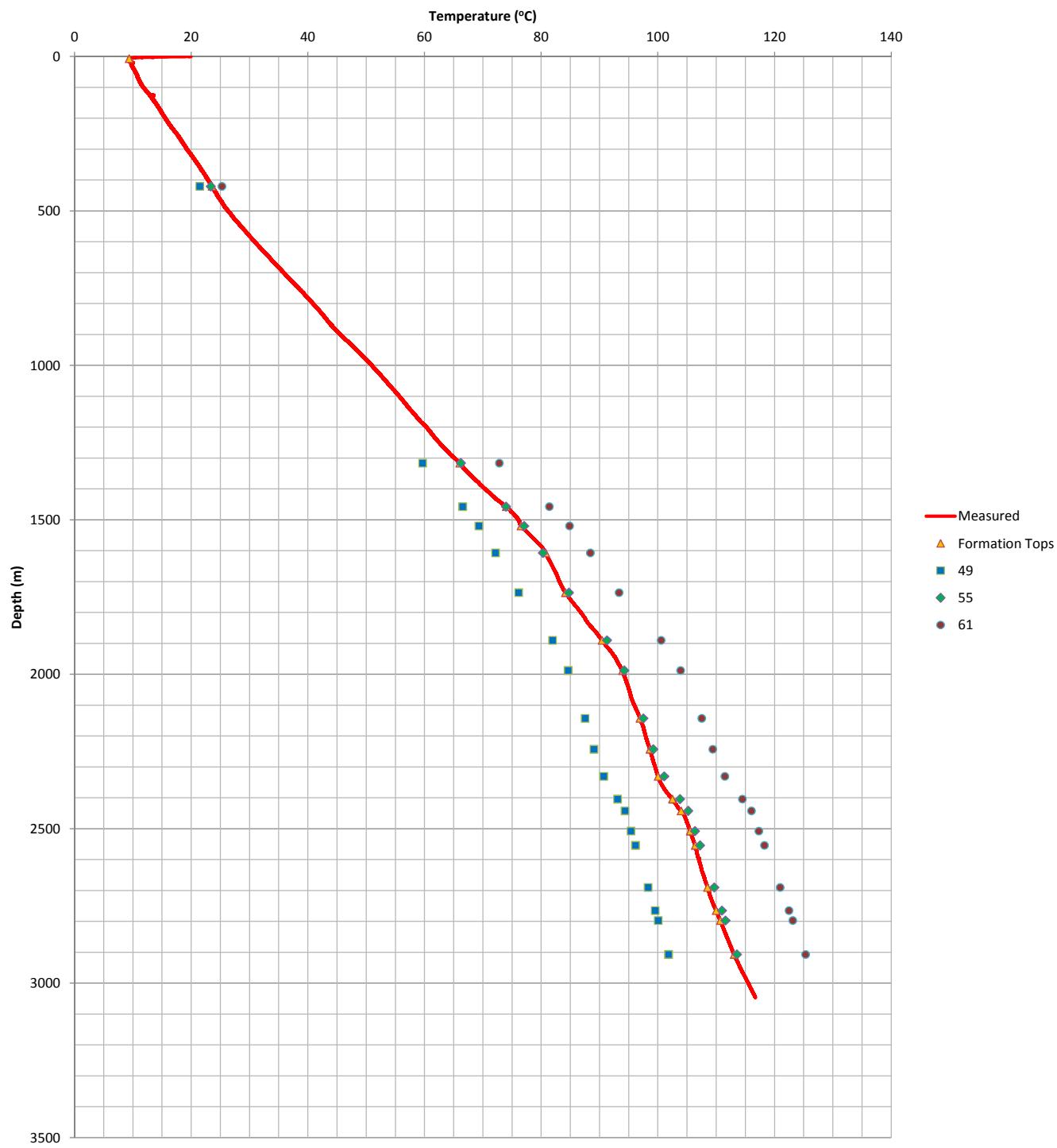
NDIC 17043 - St. Andes 151-89-2413H-1

Mountrail County, ND

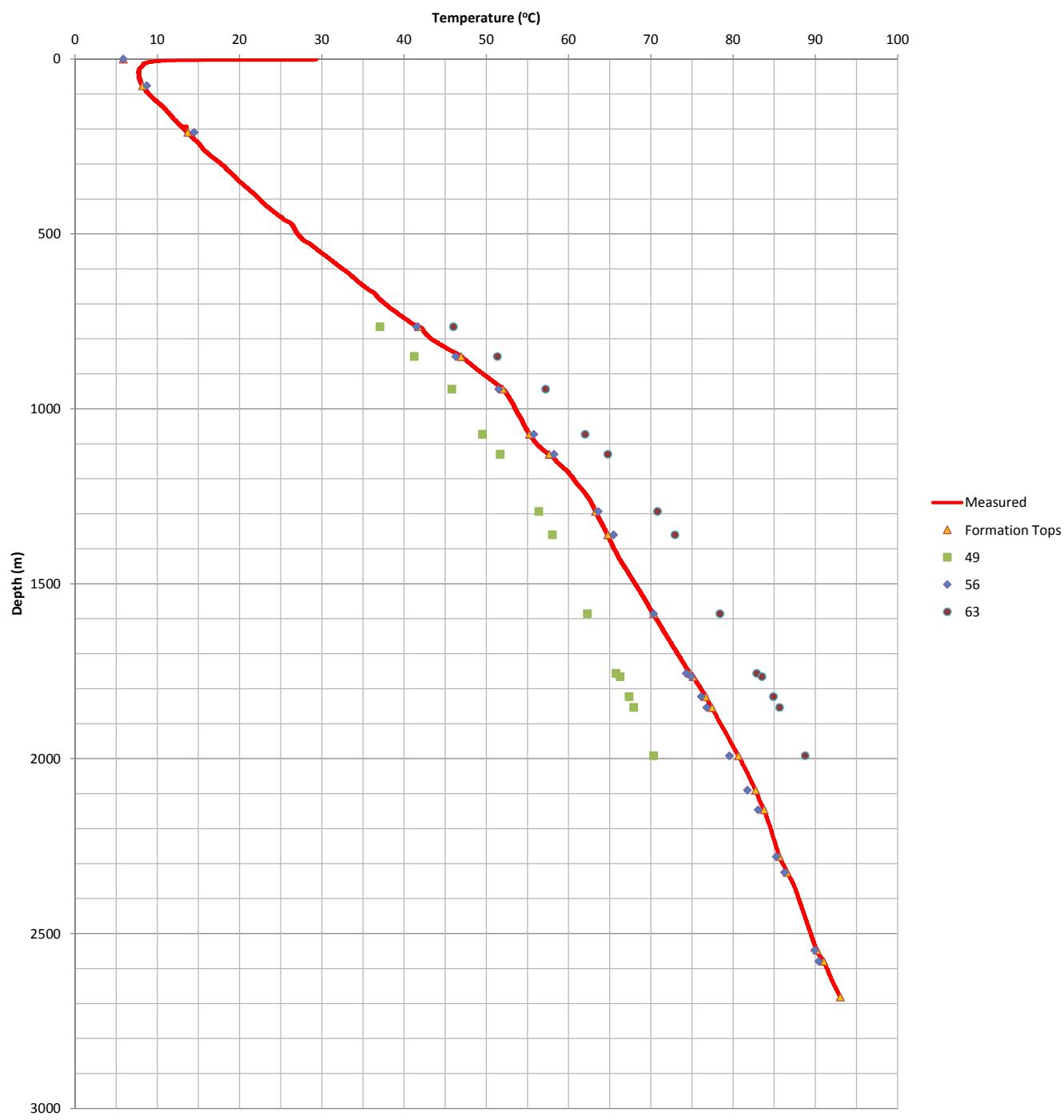
Temperature (oC)



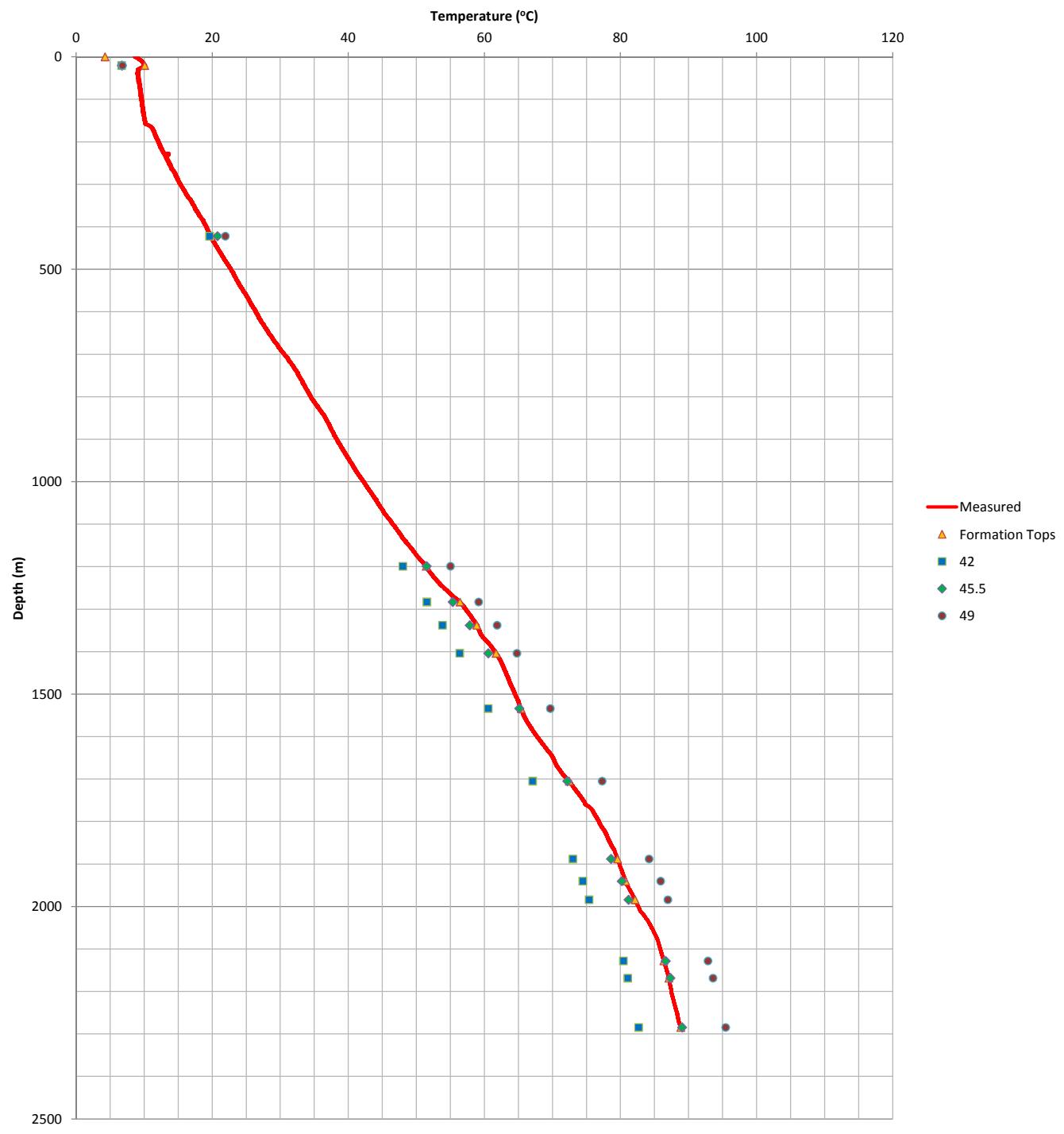
Temperature Profile and Modeled Heat Flow
NDIC 17230 - Roosevelt Federal 2-4H
Billings County, ND



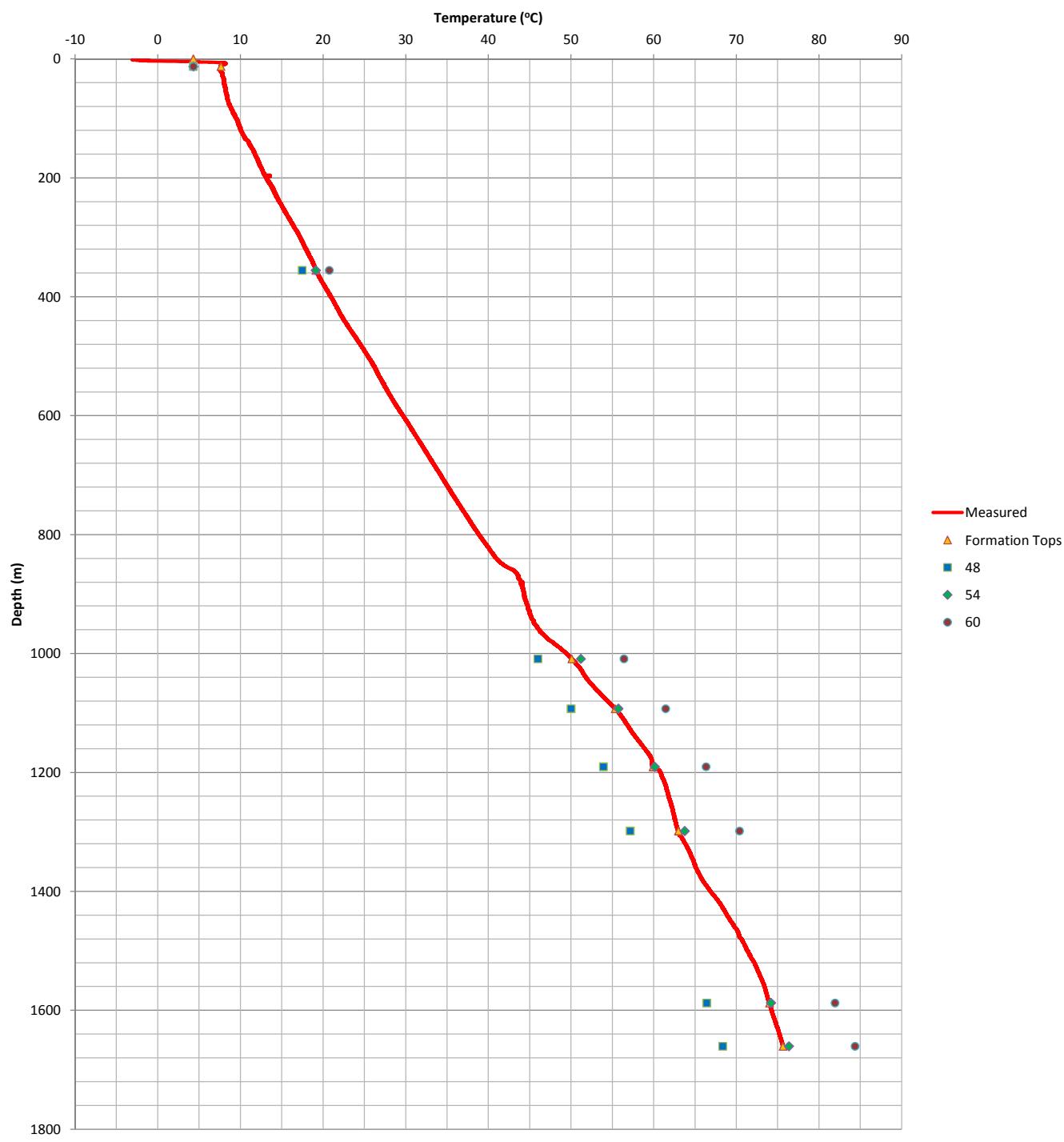
Temperature Profile and Modeled Heat Flow
NDIC 17317 - E-M Emmel 10-3
Renville County, ND



Temperature Profile and Modeled Heat Flow
NDIC 3090 - Grenora-Madison Unit 08
Williams County, ND



Temperature Profile and Modeled Heat Flow
NDIC 13725 - JC Woods 26H-1
Burke County, ND



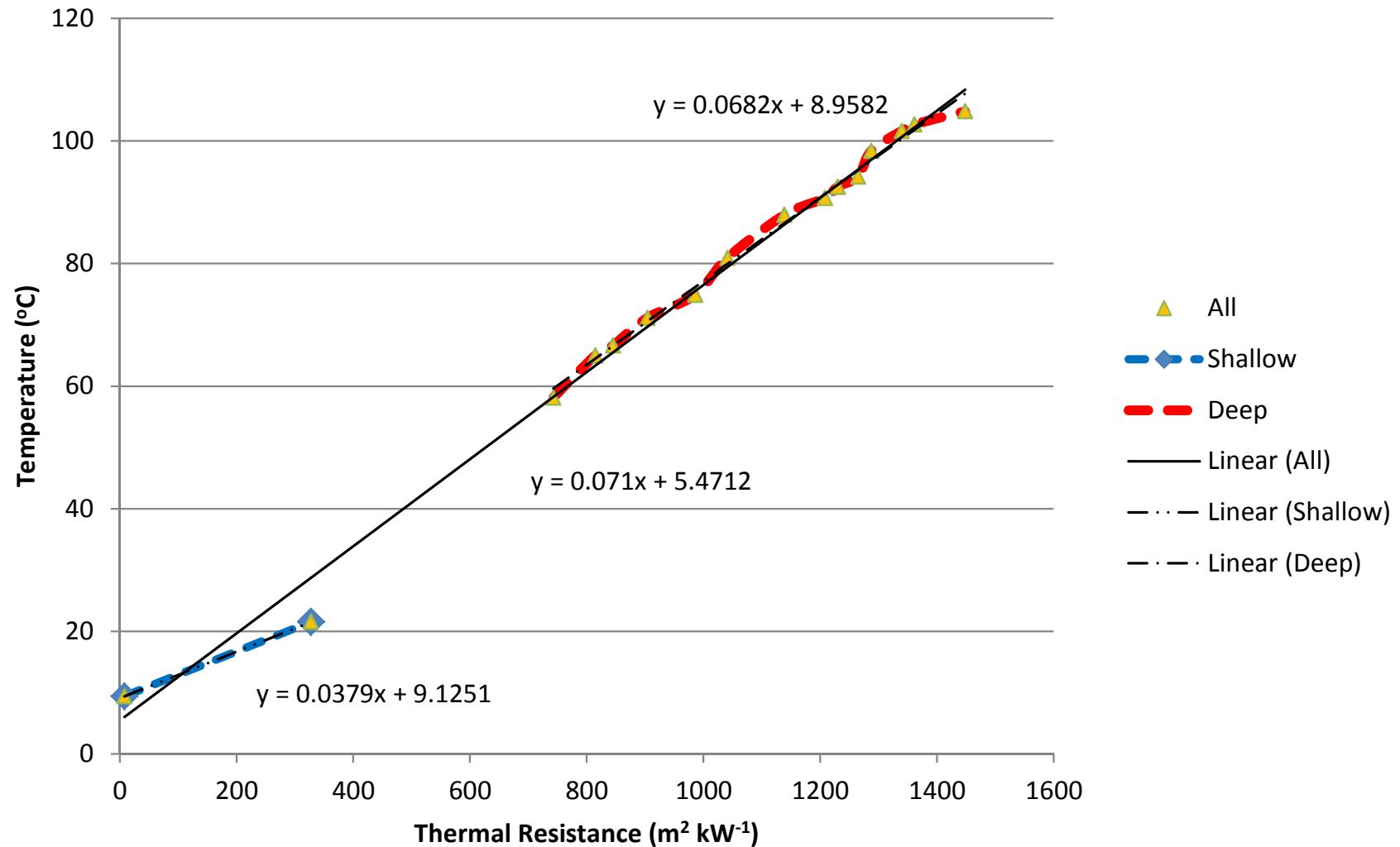
APPENDIX D

BULLARD METHOD PLOTS

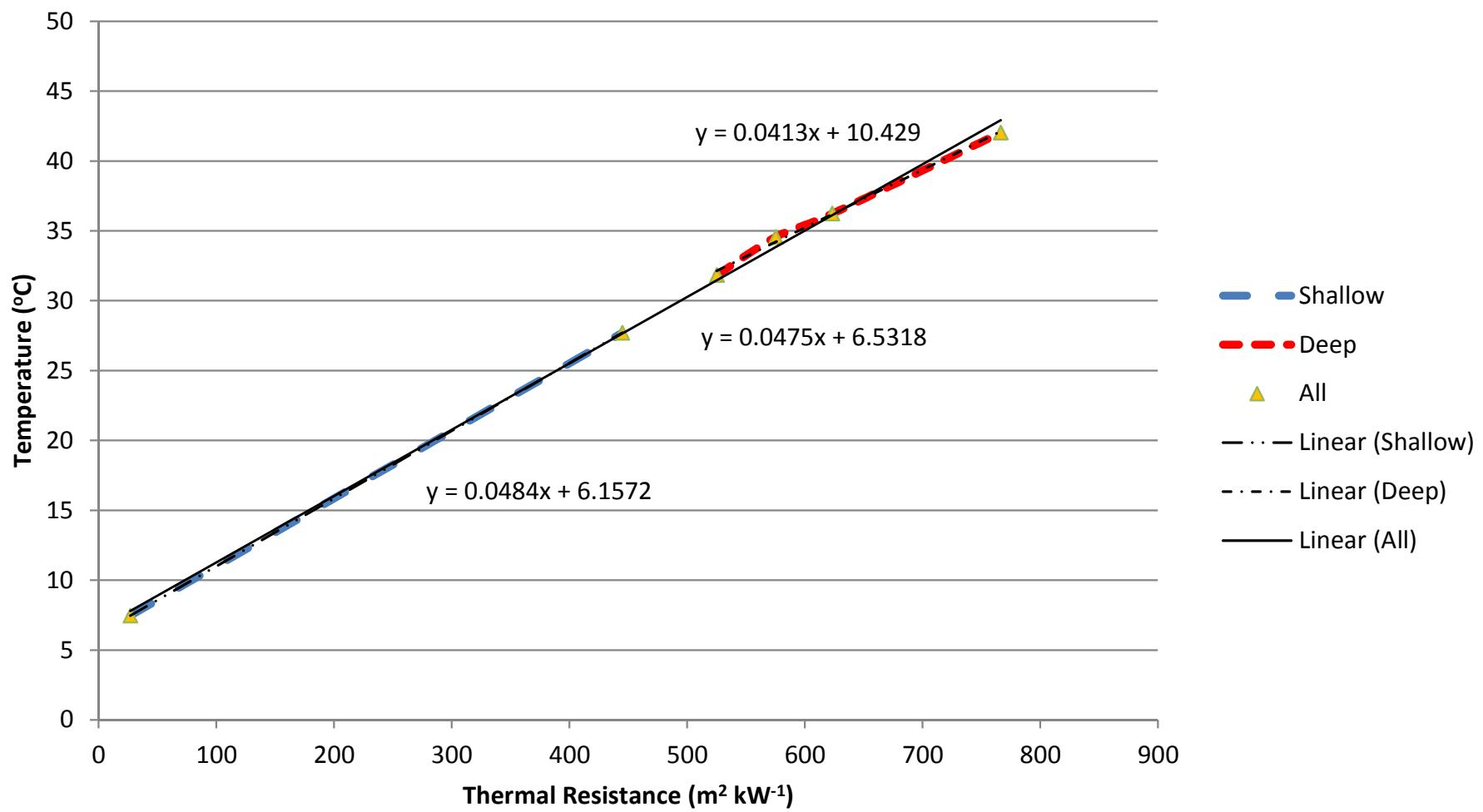
Bullard Method

NDIC 1140 Capa Madison Unit H-205

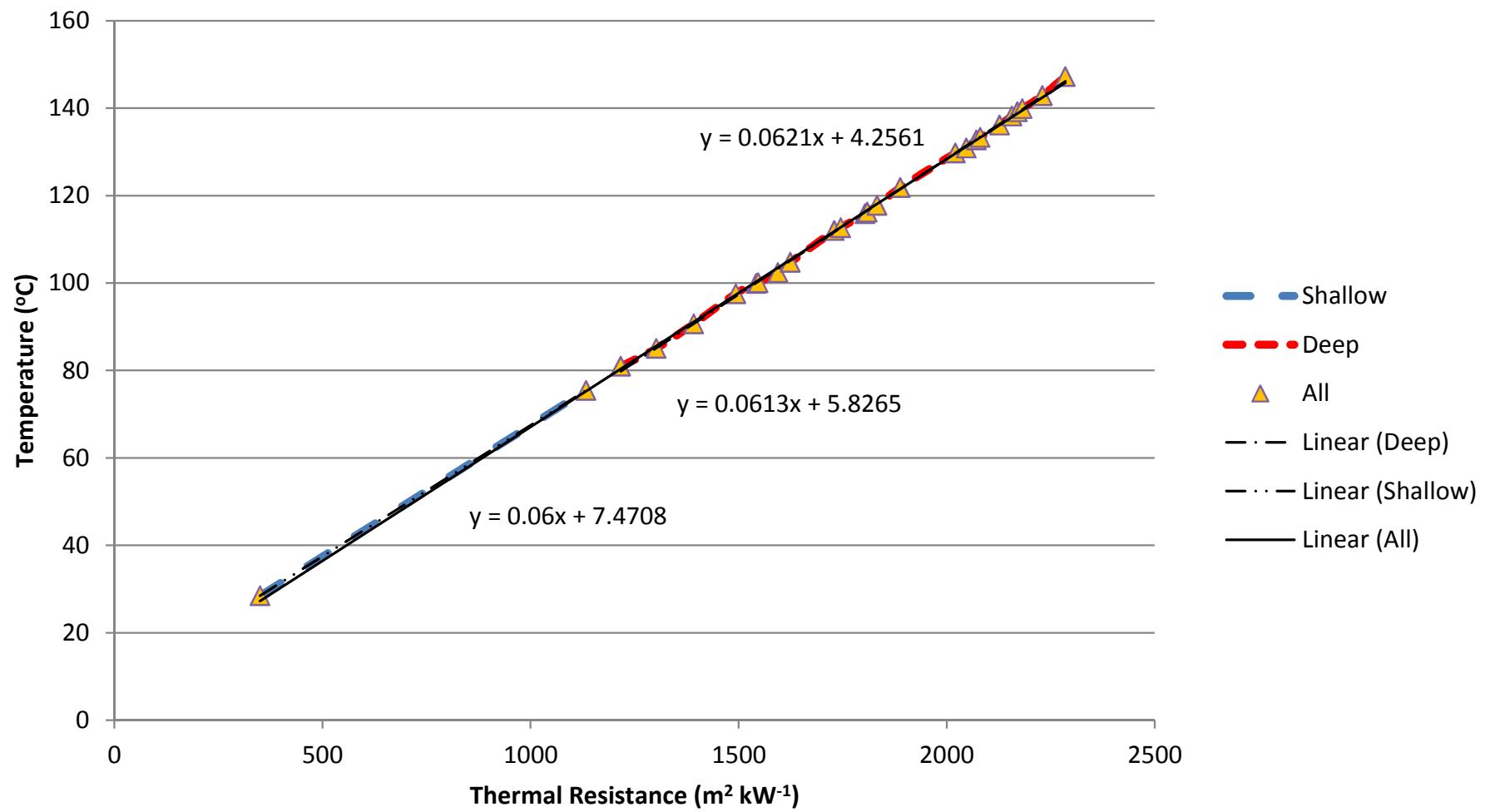
Williams County, ND



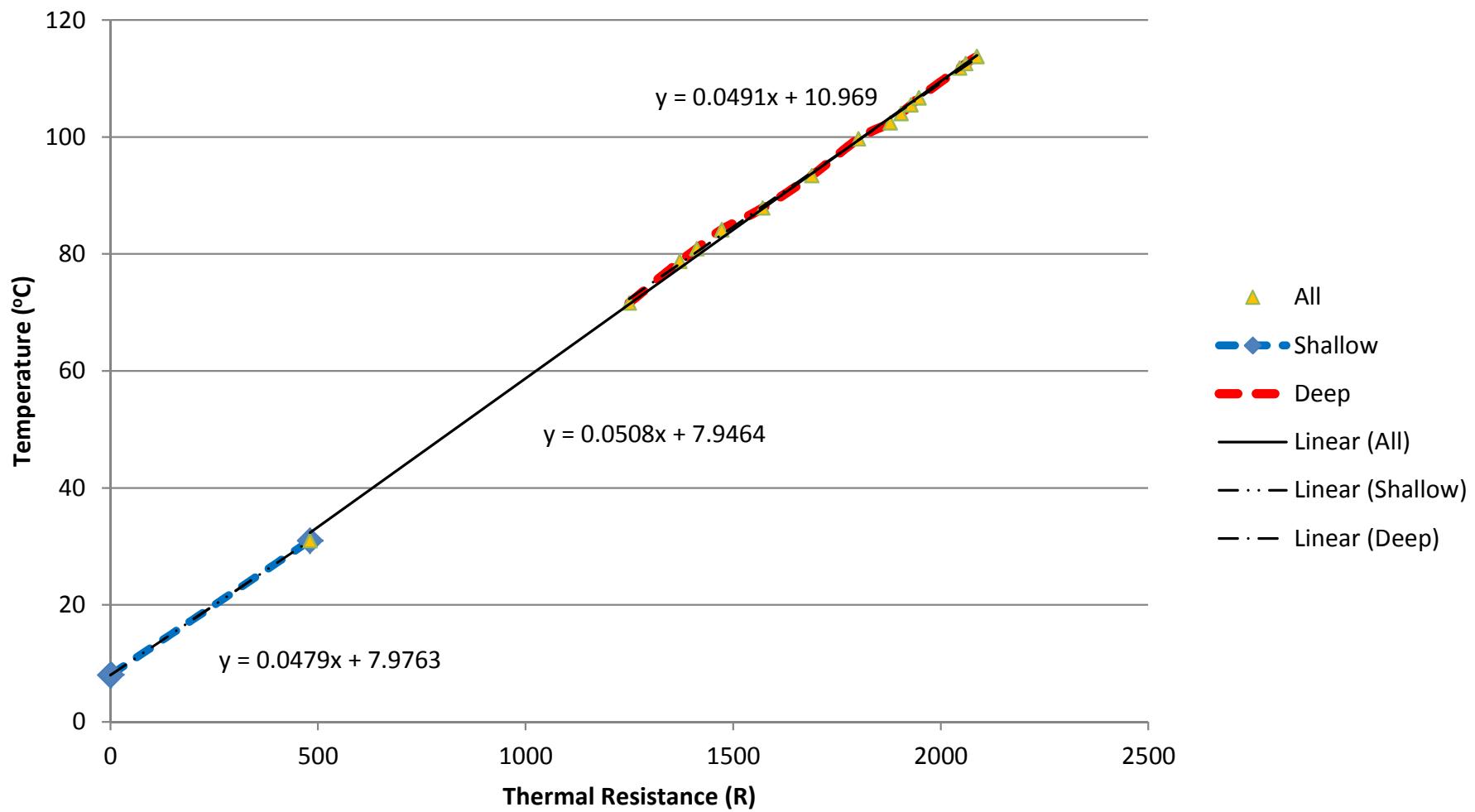
Bullard Method
NDIC 2139 NSCU V-706
Bottineau County, ND



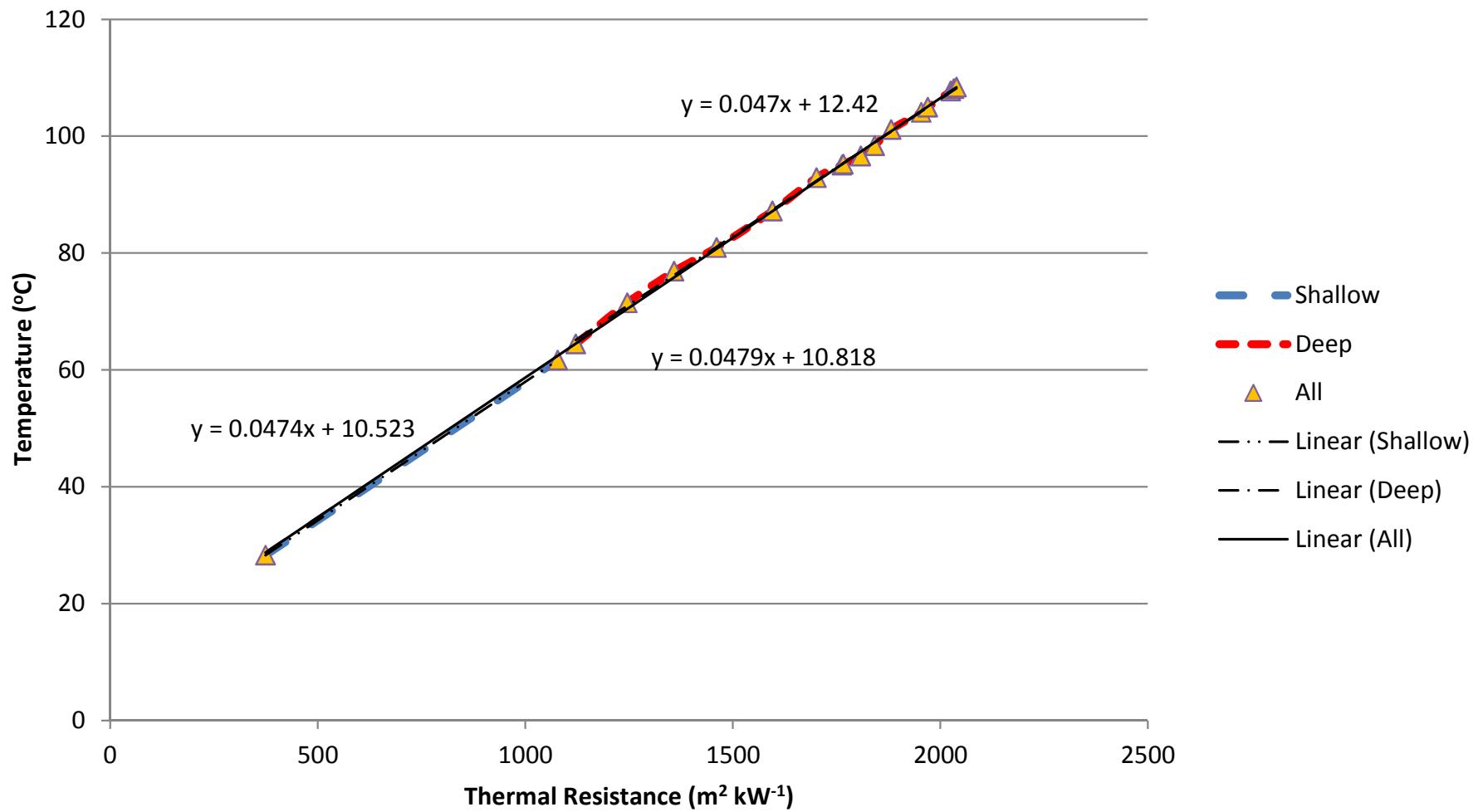
Bullard Method
NDIC 8005 - Sivertson 29-23R1
McKenzie County, ND



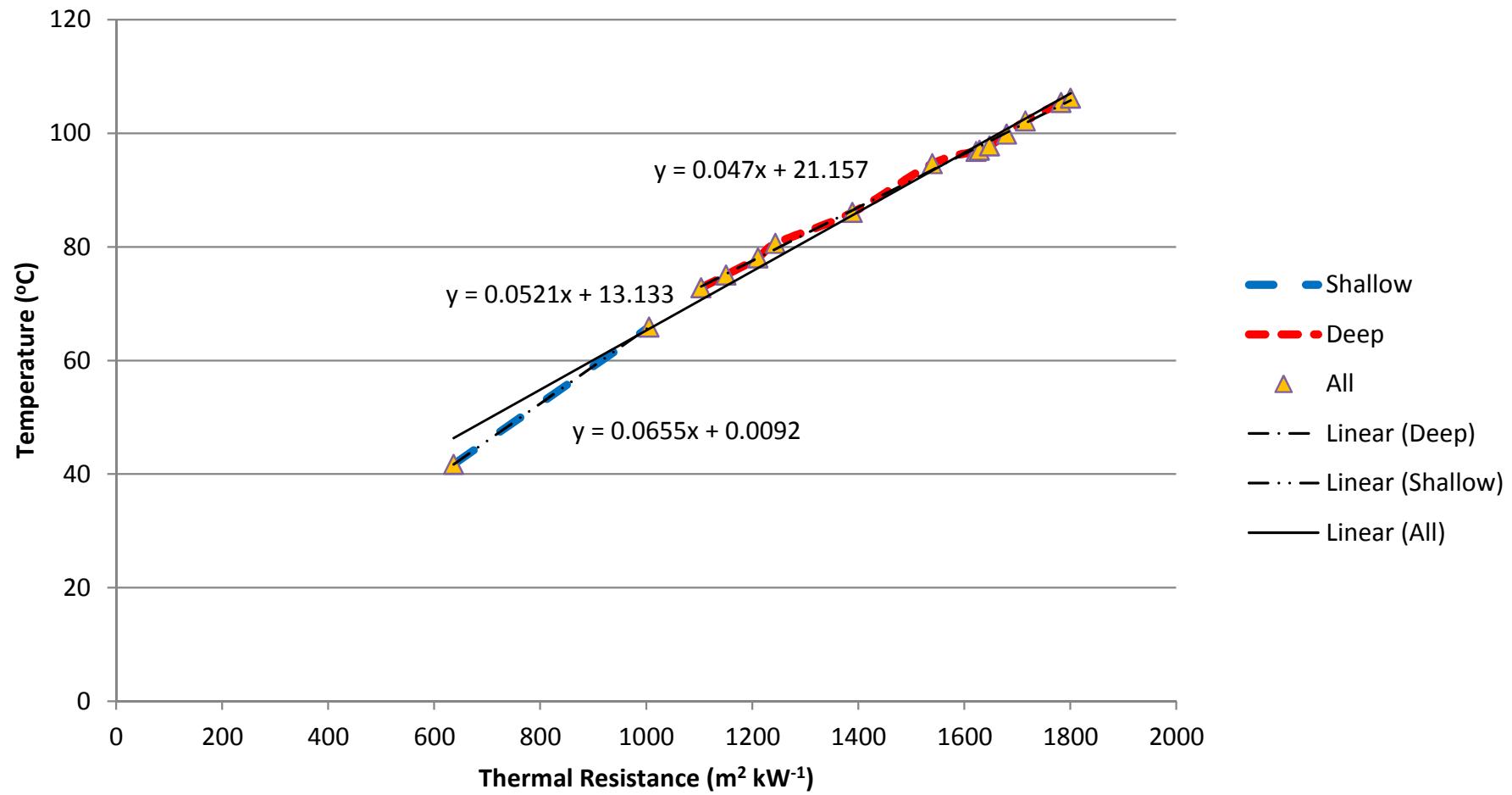
Bullard Method
NDIC 8706 - Berge C-1
McKenzie County, ND



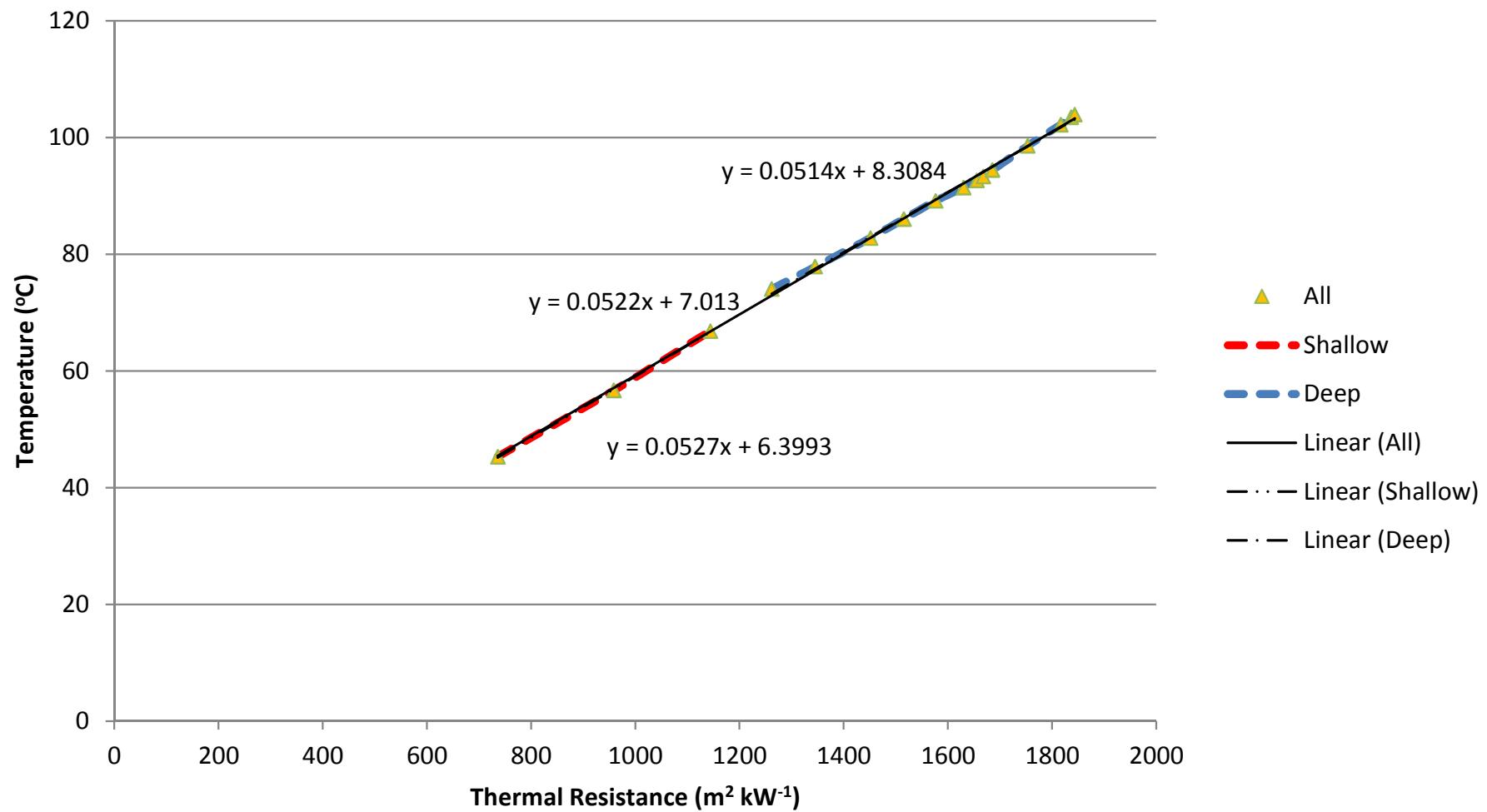
Bullard Method
NDIC 9653 - Cutlip 1
McKenzie County, ND



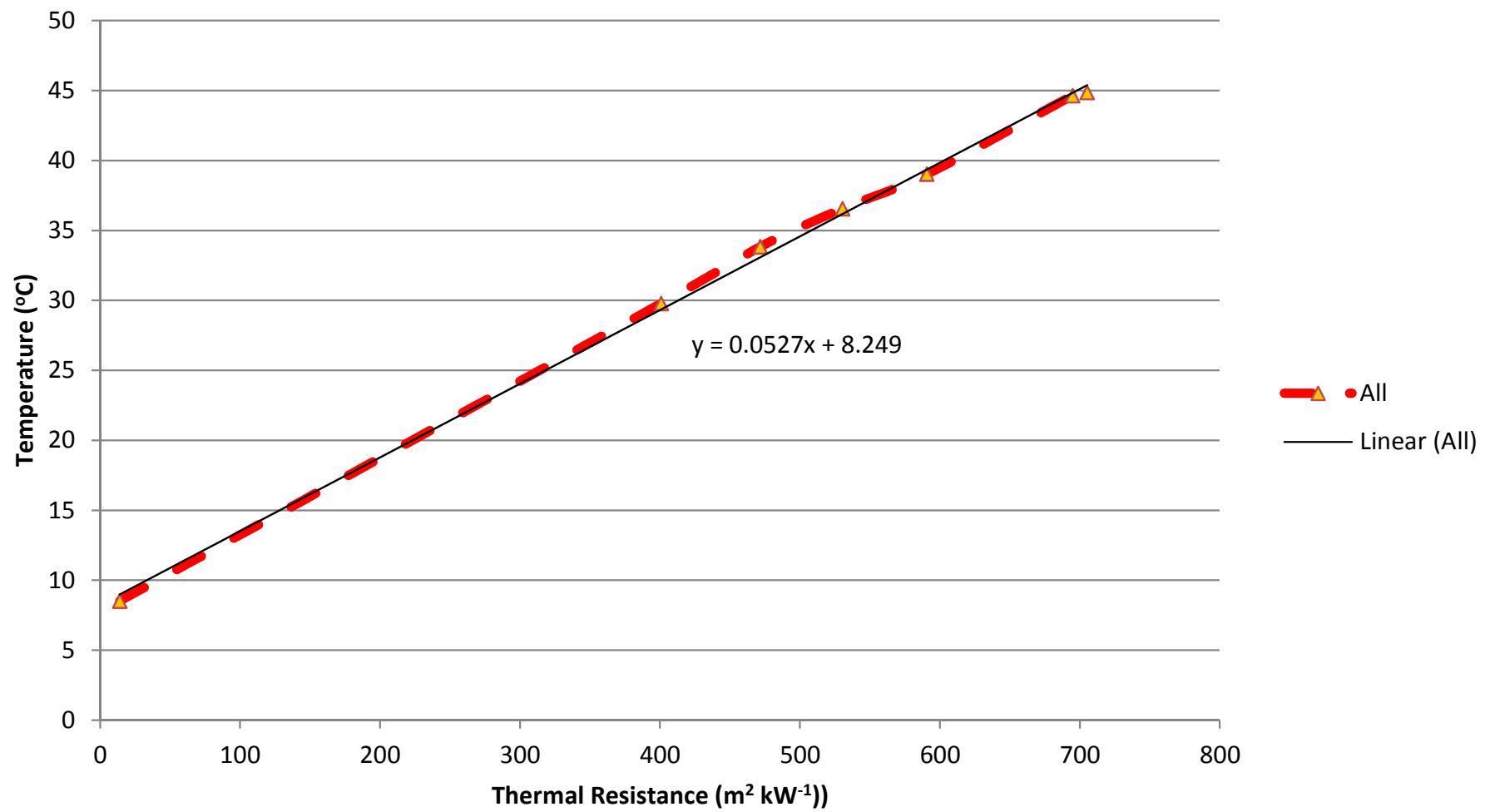
Bullard Method
NDIC 10103 - Iverson State A-1
McKenzie County, ND



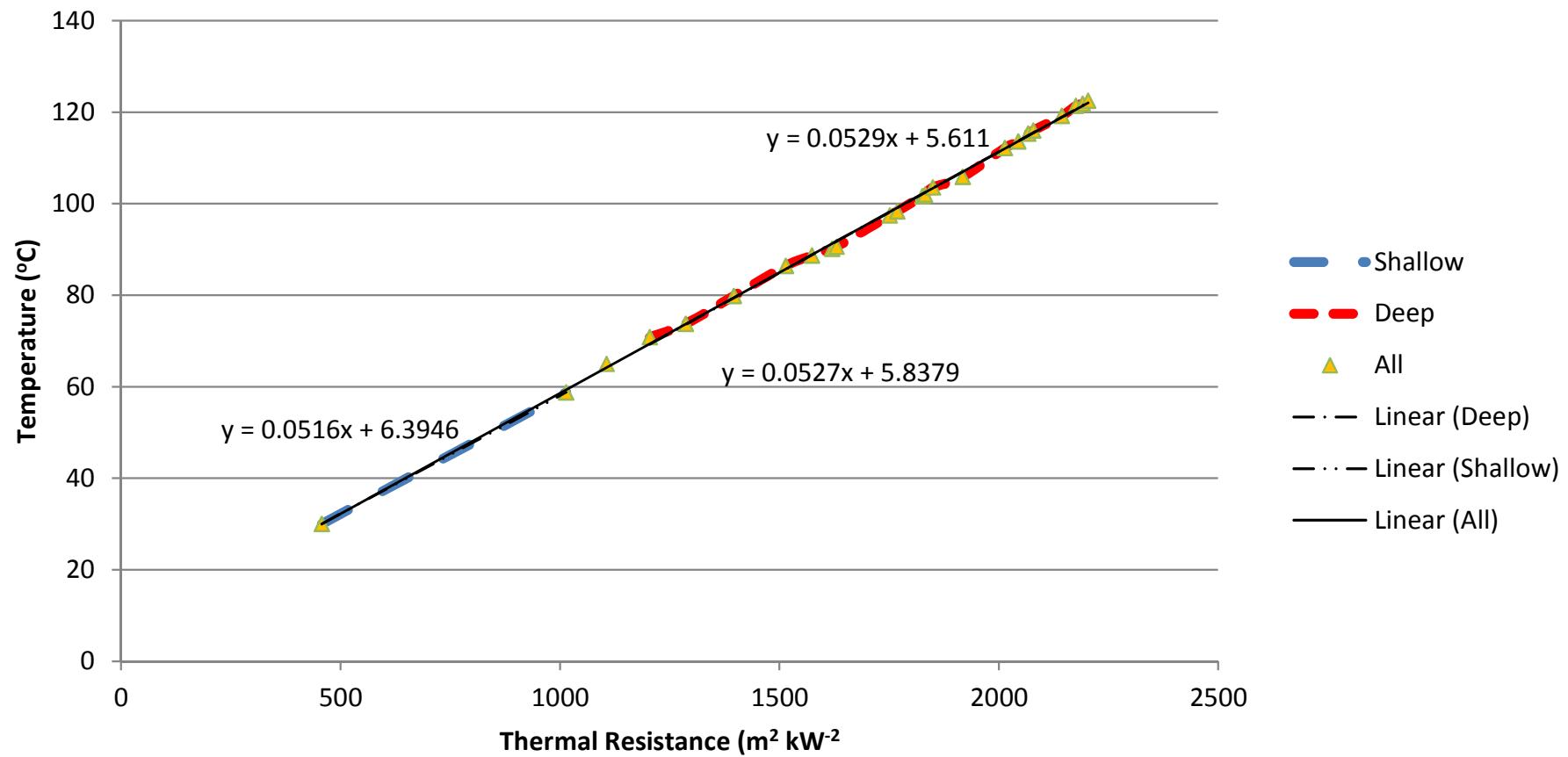
Bullard Method
NDIC 10278 - Mud Buttes State 1-36
Bowman County, ND



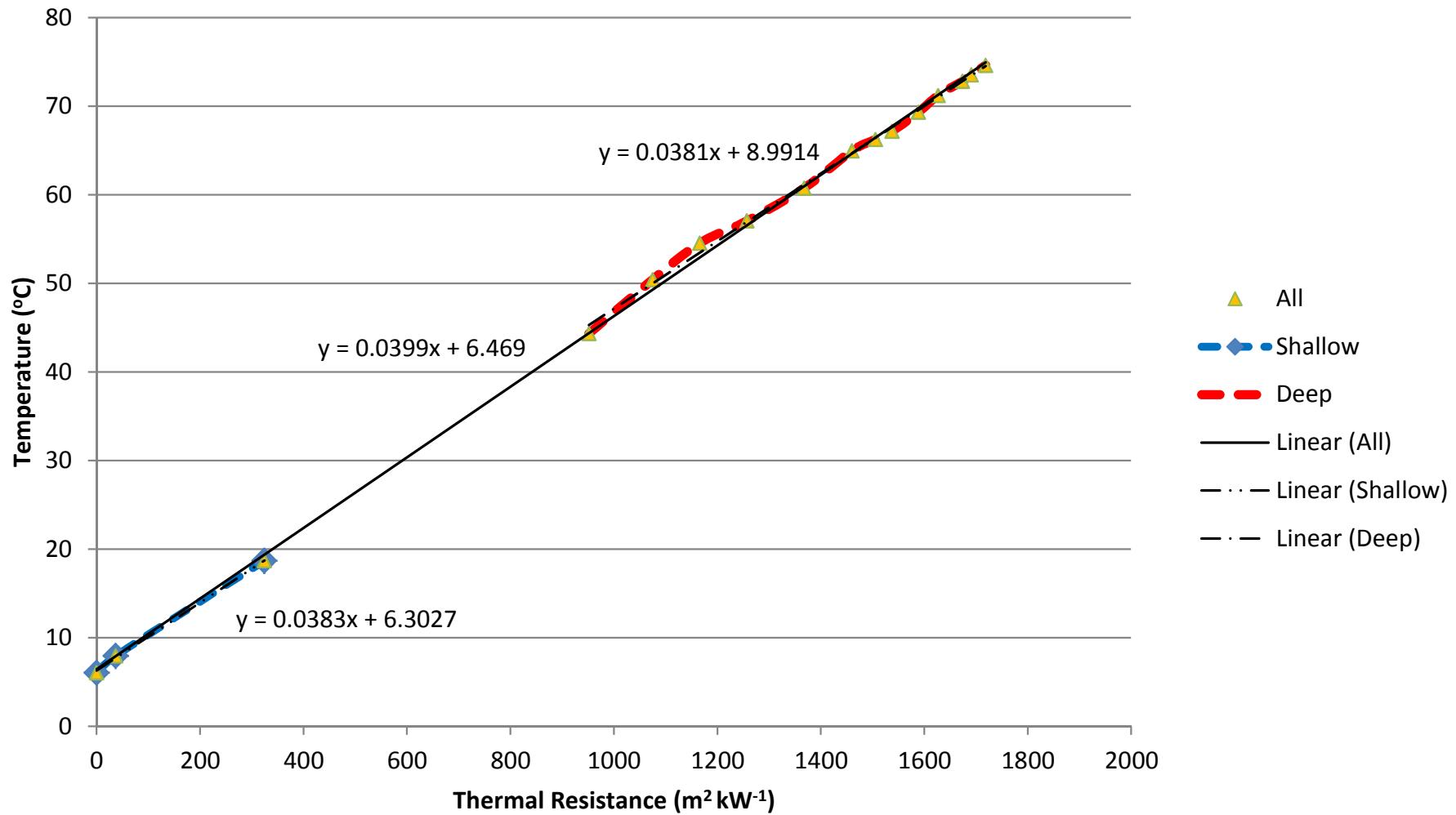
Bullard Method
NDIC 12280 - Bandjord 1-20
Bottineau County, ND



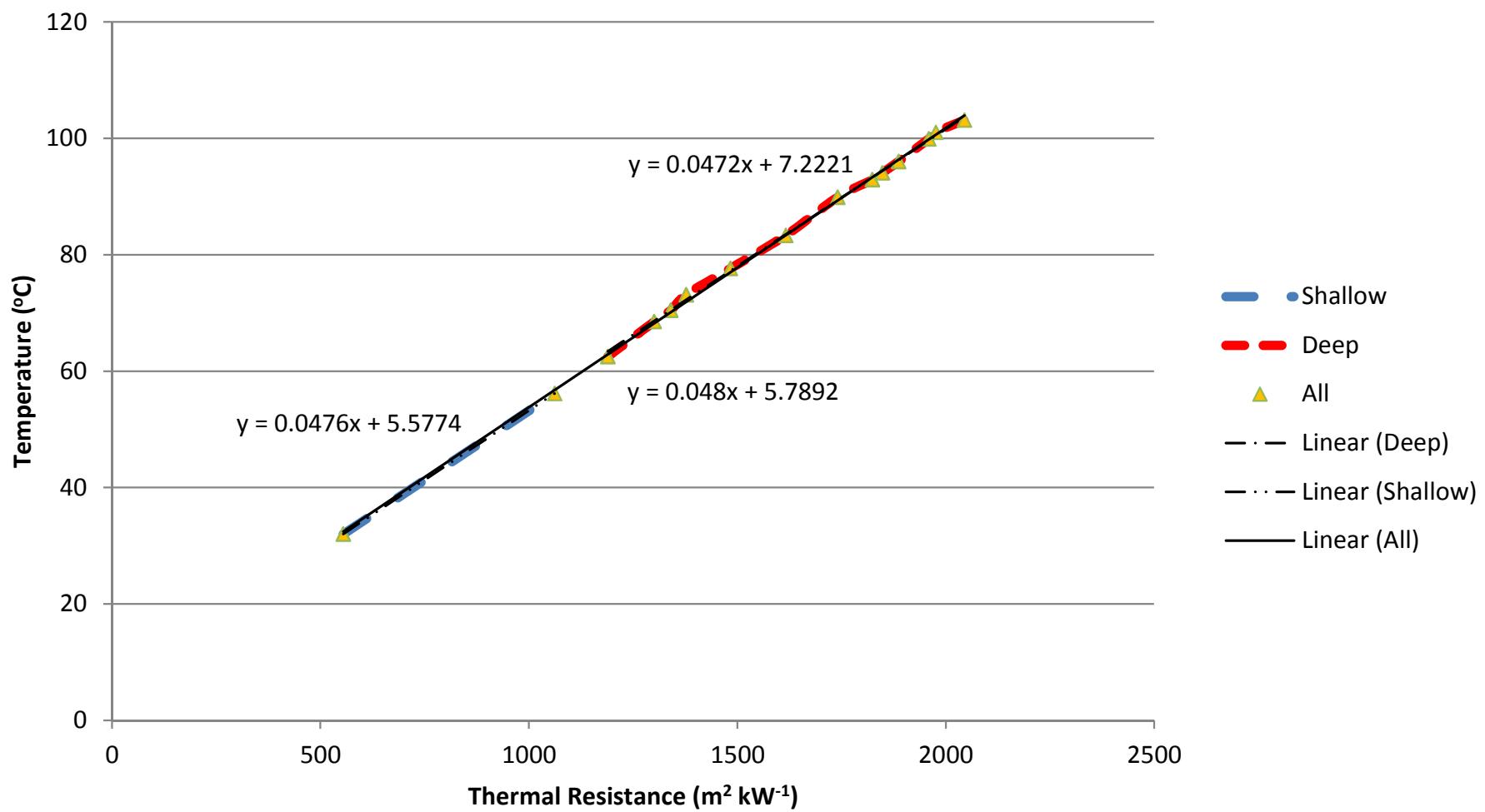
Bullard Method
NDIC 12363 Astrid Ongstad 14-22
Williams County, ND



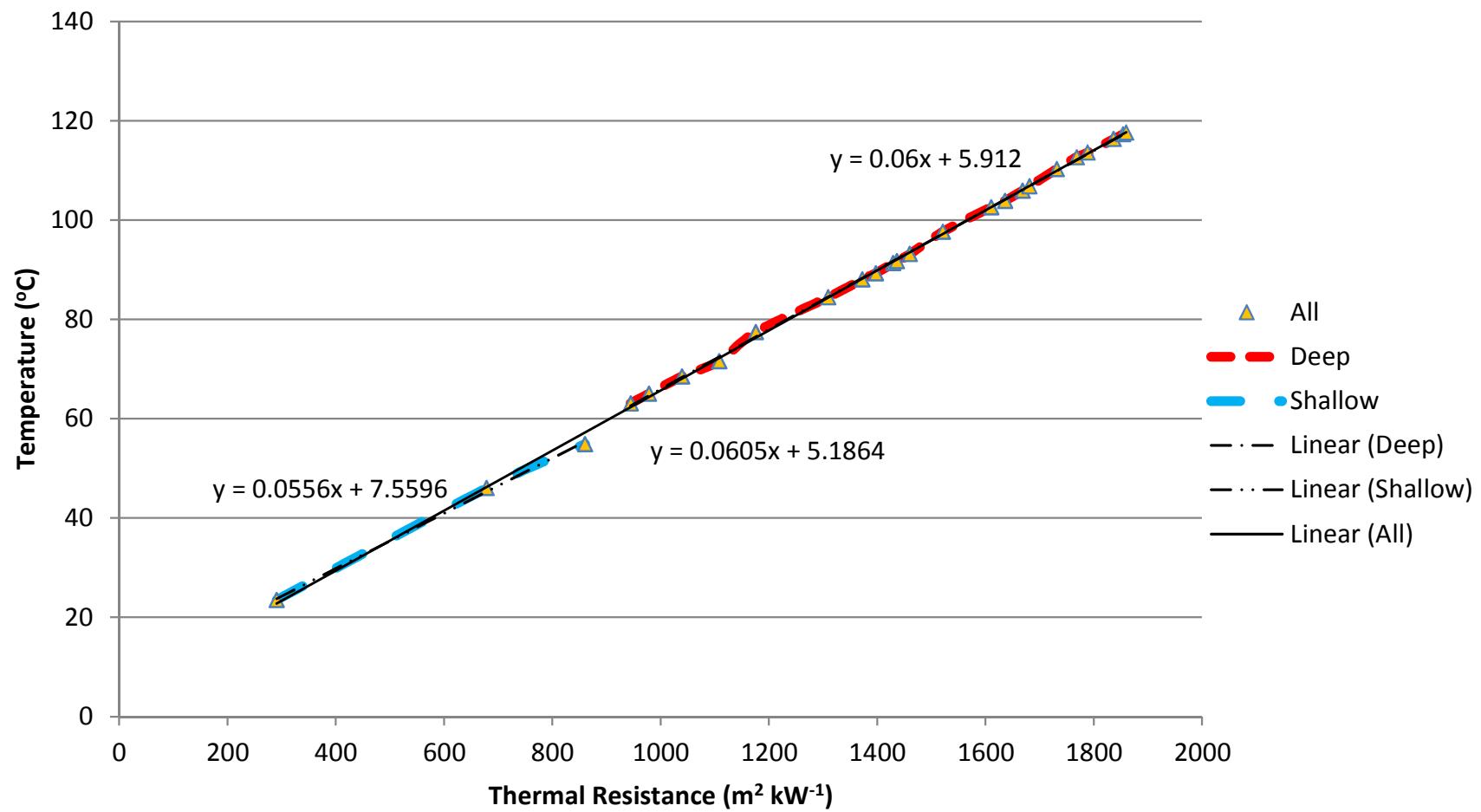
Bullard Method
NDIC 13132 - Frink 13-15
McClean County, ND



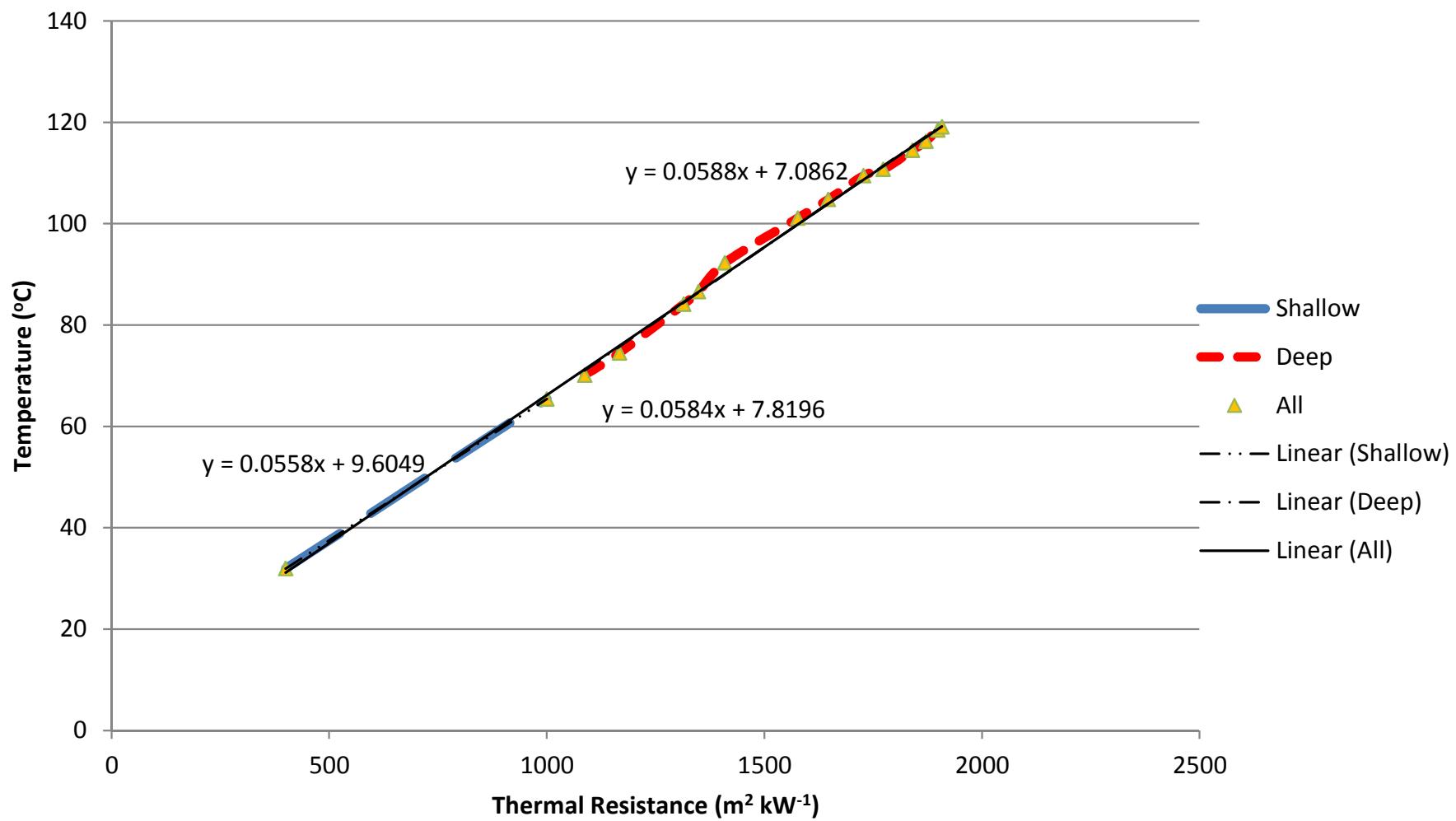
Bullard Method
NDIC 13666 - Rieder 1-9 SWD
Williams County, ND



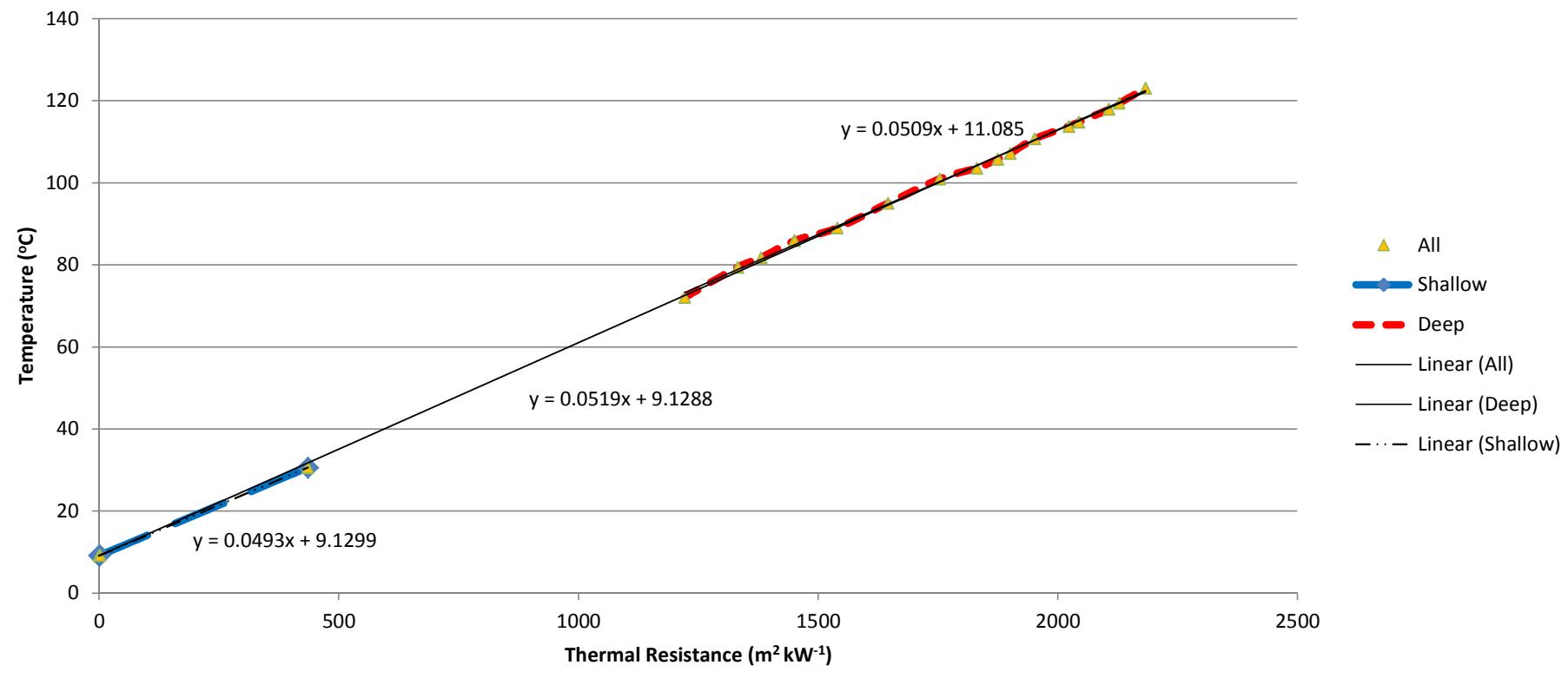
Bullard Method
NDIC 15137 Holte 6-21
Burke County, ND



Bullard Method
NDIC 15593 - FHMU K-810
Billings County, ND



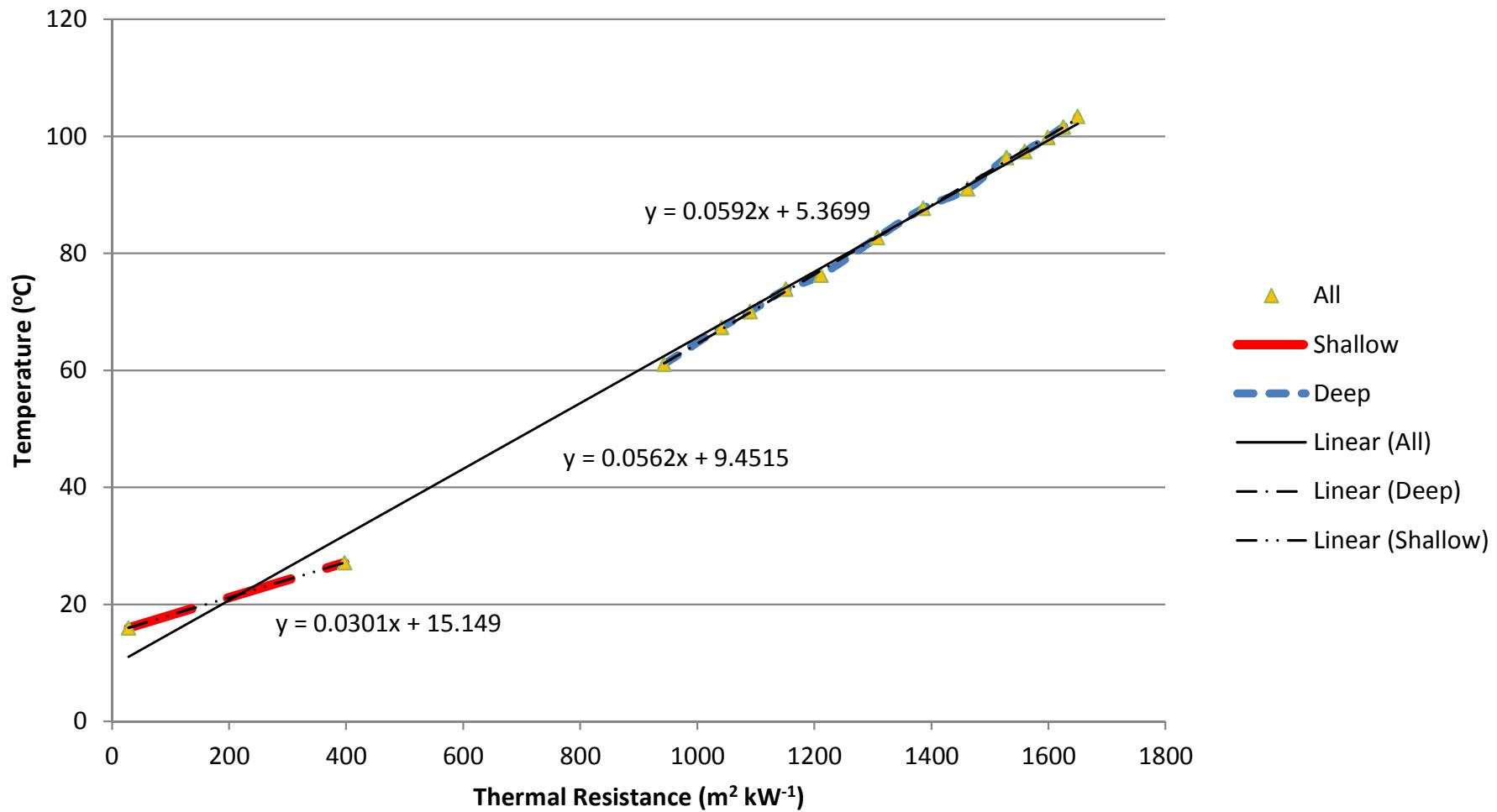
Bullard Method
NDIC 15875 - Ann 1
McKenzie County, ND



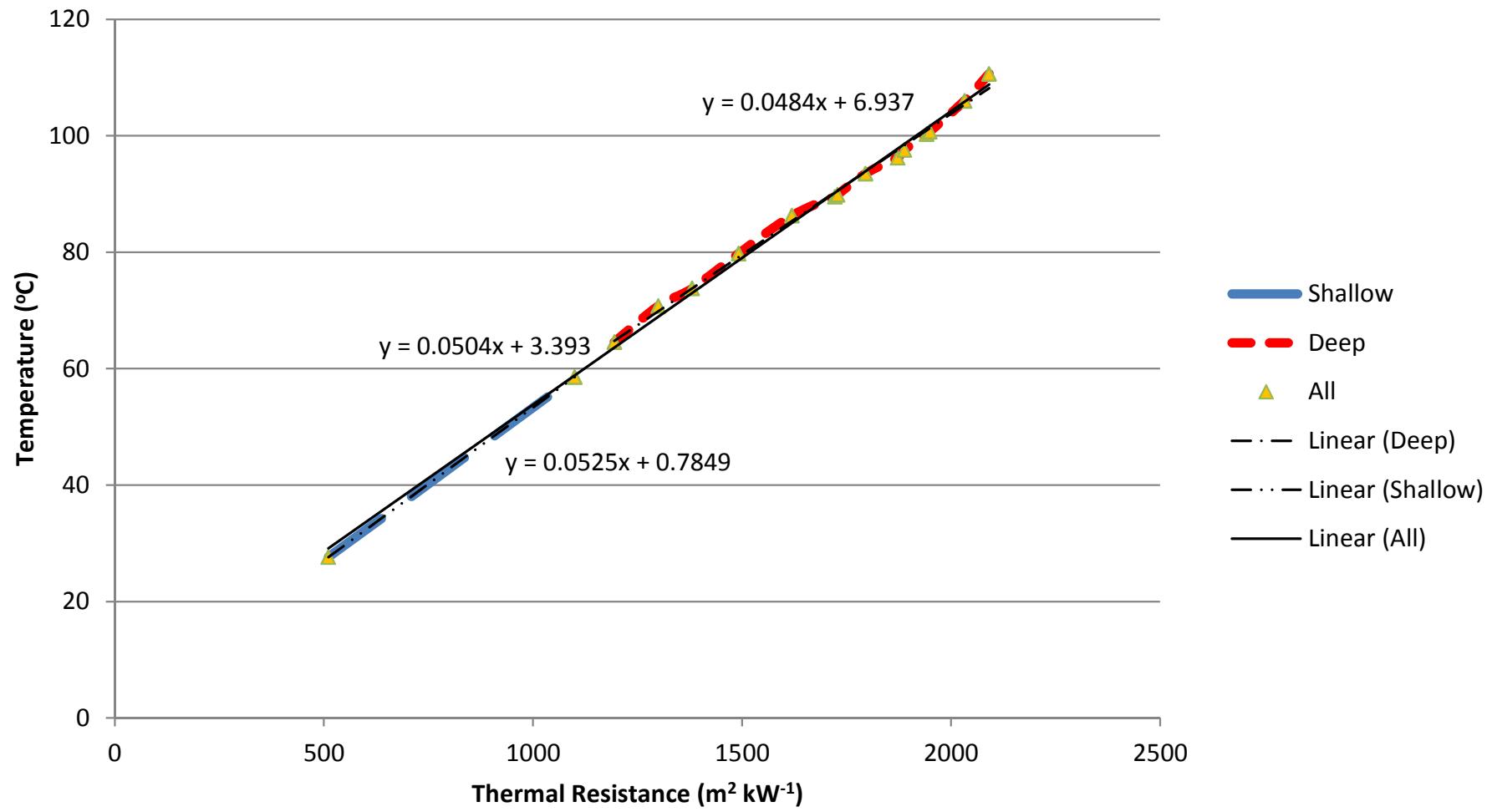
Bullard Method

NDIC 16160 - Nelson 1-11H

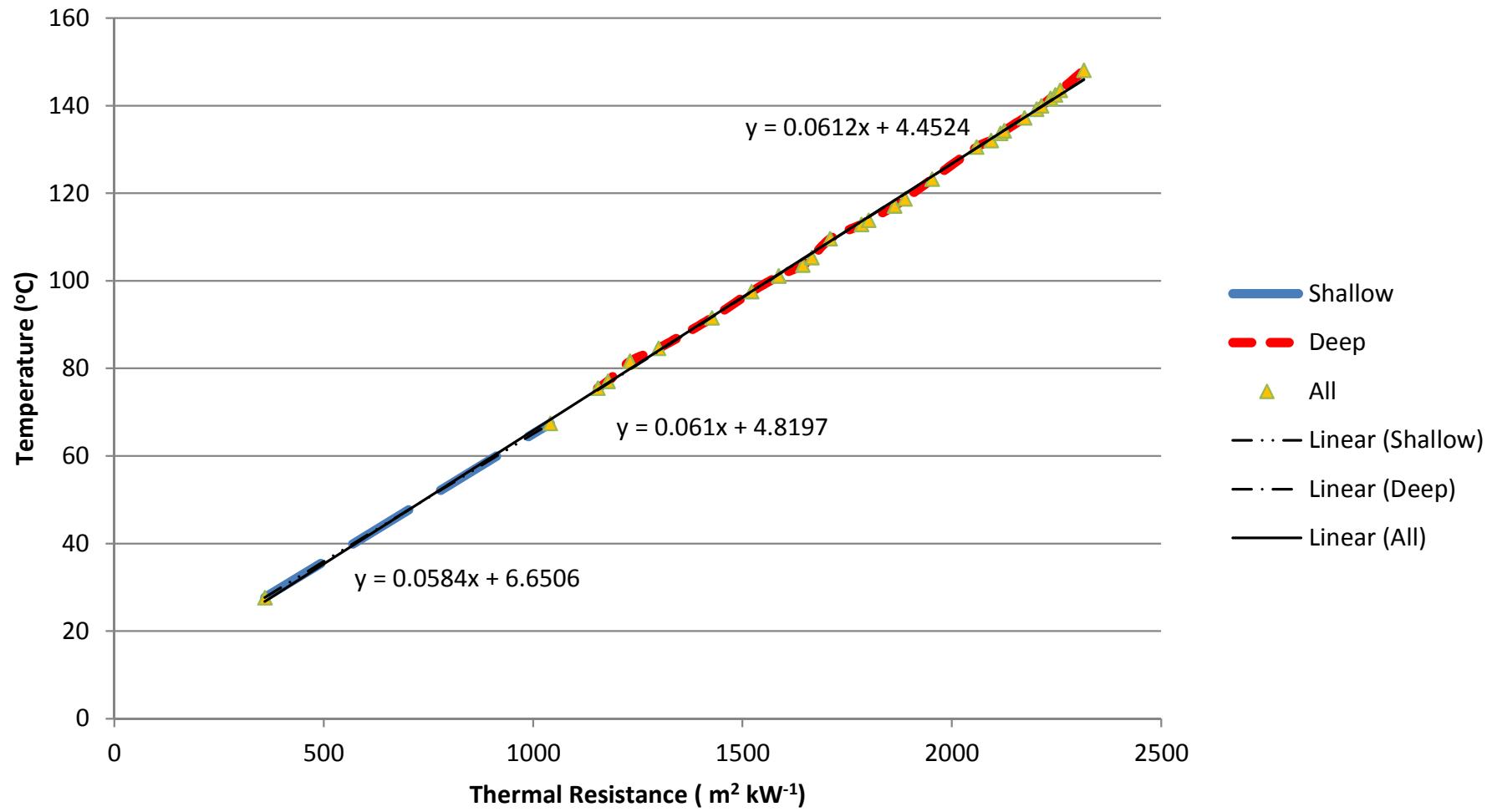
McClean County, ND



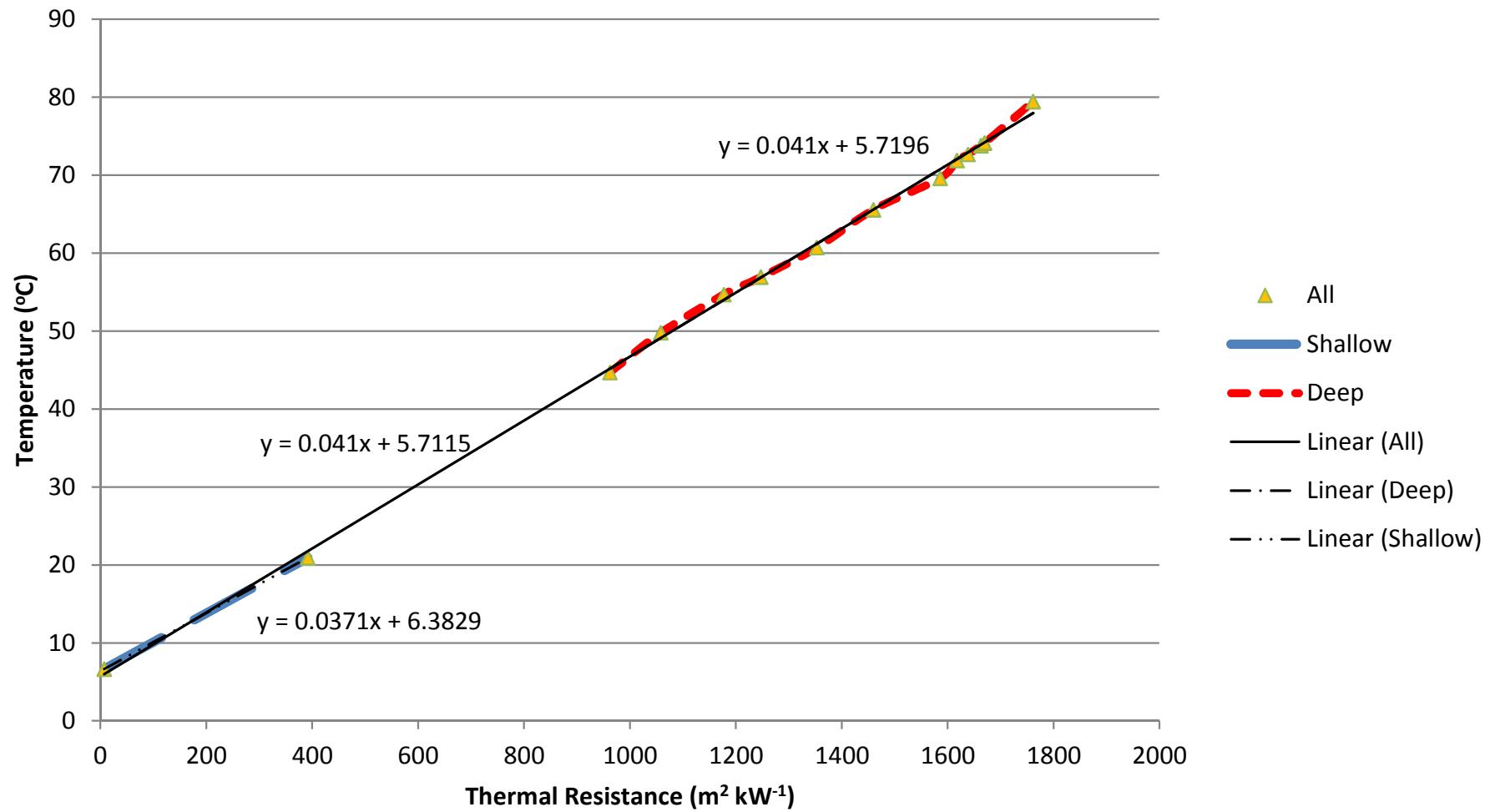
Bullard Method
NDIC 16182 - 2004 JV-P NCDA-7
Williams County, ND



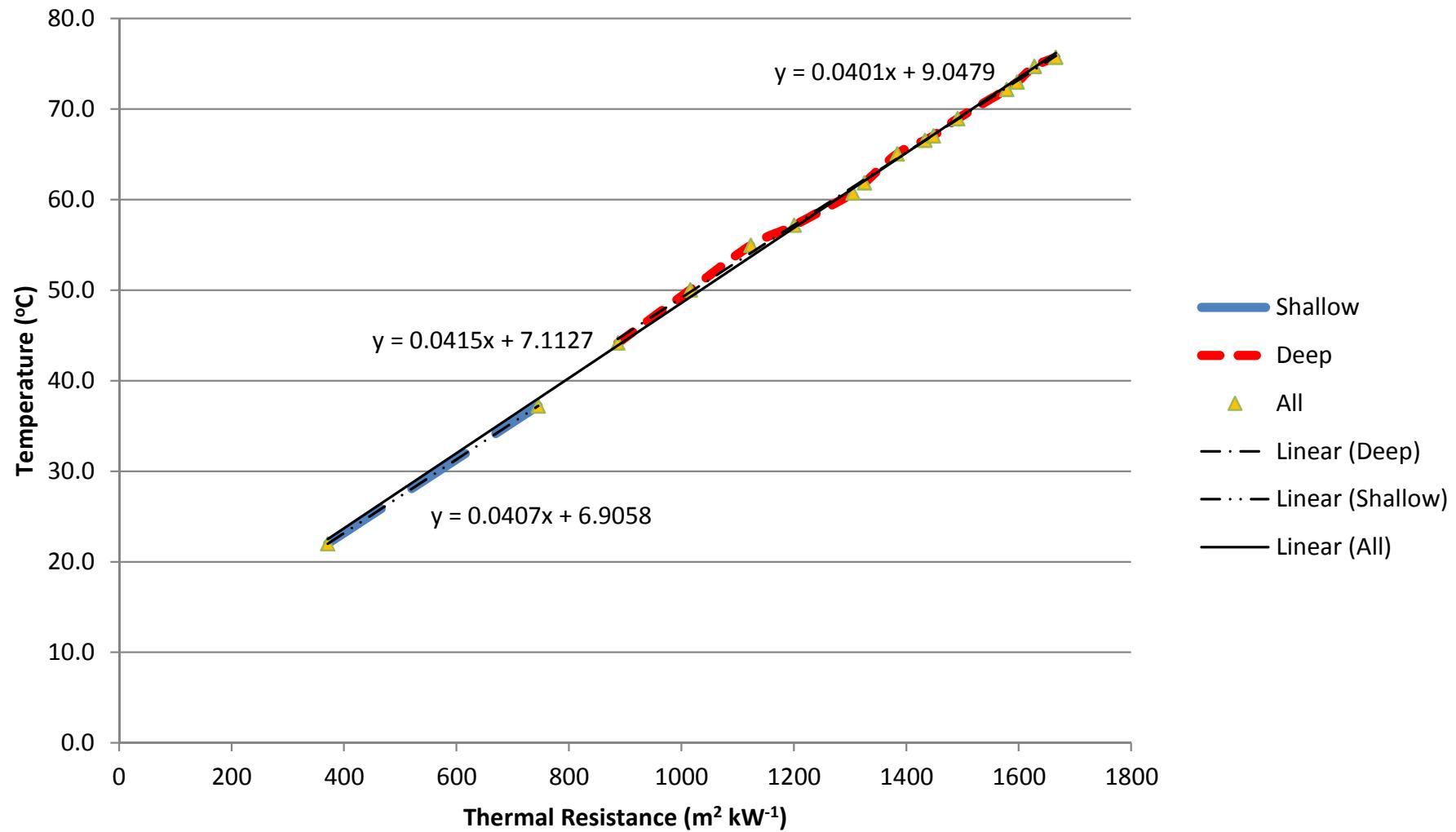
Bullard Method
NDIC 16376 - Vernie Chapin 32-21
McKenzie County, ND



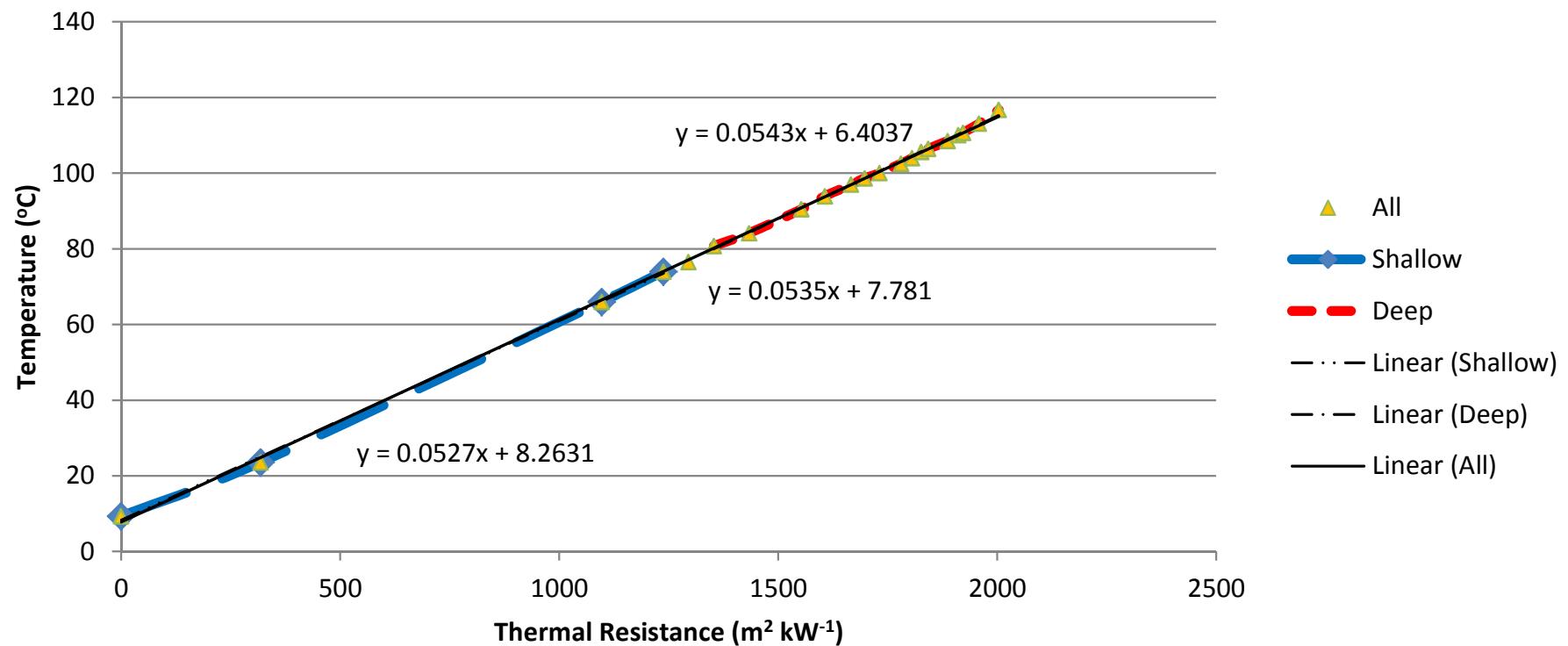
Bullard Method
NDIC 17014 - Edwards 1-33BH
Mountrail County, ND



Bullard Method
NDIC 17043 - St. Andes 151-89-2413H-1
Mountrail County, ND



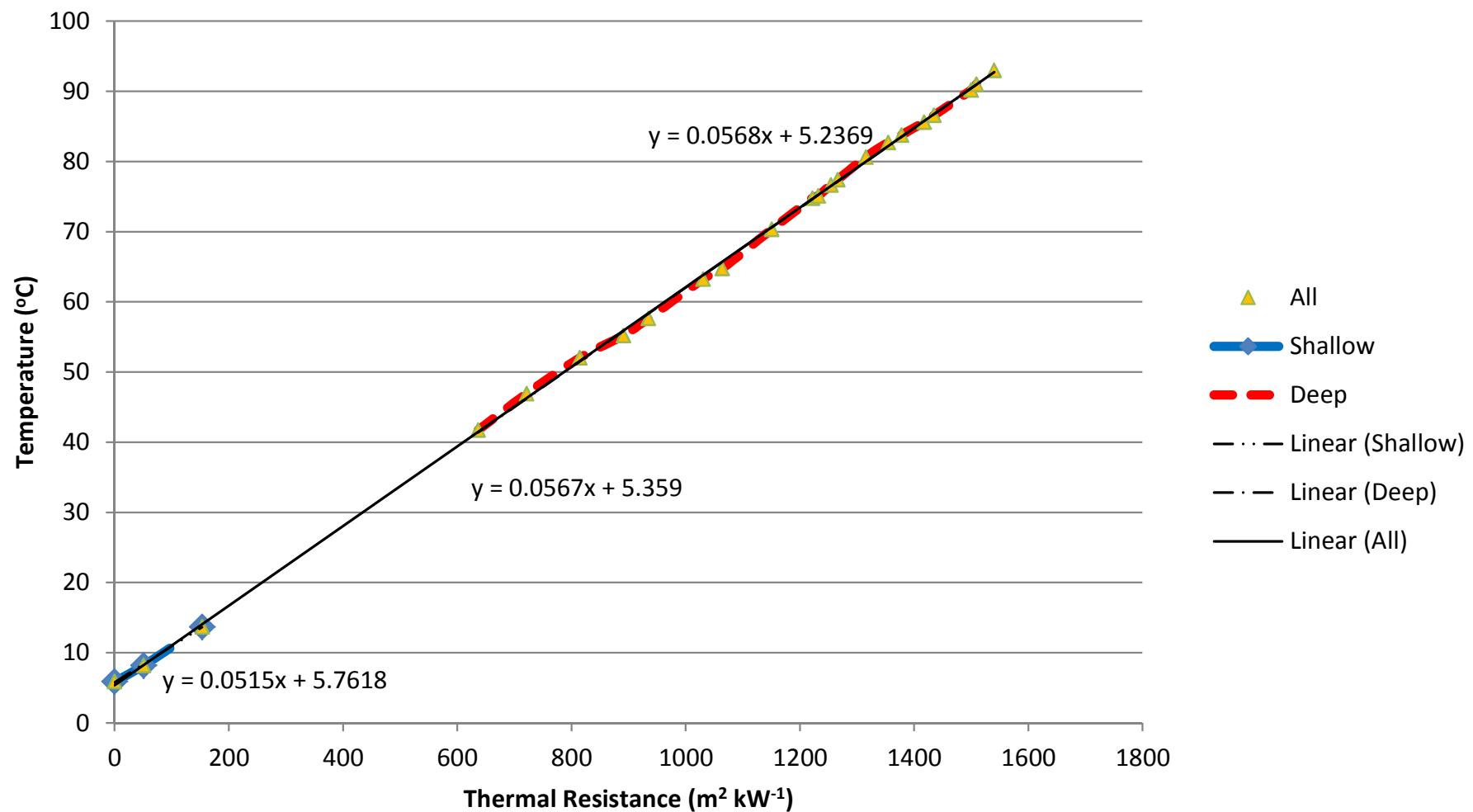
Bullard Method
NDIC 17230 - Roosevelt Federal 2-4H
Billings County, ND



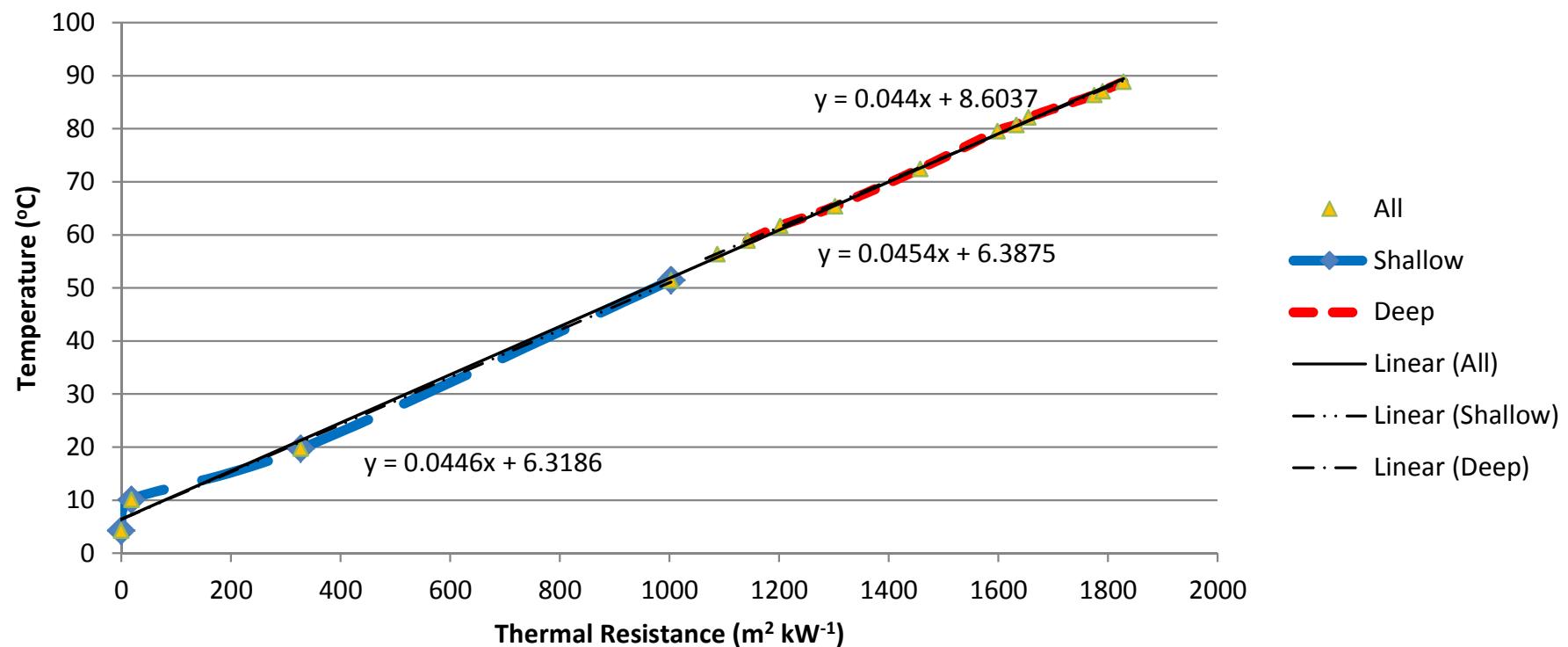
Bullard Method

NDIC 17317 - E-M Emmel 10-3

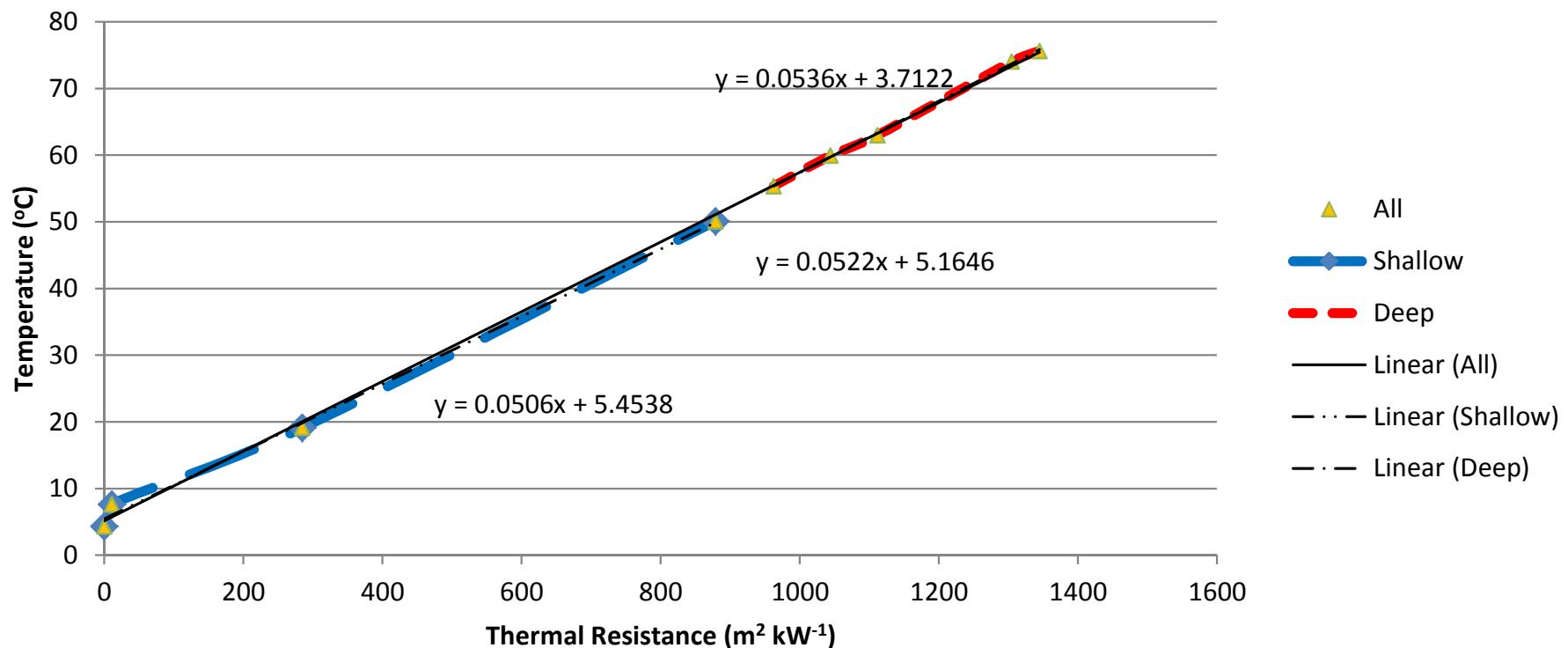
Renville County, ND



Bullard Method
NDIC 3090 - Grenora-Madison Unit 08
Williams County, ND



Bullard Method
NDIC 13725 - JC Woods 26H-1
Burke County, ND



APPENDIX E

SUMMARIES OF HEAT FLOW CALCULATIONS

Summary of Heat Flow Calculations

NDIC 1140

Capa Madison Unit H-205

Williams County, ND

Summary of Heat Flow Calculations

NDIC 2139

NSCU V-706

Bottineau County, ND

Formation	Depth (Z)	Δz	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta Z_i/\lambda$	R _i	λ_{hi}^5	grad _i	Q _{graph} ⁶	Q ₂ ⁷	Q _N ⁸	Q _{Bullard} ⁹	Q _{hi} ¹⁰
	(m)		(°C)														
Foxhills	32.0	9.8	6.7	0.8	1.20	1.72	0.04	0.07	26.92	26.92				28.7	41.1		
Pierre	64.3	19.6	7.5	20.3	1.10	1.62	0.57	0.88	418.13	445.05	0.14	23.90		48.4	71.3	3.5	
Greenhorn	524.3	159.8	27.7	4.1	1.00	1.62	0.09	0.15	80.16	525.22	1.00	42.71		51.5	83.4	42.6	
Mowry	604.4	184.2	31.8	2.7	1.20	1.80	0.08	0.13	50.04	575.25	1.05	43.94		54.4	81.6	46.2	
Inyan Kara	664.5	202.5	34.6	1.7	1.60	2.35	0.14	0.21	48.01	623.26	1.07	44.07		34.7	51.0	47.0	
Swift	741.3	225.9	36.2	5.8	1.20	2.10	0.23	0.43	143.15	766.41	0.97	41.65		40.5	70.8	40.3	
BOH	913.1		42.0									40.10					
					$\Sigma =$	1.16	1.86										
Notes													Average	43.0	66.5	47.5	44
1 - Thermal conductivity derived from graphical method													Wtd Average	46.6	75.6		
2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)													Shallow			48.4	23.2
3 - Weighted average of graphical thermal conductivity													Deep	48		41.3	44.5
4 - Weighted average of Nordeng's thermal conductivity																	
5 - Harmonic mean of thermal conductivity																	
6 - Heat flow derived from graphical method																	
7- Heat flow derived from Equation 1 for each formation																	
8 - Heat Flow derived from Equation 1 and Nordeng's λ																	
9 - Heat flow derived from Bullard's Method																	
10 - Heat flow derived using harmonic mean method																	

Summary of Heat Flow Calculations

NDIC 8005

Sivertson 29-23R1

McKenzie County, ND

Formation	Depth (Z)	ΔZ	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta Z_i/\lambda$	R_i	λ_{hi}^5	grad _i	Q_{graph}^6	Q_2^7	Q_N^8	$Q_{Bullard}^9$	Q_{hi}^{10}
	(m)		(°C)														
FU/HC/FH ¹¹	0.0	490.4	-0.4	28.9	1.40	1.72	0.17	0.21	350.30	350.30				82.5	101.4		
Cretaceous Shale ?	490.4	900.4	28.5	46.9	1.15	1.62	0.26	0.37	782.94	1133.24	0.43	58.93		60.0	84.5	25.5	
Mowry	1390.8	100.3	75.4	5.5	1.20	1.80	0.03	0.05	83.57	1216.81	1.14	54.53		66.1	99.2	62.3	
Inyan Kara	1491.1	136.6	80.9	4.1	1.60	2.35	0.06	0.08	85.34	1302.15	1.15	54.57		47.8	70.3	62.5	
Swift	1627.6	135.3	85.0	5.7	1.50	2.10	0.05	0.07	90.22	1392.37	1.17	52.50		62.7	87.8	61.4	
Rierdon	1763.0	201.5	90.7	6.9	2.00	2.10	0.10	0.11	100.74	1493.11	1.18	51.68		68.2	71.6	61.0	
Spearfish	1964.4	118.9	97.6	2.3	2.40	2.10	0.07	0.06	49.53	1542.64	1.27	49.88		47.2	41.3	63.5	
Minnekahta	2083.3	10.4	99.9	0.2	2.40	3.04	0.01	0.01	4.32	1546.96	1.35	48.15		37.3	47.3	64.8	
Opeche	2093.7	104.2	100.1	2.3	2.20	3.04	0.06	0.08	47.38	1594.34	1.31	47.99		48.8	67.4	63.0	
Broom Creek	2197.9	111.9	102.4	2.3	3.80	3.04	0.11	0.09	29.44	1623.78	1.35	46.77		79.5	63.6	63.3	
Tyler	2309.8	170.4	104.7	7.3	1.60	2.68	0.07	0.12	106.49	1730.27	1.33	45.51		68.3	114.4	60.8	
Kibbey Lime	2480.2	41.1	112.0	0.7	2.70	3.62	0.03	0.04	15.24	1745.51	1.42	45.32		46.3	62.1	64.4	
Madison	2521.3	176.8	112.7	3.2	3.05	3.45	0.14	0.15	57.96	1803.47	1.40	44.86		54.9	62.1	62.7	
Ratcliffe	2698.1	18.6	115.9	0.4	3.05	3.45	0.01	0.02	6.10	1809.56	1.49	43.10		60.1	68.0	64.3	
Last Salt	2716.7	70.4	116.2	1.5	3.05	3.45	0.05	0.06	23.08	1832.65	1.48	42.94		65.0	73.5	63.7	
Frobisher-Alida	2787.1	171.6	117.7	4.1	3.05	3.45	0.13	0.15	56.26	1888.91	1.48	42.39		72.9	82.4	62.6	
Lodgepole	2958.7	264.3	121.8	7.9	2.00	3.45	0.13	0.23	132.13	2021.04	1.46	41.32		60.0	103.4	60.5	
Bakken	3223.0	26.2	129.8	1.1	1.00	4.00	0.01	0.03	26.21	2047.25	1.57	40.39		42.4	169.6	63.6	
Three Forks	3249.2	64.0	130.9	1.9	2.70	4.00	0.04	0.06	23.71	2070.96	1.57	40.41		78.8	116.8	63.4	
Birdbear	3313.2	27.1	132.7	0.6	2.80	4.00	0.02	0.03	9.69	2080.65	1.59	40.19		62.8	89.8	64.0	
Duperow	3340.3	121.0	133.3	2.8	2.60	4.00	0.08	0.12	46.54	2127.19	1.57	40.05		59.3	91.3	62.9	
Souris River	3461.3	83.5	136.1	2.1	2.80	3.09	0.06	0.07	29.83	2157.02	1.60	39.44		70.8	78.1	63.3	
Dawson Bay	3544.8	36.6	138.2	0.9	2.75	3.09	0.03	0.03	13.30	2170.32	1.63	39.11		68.9	77.4	63.9	
Prairie	3581.4	46.0	139.1	0.8	4.00	2.18	0.05	0.03	11.51	2181.82	1.64	38.97		66.1	36.1	64.0	
Winnipegosis	3627.4	125.0	139.9	3.0	2.60	2.83	0.08	0.09	48.06	2229.89	1.63	38.68		62.2	67.7	62.9	
Interlake	3752.4	208.7	142.9	4.35	3.77	3.72	0.19863	0.19599	55.3564	2285.24	1.64	38.19		78.5817	77.5395	62.7091	
BOH	3961.1		147.2														
						$\Sigma =$	2.04	2.53									
Notes													Average	62.2	80.9	61.3	61.5
1 - Thermal conductivity derived from graphical method													Wtd Average	76.2	94.4		
2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)													Shallow			60.0	43.9
3 - Weighted average of graphical thermal conductivity													Deep	61		62.1	63.0
4 - Weighted average of Nordeng's thermal conductivity																	
5 - Harmonic mean of thermal conductivity																	
6 - Heat flow derived from graphical method																	
7 - Heat flow derived from Equation 1 for each formation																	
8 - Heat Flow derived from Equation 1 and Nordeng's λ																	
9 - Heat flow derived from Bullard's Method																	
10 - Heat flow derived using harmonic mean method																	
11 - FU/HC/FH - Fort Union Group/Hell Creek Formation/Fox Hills Formation combined																	

Summary of Heat Flow Calculations

NDIC8706

Berge C-1

McKenzie County, ND

Summary of Heat Flow Calculations

NDIC 9653

Cutlip 1

McKenzie County, ND

Summary of Heat Flow Calculations

NDIC 10103

Iverson State A-1

McKenzie County, ND

Formation	Depth (Z)	ΔZ	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta Z_i/\lambda$	R _i	λ_{hi}^5	grad _i	Q _{graph} ⁶	Q ₂ ⁷	Q _N ⁸	Q _{Bullard} ⁹	Q _{hi} ¹⁰
	(m)		(°C)														
FU/HC/FH ¹¹	27.7	555.7	8.8	19.2	1.40	1.72	0.29	0.36	636.81	636.81				48.3	59.3		
Pierre	583.4	847.3	28.0	37.7	1.40	1.62	0.45	0.52	368.81	1005.62	0.91	36.98		62.3	72.0		33.8
Greenhorn	1430.7	121.3	65.6	7.1	1.20	1.62	0.05	0.07	98.04	1103.67	1.30	40.58		70.6	95.3		52.8
Mowry	1552.0	50.9	72.8	2.4	1.00	1.80	0.02	0.03	47.24	1150.91	1.35	41.96		47.4	85.3		56.6
Newcastle	1602.9	107.9	75.2	5.5	1.00	1.80	0.04	0.07	59.74	1210.65	1.32	42.16		51.3	92.4		55.7
Inyan Kara	1710.8	113.1	80.7	1.7	1.40	2.35	0.06	0.10	33.31	1243.96	1.33	42.44		21.2	35.6		56.6
Swift	1823.9	167.9	82.4	6.4	1.50	2.10	0.10	0.13	145.29	1389.25	1.23	42.78		56.8	79.5		52.6
Rierdon	1991.9	160.6	88.8	5.9	1.50	2.10	0.09	0.13	150.57	1539.82	1.25	40.75		55.1	77.1		50.9
Spearfish	2152.5	107.6	94.7	2.1	1.30	3.04	0.05	0.12	82.53	1622.35	1.33	40.45		25.8	60.3		53.6
Minnehahta	2260.1	10.7	96.8	0.3	1.80	3.04	0.01	0.01	5.93	1628.28	1.39	39.48		44.1	74.4		54.7
Opeche	2270.8	58.8	97.1	1.2	2.40	3.04	0.05	0.07	19.81	1648.09	1.38	39.39		49.2	62.3		54.2
Broom Creek	2329.6	92.4	98.3	2.1	2.80	3.04	0.10	0.11	31.90	1679.98	1.38	38.90		62.5	67.8		53.6
Tyler	2421.9	31.7	100.3	1.7	1.40	2.68	0.02	0.03	35.71	1715.69	1.40	38.31		75.6	144.7		53.7
Big Snowy	2453.6	110.6	102.1	3.3	1.70	3.62	0.07	0.15	66.88	1782.57	1.38	38.47		50.9	108.3		53.0
Kibbey Lime	2564.3	43.0	105.4	0.8	2.30	3.62	0.04	0.06	18.16	1800.72	1.43	38.04		42.2	66.4		54.3
Madison	2607.3	43.2	106.2	0.5	3.10	3.45	0.05	0.06	12.74	1813.47	1.44	37.71		35.9	40.0		54.3
BOH	2650.4		106.7														
					$\Sigma =$	1.49	2.03										
Notes																	
1 - Thermal conductivity derived from graphical method																	
2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)																	
3 - Weighted average of graphical thermal conductivity																	
4 - Weighted average of Nordeng's thermal conductivity																	
5 - Harmonic mean of thermal conductivity																	
6 - Heat flow derived from graphical method																	
7- Heat flow derived from Equation 1 for each formation																	
8 - Heat Flow derived from Equation 1 and Nordeng's λ																	
9 - Heat flow derived from Bullard's Method																	
10 - Heat flow derived using harmonic mean method																	
11- FU/HC/FH - Fort Union Group/Hell Creek Formation/Fox Hills Formation combined																	

Summary of Heat Flow Calculations

NDIC 10278

Mud Buttes 1-36

Bowman County, ND

Summary of Heat Flow Calculations

NDIC 12280

Brandjord 1-20

Bottineau County, ND

Summary of Heat Flow Calculations

NDIC 12363

Astrid Ongstad 14-22

Williams County, ND

Formation	Depth (Z)	ΔZ	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta z_i/\lambda$	R_i	λ_{hi}^5	$grad_i$	Q_{graph}^6	Q_z^7	Q_N^8	$Q_{Bullard}^9$	Q_{hi}^{10}
	(m)			(°C)													
FU/HC/FH ¹¹	20.7	595.0	3.9	26.1	1.30	1.72	0.23	0.31	457.7	457.7				57.1	75.5		
Pierre	615.7	612.3	30.0	28.7	1.10	1.62	0.20	0.30	556.7	1014.3	0.61	43.92		51.6	76.0	26.7	
Greenhorn	1228.0	100.9	58.8	6.3	1.10	1.62	0.03	0.05	91.7	1106.1	1.11	45.45		68.3	100.5	50.5	
Mowry	1328.9	108.5	65.0	5.8	1.10	1.80	0.04	0.06	98.6	1204.7	1.10	46.73		58.7	96.0	51.5	
Inyan Kara	1437.4	131.7	70.8	3.0	1.60	2.35	0.06	0.09	82.3	1287.0	1.12	47.24		36.0	52.9	52.8	
Swift	1569.1	131.4	73.8	6.1	1.20	2.10	0.05	0.08	109.5	1396.5	1.12	45.14		55.6	97.2	50.7	
Reirdon	1700.5	178.0	79.9	6.6	1.50	2.10	0.08	0.11	118.7	1515.1	1.12	45.23		55.4	77.6	50.8	
Spearfish	1878.5	94.2	86.4	2.2	1.60	3.04	0.04	0.09	58.9	1574.0	1.19	44.44		37.2	70.7	53.0	
Opeche	1972.7	60.4	88.6	1.5	1.30	3.04	0.02	0.05	46.4	1620.4	1.22	43.41		32.8	76.7	52.8	
Broom Creek/Amsd	2033.0	22.9	90.2	0.5	2.20	3.04	0.02	0.02	10.4	1630.8	1.25	42.87		46.0	63.5	53.4	
Tyler	2055.9	169.5	90.6	6.8	1.40	2.68	0.07	0.14	121.0	1751.9	1.17	42.62		56.1	107.4	50.0	
Kibbey	2225.3	44.5	97.4	0.9	2.70	3.62	0.04	0.05	16.5	1768.4	1.26	42.43		55.6	74.6	53.4	
Madison Group	2269.8	174.3	98.3	3.3	3.05	3.45	0.16	0.18	57.2	1825.5	1.24	41.99		57.0	64.5	52.2	
Ratcliffe	2444.2	18.9	101.6	0.4	3.05	3.45	0.02	0.02	6.2	1831.7	1.33	40.32		64.6	73.0	53.8	
Base of Last Salt	2463.1	55.5	102.0	1.6	3.05	3.45	0.05	0.06	18.2	1849.9	1.33	40.17		85.2	96.4	53.5	
Frobisher-Alida	2518.6	198.1	103.6	2.3	2.90	3.45	0.17	0.20	68.3	1918.2	1.31	39.90		34.2	40.7	52.4	
Lodgepole	2716.7	200.9	105.9	6.3	2.10	3.45	0.13	0.21	95.6	2013.9	1.35	37.83		65.7	108.0	51.0	
Bakken	2917.5	33.5	112.2	1.4	1.10	4.00	0.01	0.04	30.5	2044.3	1.43	37.38		46.7	169.7	53.3	
Three Forks	2951.1	57.3	113.6	1.7	2.50	4.00	0.04	0.07	22.9	2067.3	1.43	37.44		75.9	121.4	53.4	
Birdbear	3008.4	29.6	115.3	0.7	2.50	4.00	0.02	0.04	11.8	2079.1	1.45	37.30		57.8	92.4	54.0	
Duperow	3037.9	142.3	116.0	3.2	2.20	4.00	0.09	0.17	64.7	2143.8	1.42	37.16		49.5	90.1	52.7	
Souris River	3180.3	83.2	119.2	2.2	2.60	3.09	0.06	0.08	32.0	2175.8	1.46	36.50		67.4	80.0	53.4	
Dawson Bay	3263.5	38.7	121.4	0.4	2.50	3.09	0.03	0.04	15.5	2191.3	1.49	36.23		28.7	35.5	54.0	
Prairie Evaporite	3302.2	49.3	121.8	0.7	4.00	2.18	0.06	0.03	12.3	2203.6	1.50	35.94		58.6	31.9	53.9	
BOH	3351.5		122.6														
					$\Sigma =$	1.73	2.46										
Notes																	
1 - Thermal conductivity derived from graphical method												Average		54.2	82.2	52.7	51.4
2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)												Wtd Average		61.1	87.2		
3 - Weighted average of graphical thermal conductivity												Shallow			51.6	38.6	
4 - Weighted average of Nordeng's thermal conductivity												Deep		52.0		52.9	52.7
5 - Harmonic mean of thermal conductivity																	
6 - Heat flow derived from graphical method																	
7 - Heat flow derived from Equation 1 for each formation																	
8 - Heat Flow derived from Equation 1 and Nordeng's λ																	
9 - Heat flow derived from Bullard's Method																	
10 - Heat flow derived using harmonic mean method																	
11- FU/HC/FH - Fort Union Group/Hell Creek Formation/Fox Hills Formation combined																	

Summary of Heat Flow Calculations

NDIC 13132

Frink 13-15

McClean County, ND

Formation	Depth (Z)	ΔZ	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta Z_i/\lambda$	R _i	λ_{hi}^5	grad _i	Q _{graph} ⁶	Q ₂ ⁷	Q _N ⁸	Q _{Bullard} ⁹	Q _{hi} ¹⁰
	(m)		(°C)														
Till	0.0	44.2	6.1	1.9	1.20	1.72	0.02	0.03	36.83	36.83				51.4	73.7		
FU/HC/FH ¹¹	44.2	460.2	8.0	10.7	1.60	1.72	0.32	0.34	287.66	324.49	0.14	42.85		37.3	40.1		5.8
Pierre	504.4	690.1	18.7	25.6	1.10	1.62	0.33	0.48	627.33	951.82	0.53	25.05		40.9	60.2		13.3
Greenhorn	1194.5	122.8	44.4	6.1	1.00	1.62	0.05	0.09	122.83	1074.65	1.11	32.04		49.4	80.1		35.6
Mowry	1317.3	100.6	50.4	4.1	1.10	1.80	0.05	0.08	91.44	1166.09	1.13	33.66		45.3	74.1		38.0
Inyan Kara	1417.9	127.4	54.6	2.5	1.40	2.35	0.08	0.13	91.00	1257.10	1.13	34.19		27.4	45.9		38.6
Swift	1545.3	133.2	57.1	3.7	1.20	2.10	0.07	0.12	111.00	1368.10	1.13	32.99		33.6	58.8		37.3
Rierdon	1678.5	147.2	60.8	4.2	1.60	2.10	0.10	0.13	92.01	1460.11	1.15	32.59		45.5	59.8		37.5
Spearfish	1825.8	73.2	65.0	1.3	1.60	3.04	0.05	0.10	45.72	1505.83	1.21	32.26		28.2	53.6		39.1
Opeche	1898.9	48.2	66.3	0.9	1.50	3.04	0.03	0.06	32.11	1537.93	1.23	31.69		29.3	59.3		39.1
Broom Creek	1947.1	117.3	67.2	2.1	2.30	3.04	0.12	0.15	51.02	1588.95	1.23	31.39		41.9	55.4		38.5
Tyler	2064.4	45.4	69.3	1.9	1.20	2.68	0.02	0.05	37.85	1626.80	1.27	30.65		49.9	111.5		38.9
Big Snowy	2109.8	75.3	71.2	1.6	1.60	3.62	0.05	0.12	47.05	1673.85	1.26	30.88		34.2	77.4		38.9
Kibbey Lime	2185.1	46.0	72.8	0.7	2.70	3.62	0.05	0.07	17.05	1690.90	1.29	30.55		41.7	55.8		39.5
Madison	2231.1	84.5	73.6	1.1	3.05	3.45	0.11	0.13	27.71	1718.61	1.30	30.24		39.3	44.5		39.3
BOH	2315.7		74.6														59.5
					$\Sigma =$	1.46	2.09										

Notes

1 - Thermal conductivity derived from graphical method

2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)

3 - Weighted average of graphical thermal conductivity

4 - Weighted average of Nordeng's thermal conductivity

5 - Harmonic mean of thermal conductivity

6 - Heat flow derived from graphical method

7 - Heat flow derived from Equation 1 for each formation

8 - Heat Flow derived from Equation 1 and Nordeng's λ

9 - Heat flow derived from Bullard's Method

10 - Heat flow derived using harmonic mean method

11- FU/HC/FH - Fort Union Group/Hell Creek Formation/Fox Hills Formation combined

Average

39.7

63.4

39.9

34.2

Wtd Average

43.1

61.8

Shallow

38.1

13.3

Deep

40

38.3

38.4

Summary of Heat Flow Calculations

NDIC 13666

Rieder 1-9 SWD

Williams County, ND

Summary of Heat Flow Calculations

NDIC 15137

Holte 6-21

Burke County, ND

Formation	Depth (Z)	ΔZ	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta Z_i/\lambda$	R_i	λ_{hi}^5	grad _i	Q_{graph}^6	Q_2^7	Q_N^8	$Q_{Bullard}^9$	Q_{hi}^{10}
	(m)			(°C)													
FU/HC/FH ¹¹	6.7	465.7	3.7	20.8	1.60	1.72	0.24	0.26	388.11	388.11				51.1	73.3		
Pierre	472.4	550.5	24.5	25.9	1.20	1.62	0.21	0.29	366.98	755.09	0.70	42.62		72.5	78.4	28.8	
Niobrara	1022.9	114.6	50.3	7.2	1.10	1.62	0.04	0.06	143.26	898.35	1.09	45.49		35.6	72.0	45.0	
Greenhorn	1137.5	84.1	57.5	5.6	1.00	1.62	0.03	0.04	70.10	968.45	1.20	45.31		117.0	157.9	50.6	
Mowry	1221.6	37.2	63.1	1.9	1.10	1.80	0.01	0.02	41.32	1009.77	1.25	48.92		46.5	93.0	56.4	
Newcastle	1258.8	61.3	65.0	3.4	1.00	1.80	0.02	0.04	55.70	1065.46	1.21	49.01		62.6	102.5	55.3	
Inyan Kara	1320.1	103.0	68.4	3.2	1.50	2.35	0.05	0.08	64.39	1129.85	1.19	49.38		48.1	70.7	55.3	
Swift	1423.1	128.3	71.6	5.8	1.90	2.10	0.08	0.09	53.47	1183.32	1.21	47.97		108.7	95.1	55.4	
Rierdon	1551.4	187.1	77.4	7.5	1.40	2.10	0.08	0.13	74.86	1258.18	1.18	47.75		94.0	78.9	56.6	
Spearfish	1738.6	132.6	84.9	3.2	2.10	3.04	0.09	0.13	88.39	1346.57	1.27	46.65		40.7	82.4	58.1	
Kibbey	1871.2	54.9	88.1	1.3	2.20	3.64	0.04	0.06	30.48	1377.05	1.34	45.26		41.4	83.7	59.4	
Madison	1926.0	99.4	89.3	2.0	3.10	3.45	0.10	0.11	32.58	1409.63	1.35	44.63		62.2	70.4	58.9	
Ratcliffe	2025.4	18.0	91.3	0.4	2.60	3.45	0.02	0.02	7.49	1417.12	1.41	43.43		51.9	74.6	60.0	
Last Salt	2043.4	61.6	91.7	1.4	2.60	3.45	0.05	0.07	18.66	1435.78	1.40	43.24		76.2	79.7	59.5	
Frobisher	2104.9	171.3	93.2	4.5	2.80	3.45	0.15	0.19	47.58	1483.36	1.38	42.65		94.6	90.6	58.6	
Lodgepole	2276.2	178.3	97.7	5.0	2.00	3.45	0.11	0.20	50.95	1534.31	1.41	41.41		97.2	95.8	59.5	
Bakken	2454.6	30.8	102.6	1.3	1.20	4.00	0.01	0.04	30.78	1565.09	1.50	40.42		41.9	167.5	61.4	
Three Forks	2485.3	64.6	103.9	2.0	2.00	4.00	0.04	0.08	26.92	1592.02	1.49	40.44		75.5	125.9	61.2	
Birdbear	2550.0	29.9	105.9	0.8	2.40	4.00	0.02	0.04	19.91	1611.93	1.52	40.21		42.1	112.3	61.7	
Duperow	2579.8	146.6	106.7	3.5	2.90	4.00	0.14	0.19	43.12	1655.05	1.49	40.07		81.4	95.8	60.6	
Souris River	2726.4	103.3	110.3	2.4	2.80	3.09	0.09	0.10	35.63	1690.68	1.54	39.20		67.5	71.9	61.4	
Dawson Bay	2829.8	46.6	112.7	0.9	2.30	3.09	0.03	0.05	21.20	1711.88	1.58	38.62		42.2	59.3	62.0	
Prairie Evaporite	2876.4	173.1	113.6	2.7	3.60	2.18	0.20	0.12	41.22	1753.10	1.57	38.30		66.4	34.5	61.1	
Winnepegosis	3049.5	43.0	116.3	1.0	2.50	2.83	0.03	0.04	15.92	1769.02	1.64	37.02		61.4	64.4	62.1	
Interlake	3092.5	15.2	117.3	0.3	2.70	3.72	0.01	0.02	5.06	1774.07	1.66	36.82		67.0	83.1	62.4	
Bottom of Well	3107.7		117.6		3	3.72					1.67	36.75					
					$\Sigma =$	1.92	2.45										
Notes																	
1 - Thermal conductivity derived from graphical method																	
2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)																	
3 - Weighted average of graphical thermal conductivity																	
4 - Weighted average of Nordeng's thermal conductivity																	
5 - Harmonic mean of thermal conductivity																	
6 - Heat flow derived from graphical method																	
7 - Heat flow derived from Equation 1 for each formation																	
8 - Heat Flow derived from Equation 1 and Nordeng's λ																	
9 - Heat flow derived from Bullard's Method																	
10 - Heat flow derived using harmonic mean method																	
11 - FU/HC/FH - Fort Union Group/Hell Creek Formation/Fox Hills Formation combined																	
Average																	
Wtd Average																	
Shallow																	
Deep																	

Summary of Heat Flow Calculations

NDIC 15593

FHMU K-810

Billings County, ND

Summary of Heat Flow Calculations

NDIC 15875

Ann 1

McKenzie County, ND

Formation	Depth (Z)	ΔZ	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta z_i/\lambda$	R _i	λ_{hi}^5	grad _i	Q_{graph}^6	Q ₂ ⁷	Q _N ⁸	Q _{Bullard} ⁹	Q _{hi} ¹⁰
	(m)		(°C)														
Till	0.0	2.4	9.1	0.1	1.20	1.72	0.00	0.00	2.03	2.03				39.4	56.4		
FU/HC/FH ¹¹	2.4	606.9	9.2	21.4	1.40	1.72	0.27	0.33	433.47	435.50	0.01	32.81		49.3	60.6		0.2
Pierre	609.3	864.7	30.6	41.5	1.10	1.62	0.30	0.45	786.11	1221.61	0.50	35.24		52.7	77.7		17.6
Greenhorn	1474.0	121.9	72.1	7.4	1.10	1.62	0.04	0.06	110.84	1332.44	1.11	42.69		66.5	97.9		47.2
Mowry	1595.9	48.5	79.4	2.3	1.00	1.80	0.02	0.03	48.46	1380.91	1.16	44.05		47.5	85.4		50.9
Newcastle	1644.4	83.8	81.7	4.2	1.20	1.80	0.03	0.05	69.85	1450.76	1.13	44.15		59.4	89.1		50.0
Inyan Kara	1728.2	125.0	85.9	3.1	1.40	2.35	0.06	0.09	89.26	1540.02	1.12	44.41		34.8	58.5		49.8
Swift	1853.2	147.8	89.0	6.0	1.40	2.10	0.07	0.10	105.59	1645.61	1.13	43.09		57.0	85.5		48.5
Rierdon	2001.0	172.2	95.0	5.9	1.60	2.10	0.09	0.12	107.63	1753.24	1.14	42.92		55.0	72.2		49.0
Spearfish	2173.2	140.5	100.9	2.7	1.80	3.04	0.08	0.14	78.06	1831.31	1.19	42.24		34.1	57.5		50.1
Minnekahta/Opech	2313.7	113.4	103.6	2.2	2.60	3.04	0.09	0.11	43.61	1874.92	1.23	40.83		50.0	58.4		50.4
Broom Creek	2427.1	61.9	105.8	1.4	2.40	3.04	0.05	0.06	25.78	1900.70	1.28	39.82		53.1	67.3		50.8
Tyler	2489.0	61.9	107.2	3.6	1.20	2.68	0.02	0.05	51.56	1952.26	1.27	39.38		69.2	154.6		50.2
Big Snowy	2550.9	106.1	110.7	3.0	1.50	3.62	0.05	0.12	70.71	2022.97	1.26	39.82		43.0	103.7		50.2
Kibbey Lime	2656.9	55.2	113.8	1.0	2.70	3.62	0.05	0.06	20.43	2043.41	1.30	39.38		49.9	66.9		51.2
Madison	2712.1	192.6	114.8	3.1	3.05	3.45	0.19	0.21	63.16	2106.56	1.29	38.95		49.7	56.2		50.1
Ratcliffe	2904.7	65.8	117.9	1.5	3.05	3.45	0.06	0.07	21.59	2128.15	1.36	37.45		68.1	77.0		51.1
Frobisher	2970.6	168.0	119.4	3.7	3.05	3.45	0.16	0.18	55.08	2183.24	1.36	37.11		66.8	75.6		50.5
Bottom of Well	3138.6		123.1														
					$\Sigma =$	1.63	2.24										
Notes																	
1 - Thermal conductivity derived from graphical method																	Average
2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)																	52.5
3 - Weighted average of graphical thermal conductivity																	77.8
4 - Weighted average of Nordeng's thermal conductivity																	51.9
5 - Harmonic mean of thermal conductivity																	45.2
6 - Heat flow derived from graphical method																	59.3
7 - Heat flow derived from Equation 1 for each formation																	81.3
8 - Heat Flow derived from Equation 1 and Nordeng's λ																	49.3
9 - Heat flow derived from Bullard's Method																	17.6
10 - Heat flow derived using harmonic mean method																	50.9
11 - FU/HC/FH - Fort Union Group/Hell Creek Formation/Fox Hills Formation combined																	50.0

Summary of Heat Flow Calculations

NDIC 16160

Nelson 1-11H

McClean County, ND

Formation	Depth (Z)	ΔZ	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta z_i/\lambda$	R _i	λ_{hi}^5	grad _i	Q_{graph}^6	Q_2^7	Q_N^8	$Q_{Bullard}^9$	Q_{hi}^{10}
	(m)		(°C)														
Till	0.0	31.1	5.9	1.1	1.10	1.72	0.01	0.02	28.26	28.26				370.4	579.2		
FU/HC/FH ¹¹	31.1	590.7	6.9	20.2	1.60	1.72	0.37	0.40	369.19	397.45	0.08	325.51		29.2	31.4		25.5
Pierre	621.8	709.6	27.1	34.0	1.30	1.62	0.36	0.45	545.83	943.28	0.66	34.16		62.2	77.5		22.5
Greenhorn	1331.4	98.1	61.1	6.3	1.00	1.62	0.04	0.06	98.15	1041.42	1.28	41.45		64.0	103.7		53.0
Mowry	1429.5	53.9	67.4	2.7	1.10	1.80	0.02	0.04	49.05	1090.47	1.31	43.00		55.5	90.8		56.4
Newcastle	1483.5	79.2	70.1	3.8	1.30	1.80	0.04	0.06	60.96	1151.43	1.29	43.27		62.2	86.1		55.7
Inyan Kara	1562.7	84.1	73.9	2.4	1.40	2.35	0.05	0.08	60.09	1211.52	1.29	43.50		40.6	68.2		56.1
Swift	1646.8	154.2	76.3	6.4	1.60	2.10	0.10	0.13	96.39	1307.91	1.26	42.76		66.7	87.6		53.8
Rierdon	1801.1	141.1	82.7	5.0	1.80	2.10	0.10	0.12	78.40	1386.31	1.30	42.67		63.5	74.1		55.4
Spearfish	1942.2	128.3	87.7	3.3	1.70	3.04	0.08	0.15	75.48	1461.80	1.33	42.13		43.9	78.4		56.0
Tyler	2070.5	146.3	91.0	5.3	2.20	2.68	0.13	0.15	66.50	1528.30	1.35	41.12		80.3	97.8		55.7
Kibbey Lime	2216.8	62.2	96.4	1.1	2.00	3.62	0.05	0.09	31.09	1559.39	1.42	40.82		34.1	61.7		58.0
Madison	2279.0	130.5	97.4	2.4	3.30	3.45	0.17	0.18	39.53	1598.92	1.43	40.17		61.2	64.0		57.3
Ratcliffe	2409.4	79.2	99.8	1.8	3.00	3.45	0.09	0.11	26.42	1625.33	1.48	39.00		66.6	76.6		57.8
Frobisher	2488.7	80.7	101.6	1.8	3.30	3.45	0.10	0.11	24.45	1649.78	1.51	38.46		74.4	77.8		58.0
Bottom of Well	2569.4		103.4		3.30												
					$\Sigma =$	1.70	2.12										
Notes																	
1 - Thermal conductivity derived from graphical method																	Average
2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)																	78.3
3 - Weighted average of graphical thermal conductivity																	110.3
4 - Weighted average of Nordeng's thermal conductivity																	56.2
5 - Harmonic mean of thermal conductivity																	51.5
6 - Heat flow derived from graphical method																	
7 - Heat flow derived from Equation 1 for each formation																	
8 - Heat Flow derived from Equation 1 and Nordeng's λ																	
9 - Heat flow derived from Bullard's Method																	
10 - Heat flow derived using harmonic mean method																	
11 - FU/HC/FH - Fort Union Group/Hell Creek Formation/Fox Hills Formation combined																	

Summary of Heat Flow Calculations

NDIC 16182

NDCA7

Williams County, ND

Summary of Heat Flow Calculations

NDIC 16376

Vernie Chapin 32-21
McKenzie County, ND

Formation	Depth (Z)	ΔZ	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta Z_i / \lambda$	R_i	λ_{hi}^5	grad_i^6	Q_{graph}^6	Q_2^7	Q_N^8	Q_{Bullard}^9	Q_{hi}^{10}
	(m)		(°C)														
FU/HC/FH ¹¹	0.0	503.2	5.2	22.5	1.40	1.72	0.18	0.22	359.45	359.45			62.5	76.8			
Pierre	503.2	783.6	27.6	39.8	1.15	1.62	0.23	0.32	681.43	1040.87	0.48	44.65	58.4	82.3		21.6	
Greenhorn	1286.9	125.0	67.4	8.1	1.10	1.62	0.03	0.05	113.61	1154.48	1.11	48.38	71.2	104.8		53.9	
Mowry	1411.8	29.0	75.5	1.6	1.20	1.80	0.01	0.01	24.13	1178.61	1.20	49.82	64.7	97.0		59.7	
Newcastle	1440.8	79.9	77.1	4.5	1.50	1.80	0.03	0.04	53.24	1231.85	1.17	49.90	85.3	102.3		58.4	
Inyan Kara	1520.6	107.9	81.6	3.0	1.60	2.35	0.04	0.06	67.44	1299.29	1.17	50.27	43.9	64.5		58.8	
Swift	1628.5	179.2	84.6	7.0	1.40	2.10	0.06	0.10	128.02	1427.30	1.14	48.76	54.5	81.8		55.6	
Rierdon	1807.8	151.5	91.6	6.0	1.60	2.10	0.06	0.08	94.68	1521.98	1.19	47.78	63.1	82.8		56.8	
Spearfish	1959.3	155.8	97.5	3.6	2.40	3.04	0.09	0.12	64.90	1586.88	1.23	47.14	54.7	69.3		58.2	
Opeche	2115.0	126.5	101.1	2.6	2.20	3.04	0.07	0.10	57.50	1644.37	1.29	45.34	44.8	62.0		58.3	
Amsden	2241.5	82.6	103.7	1.7	3.80	3.04	0.08	0.06	21.74	1666.11	1.35	43.93	76.4	61.1		59.1	
Tyler	2324.1	69.2	105.3	4.3	1.60	2.68	0.03	0.05	43.24	1709.35	1.36	43.09	99.2	166.1		58.6	
Big Snowy	2393.3	104.5	109.6	3.3	1.40	3.62	0.04	0.10	74.68	1784.03	1.34	43.63	43.7	112.9		58.5	
Kibbey	2497.8	47.2	112.9	1.0	2.70	3.62	0.03	0.04	17.50	1801.53	1.39	43.11	55.9	74.9		59.8	
Madison	2545.1	187.8	113.8	3.3	3.05	3.45	0.14	0.16	61.56	1863.09	1.37	42.70	53.0	59.9		58.3	
Ratcliffe	2732.8	75.3	117.1	1.6	3.05	3.45	0.06	0.07	24.68	1887.77	1.45	40.96	65.7	74.3		59.3	
Frobisher	2808.1	183.2	118.7	4.5	2.80	3.45	0.13	0.16	65.42	1953.19	1.44	40.44	68.9	84.9		58.1	
Lodgepole	2991.3	243.8	123.2	7.3	2.30	3.45	0.14	0.21	106.02	2059.21	1.45	39.47	69.1	103.6		57.3	
Bakken	3235.1	35.1	130.6	1.5	1.00	4.00	0.01	0.04	35.05	2094.26	1.54	38.75	43.4	173.7		59.9	
Three Forks	3270.2	59.4	132.1	1.6	2.70	4.00	0.04	0.06	22.01	2116.28	1.55	38.80	74.4	110.3		60.0	
Birdbear	3329.6	25.3	133.7	0.6	2.80	4.00	0.02	0.03	9.04	2125.31	1.57	38.60	63.9	91.4		60.5	
Duperow	3354.9	125.9	134.3	3.0	2.60	4.00	0.08	0.13	48.42	2173.73	1.54	38.49	61.4	94.4		59.4	
Souris River	3480.8	79.6	137.3	2.0	2.80	3.09	0.06	0.06	28.41	2202.14	1.58	37.95	68.6	75.7		60.0	
Dawson Bay	3560.4	32.0	139.2	0.8	2.75	3.09	0.02	0.02	11.64	2213.78	1.61	37.65	65.4	73.5		60.5	
Prairie	3592.4	86.9	140.0	1.7	4.00	2.18	0.09	0.05	21.72	2235.50	1.61	37.52	76.7	41.8		60.3	
Winnipegosis	3679.2	34.4	141.6	0.9	2.99	2.83	0.03	0.02	11.52	2247.01	1.64	37.09	75.7	71.7		60.7	
Ashern	3713.7	36.3	142.5	1.0	2.99	2.83	0.03	0.03	12.13	2259.15	1.64	36.98	83.8	79.3		60.8	
Interlake	3750.0	211.2	143.5	4.6	3.77	3.72	0.20	0.20	56.03	2315.17	1.62	36.90	81.2	80.1		59.8	
BOH	3961.2		148.1														
					$\Sigma =$	2.03	2.58										
Notes												Average	65.3	87.6	61	57.5	
1 - Thermal conductivity derived from graphical method												Wtd Average	73.3	93.0			
2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)												Shallow		58.4	37.8		
3 - Weighted average of graphical thermal conductivity												Deep	60		60.3	59.1	
4 - Weighted average of Nordeng's thermal conductivity																	
5 - Harmonic mean of thermal conductivity																	
6 - Heat flow derived from graphical method																	
7- Heat flow derived from Equation 1 for each formation																	
8 - Heat Flow derived from Equation 1 and Nordengs λ																	
9 - Heat flow derived from Bullard's Method																	
10 - Heat flow derived using harmonic mean method																	
11- FU/HC/FH - Fort Union Group/Hell Creek Formation/Fox Hills Formation combined																	

Summary of Heat Flow Calculations

NDIC 17014

Edwards 1-33BH

Mountrail County, ND

Formation	Depth (Z)	ΔZ	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta Z_i/\lambda$	R _i	λ_{hi}^5	grad _i	Q_{graph}^6	Q_2^7	Q_N^8	$Q_{Bullard}^9$	Q_{hi}^{10}
	(m)		(°C)														
Till	0.0	7.6	6.6	0.2	1.10	1.72	0.00	0.01	6.93	6.93				102.5	160.3		
FU/HC/FH ¹¹	7.6	538.6	6.8	14.2	1.40	1.72	0.31	0.38	384.70	391.63	0.02	93.18		37.1	45.6	1.8	
Pierre	546.2	599.2	20.9	23.8	1.05	1.62	0.26	0.40	570.70	962.33	0.57	27.44		41.7	64.3		
Greenhorn	1145.4	96.0	44.7	5.1	1.00	1.62	0.04	0.06	96.01	1058.34	1.08	33.84		53.1	86.1	36.6	
Mowry	1241.5	107.0	49.8	4.9	0.90	1.80	0.04	0.08	118.87	1177.21	1.05	35.33		41.2	82.4	37.3	
Inyan Kara	1348.4	97.5	54.7	2.2	1.40	2.35	0.06	0.09	69.67	1246.88	1.08	36.16		32.0	53.7	39.1	
Swift	1446.0	127.4	56.9	3.8	1.20	2.10	0.06	0.11	106.17	1353.05	1.07	35.26		35.7	62.5	37.7	
Rierdon	1573.4	171.0	60.7	4.9	1.60	2.10	0.11	0.15	106.87	1459.93	1.08	34.82		45.5	59.7	37.5	
Spearfish	1744.4	176.5	65.6	4.0	1.40	3.04	0.10	0.22	126.06	1585.98	1.10	34.19		32.0	69.4	37.6	
Broom Creek	1920.8	95.7	69.6	2.3	3.00	2.68	0.12	0.11	31.90	1617.88	1.19	33.15		71.8	64.1	39.4	
Kibbey	2016.6	49.1	71.9	0.8	2.40	3.62	0.05	0.07	20.45	1638.33	1.23	32.71		38.6	58.3	40.3	
Madison	2065.6	71.9	72.7	1.1	2.90	3.45	0.09	0.10	24.80	1663.14	1.24	32.31		44.3	52.8	40.1	
Ratcliffe	2137.6	20.1	73.8	0.3	3.00	3.45	0.02	0.03	6.71	1669.84	1.28	31.74		50.7	58.3	40.6	
Frobisher	2157.7	279.7	74.1	5.3	3.05	3.45	0.35	0.40	91.70	1761.54	1.22	31.60		58.0	65.6	38.7	
Bottom of Well	2437.4		79.4		3.05												
					$\Sigma =$	1.61	2.20										
Notes																	
1 - Thermal conductivity derived from graphical method																	
2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)																	
3 - Weighted average of graphical thermal conductivity																	
4 - Weighted average of Nordeng's thermal conductivity																	
5 - Harmonic mean of thermal conductivity																	
6 - Heat flow derived from graphical method																	
7- Heat flow derived from Equation 1 for each formation																	
8 - Heat Flow derived from Equation 1 and Nordeng's λ																	
9 - Heat flow derived from Bullard's Method																	
10 - Heat flow derived using harmonic mean method																	
11- FU/HC/FH - Fort Union Group/Hell Creek Formation/Fox Hills Formation combined																	

Summary of Heat Flow Calculations

NDIC 17043

St. Andes 151-89-2413H-1

Mountrail County, ND

Formation	Depth (Z)	ΔZ	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta Z_i/\lambda$	R _i	λ_{hi}^5	grad _i	Q_{graph}^6	Q_2^7	Q_N^8	$Q_{Bullard}^9$	Q_{hi}^{10}
	(m)		(°C)														
FU/HC/FH ¹¹	15.8	593.8	6.5	15.5	1.60	1.72	0.40	0.43	371.09	371.09				41.8	44.9		
Pierre	609.6	430.4	22.0	15.2	1.15	1.62	0.21	0.29	374.24	745.34	0.82	26.11		40.7	57.3	21.4	
Niobrara	1040.0	156.1	37.2	6.9	1.10	1.62	0.07	0.11	141.87	887.21	1.17	30.00		48.9	72.1	35.2	
Greenhorn	1196.0	116.1	44.2	5.9	0.90	1.62	0.04	0.08	129.03	1016.24	1.18	31.92		45.6	82.2	37.6	
Mowry	1312.2	107.3	50.1	4.9	1.00	1.80	0.04	0.08	107.29	1123.53	1.17	33.60		45.6	82.0	39.2	
Inyan Kara	1419.5	115.5	54.9	2.2	1.50	2.35	0.07	0.11	77.01	1200.54	1.18	34.51		28.9	45.2	40.8	
Swift	1535.0	125.6	57.2	3.6	1.20	2.10	0.06	0.11	104.65	1305.19	1.18	33.35		34.0	59.5	39.2	
Rierdon	1660.6	30.5	60.7	1.1	1.50	2.10	0.02	0.03	20.32	1325.51	1.25	32.97		54.7	76.6	41.3	
Piper	1691.0	122.2	61.8	3.2	2.10	2.10	0.11	0.11	58.20	1383.71	1.22	33.03		55.4	55.4	40.4	
Spearfish	1813.3	78.9	65.1	1.5	1.60	3.04	0.05	0.10	49.34	1433.05	1.27	32.58		30.4	57.8	41.2	
Opeche	1892.2	24.7	66.6	0.5	1.60	3.04	0.02	0.03	15.43	1448.48	1.31	32.01		32.4	61.6	41.8	
Amsden	1916.9	103.3	67.1	1.9	2.40	3.04	0.10	0.13	43.05	1491.53	1.29	31.85		43.9	55.6	40.9	
Tyler	2020.2	121.6	68.9	3.2	1.40	2.68	0.07	0.14	86.87	1578.40	1.28	31.15		37.1	71.0	39.9	
Kibbey Lime	2141.8	51.2	72.2	0.8	2.70	3.62	0.06	0.08	18.97	1597.37	1.34	30.89		43.9	58.9	41.4	
Madison	2193.0	93.0	73.0	1.7	3.05	3.45	0.12	0.13	30.48	1627.85	1.35	30.54		56.5	63.9	41.1	
Ratcliffe	2317.4	116.1	74.7	1.0	3.05	3.45	0.15	0.17	38.08	1665.92	1.37	30.05		26.3	29.7	41.2	
Bottom of Well	2402.1		75.7														
					$\Sigma =$	1.59	2.11										
Notes																	
1 - Thermal conductivity derived from graphical method																	
2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)																	
3 - Weighted average of graphical thermal conductivity																	
4 - Weighted average of Nordeng's thermal conductivity																	
5 - Harmonic mean of thermal conductivity																	
6 - Heat flow derived from graphical method																	
7 - Heat flow derived from Equation 1 for each formation																	
8 - Heat Flow derived from Equation 1 and Nordeng's λ																	
9 - Heat flow derived from Bullard's Method																	
10 - Heat flow derived using harmonic mean method																	
11 - FU/HC/FH - Fort Union Group/Hell Creek Formation/Fox Hills Formation combined																	
												Average					
												Wtd Average					
												Shallow					
												Deep					
												42					

Summary of Heat Flow Calculations

NDIC 17230

Roosevelt Federal 2-4H

Billings County, ND

Formation	Depth (Z)	ΔZ	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta Z_i/\lambda$	R _i	λ_{hi}^5	grad _i	Q _{graph} ⁶	Q ₂ ⁷	Q _N ⁸	Q _{Bullard} ⁹	Q _{hi} ¹⁰
	(m)		(°C)														
FU/HC/FH ¹¹	6.7	413.3	9.4	14.2	1.30	1.72	0.18	0.28	317.93	317.93				44.8	59.2		
Pierre	420.0	896.4	23.6	42.4	1.15	1.62	0.34	0.48	779.49	1097.42	0.38	34.43		54.4	76.7		13.2
Greenhorn	1316.4	140.5	66.0	8.0	1.00	1.62	0.05	0.07	140.51	1237.94	1.06	43.27		56.8	92.0		46.0
Mowry	1456.9	62.8	74.0	2.5	1.10	1.80	0.02	0.04	57.08	1295.02	1.13	44.58		44.3	72.5		50.2
Newcastle	1519.7	87.2	76.5	4.2	1.50	1.80	0.04	0.05	58.12	1353.13	1.12	44.40		72.8	87.3		49.9
Inyan Kara	1606.9	128.9	80.8	3.4	1.60	2.35	0.07	0.10	80.58	1433.71	1.12	44.63		42.1	61.8		50.0
Swift	1735.8	154.2	84.2	6.3	1.30	2.10	0.07	0.11	118.64	1552.35	1.12	43.26		53.0	85.6		48.4
Rierdon	1890.1	97.8	90.4	3.5	1.80	2.10	0.06	0.07	54.36	1606.71	1.18	43.06		64.0	74.7		50.6
Spearfish	1987.9	154.5	93.9	3.0	2.60	3.04	0.13	0.15	59.44	1666.14	1.19	42.69		50.8	59.4		50.9
Minnekahta/Opech	2142.4	100.0	96.9	1.7	3.20	3.04	0.11	0.10	31.24	1697.38	1.26	41.01		54.1	51.4		51.8
Broom Creek	2242.4	88.1	98.6	1.4	2.60	3.04	0.08	0.09	33.88	1731.26	1.30	39.93		41.0	48.0		51.7
Tyler	2330.5	73.5	100.0	2.5	1.50	2.68	0.04	0.06	48.97	1780.24	1.31	39.02		50.6	90.5		51.1
Otter	2404.0	38.1	102.5	1.5	1.50	3.62	0.02	0.05	25.40	1805.64	1.33	38.86		57.9	139.7		51.7
Kibbey Sandstone	2442.1	65.5	104.0	1.6	3.10	3.62	0.07	0.08	21.14	1826.77	1.34	38.85		74.7	87.3		51.9
Kibbey Lime	2507.6	46.3	105.6	0.9	3.00	3.62	0.05	0.06	15.44	1842.22	1.36	38.47		56.3	68.0		52.4
Madison	2553.9	135.9	106.4	2.1	3.05	3.45	0.14	0.15	44.57	1886.79	1.35	38.11		47.1	53.3		51.6
Ratcliffe	2689.9	75.0	108.5	1.5	3.05	3.45	0.08	0.08	24.58	1911.37	1.41	36.96		60.6	68.6		52.0
Frobisher	2764.8	32.3	110.0	0.7	3.05	3.45	0.03	0.04	10.59	1921.97	1.44	36.50		65.1	73.7		52.5
Fryburg	2797.1	109.7	110.7	2.4	3.05	3.45	0.11	0.12	35.98	1957.94	1.43	36.32		65.9	74.5		51.9
Lodgepole	2906.9	139.8	113.1	3.6	3.05	3.45	0.14	0.16	45.83	2003.77	1.45	35.76		79.4	89.8		51.9
Bottom of Well	3046.7		116.7														
						$\Sigma =$	1.79	2.33									
Notes												Average		56.8	75.7	53.5	48.9
1 - Thermal conductivity derived from graphical method												Wtd Average		63.1	82.3		
2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)												Shallow				54.3	29.6
3 - Weighted average of graphical thermal conductivity												Deep		55.0		52.7	51.2
4 - Weighted average of Nordeng's thermal conductivity																	
5 - Harmonic mean of thermal conductivity																	
6 - Heat flow derived from graphical method																	
7 - Heat flow derived from Equation 1 for each formation																	
8 - Heat Flow derived from Equation 1 and Nordeng's λ																	
9 - Heat flow derived from Bullard's Method																	
10 - Heat flow derived using harmonic mean method																	
11- FU/HC/FH - Fort Union Group/Hell Creek Formation/Fox Hills Formation combined																	

Summary of Heat Flow Calculations

NDIC 17317

E-M Emmel 10-3

Renville County, ND

Summary of Heat Flow Calculations

NDIC 3090

Grenora-Madison Unit 08

Williams County, ND

Formation	Depth (Z)	ΔZ	Temp (T)	ΔT	λ^1	λ_N^2	λ_{wtd}^3	λ_{Nwtd}^4	$\Delta Z_i/\lambda$	R _i	λ_{hi}^5	grad _i	Q _{graph} ⁶	Q ₂ ⁷	Q _N ⁸	Q _{Bullard} ⁹	Q _{hi} ¹⁰
	(m)		(°C)														
FU/HC/FH ¹¹	20.4	401.4	10.1	9.6	1.30	1.62	0.44	0.55	18.6	18.6	0.06	286.72		26.3	41.2		17.9
Pierre	421.8	776.9	19.7	31.7	1.15	1.62	0.04	0.06	308.8	327.4	0.42	36.66		53.1	66.2		15.4
Greenhorn	1198.8	84.4	51.4	5.0	1.00	1.80	0.02	0.04	675.6	1002.9	1.10	39.37		67.7	95.4		43.4
Mowry	1283.2	54.9	56.4	2.5	1.00	1.80	0.03	0.05	84.4	1087.4	1.12	40.65		45.2	81.4		45.7
Newcastle	1338.1	65.8	58.9	2.8	1.10	2.35	0.06	0.13	54.9	1142.2	1.11	40.84		42.5	76.6		45.5
Inyan Kara	1403.9	130.1	61.7	3.7	1.30	2.10	0.10	0.16	59.9	1202.1	1.08	40.92		31.3	66.8		44.1
Swift	1534.1	170.7	65.4	7.1	1.10	2.10	0.09	0.17	100.1	1302.2	1.05	39.86		53.9	87.1		42.0
Rierdon	1704.7	183.2	72.5	7.1	1.30	3.04	0.03	0.07	155.2	1457.4	1.07	40.02		42.6	81.4		42.7
Spearfish	1887.9	52.1	79.6	1.2	1.50	3.04	0.03	0.06	140.9	1598.3	1.16	39.90		29.7	69.4		46.1
Broom Creek	1940.1	43.9	80.8	1.4	2.00	2.68	0.13	0.17	34.7	1633.0	1.17	39.44		46.8	94.9		46.2
Tyler	1983.9	144.2	82.1	4.2	1.20	3.62	0.02	0.06	21.9	1655.0	1.12	39.26		58.7	78.6		43.9
Kibbey Lime	2128.1	40.5	86.4	0.7	2.70	3.45	0.14	0.18	120.1	1775.1	1.19	38.59		21.9	66.1		45.9
Madison	2168.7	116.0	87.1	1.8	3.05	3.45	1.32	2.00	15.0	1790.1	1.19	38.21		41.0	52.3		45.3
BOH	2284.7		88.9														
					$\Sigma =$	2.45	3.70										
Notes																	
1 - Thermal conductivity derived from graphical method																	Average
2 - Thermal conductivity used by Nordeng and Nesheim (2011) and Nordeng (2014)																	43.1
3 - Weighted average of graphical thermal conductivity																	73.6
4 - Weighted average of Nordeng's thermal conductivity																	45.5
5 - Harmonic mean of thermal conductivity																	43.1
6 - Heat flow derived from graphical method																	
7- Heat flow derived from Equation 1 for each formation																	
8 - Heat Flow derived from Equation 1 and Nordeng's λ																	
9 - Heat flow derived from Bullard's Method																	
10 - Heat flow derived using harmonic mean method																	
11- FU/HC/FH - Fort Union Group/Hell Creek Formation/Fox Hills Formation combined																	

Summary of Heat Flow Calculations

NDIC 13725

JC Woods 26H-1

Burke County, ND